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# Recent developments in millimetre-wave measurement: S-parameters and material properties

# Advances in Leakage Corrections for Onwafer S-parameter Measurements

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Microwave&THz Electronics





- Introduction
- Error terms and error models in leaky on-wafer systems
- Conventional calibration algorithms and procedures
- Latest advances in leakage correction techniques
- Conclusions and future works
- Acknowledgement



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Signal leakage in a waveguide based Sparameter test system

- Primarily inside the VNA
- Also found in the test fixture



Flowgraph showing all the possible signal paths (by D. Rytting)



#### Simplified block diagram of a VNA system by D. Rytting



750 GHz-1.1 THz VNA+Swissto12's MCK



Signal leakage in an on-wafer S-parameter test system

- Inside the VNA
- Bu primarily between the probes









#### Signal leakage exists between probes in various forms

- Radiative over the air
- Transmissive through substrate
- Direct capacitive/inductive coupling
- and it is normally
  - Frequency dependent
  - Subject to test environment
  - Affected by nature of devices under tests (DUT) e.g. electrical property and geometry





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#### The 8 & 12 error terms and the error models





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#### The 16 error terms and the model







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#### How to obtain the error terms: solve the error matrix

Error Model

Linear-in-T Form

Measured S-Parameters

**Actual S-Parameters** 

$$\begin{bmatrix} b_0 \\ b_3 \\ a_0 \\ a_3 \end{bmatrix} = \begin{bmatrix} \mathbf{T_1} & \mathbf{T_2} \\ \mathbf{T_3} & \mathbf{T_4} \end{bmatrix} \begin{bmatrix} b_1 \\ b_2 \\ a_1 \\ a_2 \end{bmatrix}$$

$$T_{1}S + T_{2} - S_{M}T_{3}S - S_{M}T_{4} = 0$$

$$S_{M} = (T_{1}S + T_{2})(T_{3}S + T_{4})^{-1}$$

 $S = (T_1 - S_M T_3)^{-1} (S_M T_4 - T_2)$ 

- 8 term model: all leakage are zeros; at least 3 equations/3 two-port standards required
- 12 term model: VNA internal leakage included; at least 4 equations/3-4 two-port standards required
- 16 term model: all leakage included; at least 4 equations/5 two-port standards required

#### Error matrix and solving the unknowns



#### 8-Term Calibration Examples

TRL & LRL	Thru (T) or Line (L) with	Unknown equal Reflect (R)	Line (L) with known
	known S-parameters	on port-1 and port-2	S <sub>11</sub> and S <sub>22</sub>
	[4 conditions]	[1 condition]	[2 conditions]
TRM & LRM	Thru (T) or Line (L) with	Unknown equal Reflect (R)	Known Match (M)
	known S-parameters	on port-1 and port-2	on port-1 and port-2
	[4 conditions]	[1 condition]	[2 conditions]
TXYZ & LXYZ	Thru (T) or Line (L) with known S-parameters [4 conditions]	3 known Reflects (XYZ) on port-1 or port-2 [3 conditions]	
Traditional	Thru (T) with	3 known Reflects (OSL)	3 known Reflect (OSL)
TOSL	known S-parameters	on port-1	on port-2
(Overdetermined)	[4 conditions]	[3 conditions]	[3 condition]
LRRM	Line (L) with known	2 unknown equal Reflects	Known match (M)
	S-parameters	(RR) on port-1 and port-2	on port-1
	[4 conditions]	[2 conditions]	[1 condition]
UXYZ	Unknown Line (U) with	3 known Reflects (XYZ)	3 known Reflects (XYZ)
	$S_{12} = S_{21}$	on port-1	on port-2
	[1 condition]	[3 conditions]	[3 conditions]

## Calibration procedure (12-term)



 STEP 1: Calibrate Port-1 & Port-2 using One-Port procedure

Open/Short/Load

- STEP 2: Connect Ports 1 & 2 together,
  - Solve for e11, e00, & (e10e01),
  - Calculate (e10e01) from  $\Delta e$
  - Measure S21M gives e30 directly S11M e00 S11Me11 - Δe e22 = e10e32 = (S21M e30)(1 - e11e22)
  - Reverse





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### The two tier interior model

**S2** 

Port 2

Port 1



Port 2

DUT

Port 1

**S1** 

Port 2

Port 1



Strictly speaking, it is an approximation, is not completely physical, and is not precisely passive.



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#### The 10 term error model





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#### The 10 term error model



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$$T = \begin{bmatrix} E_2 - E_1 E_3^{-1} E_4 & E_1 E_3^{-1} \\ -E_3^{-1} E_4 & E_3^{-1} \end{bmatrix}$$

$$x = e_{10} e_{23} - e_{13} e_{20}$$

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$$x_{1} = x_{1} e_{30} + x_{2} e_{33} & x e_{32} + x_{1} e_{30} + x_{2} e_{33} & e_{30} e_{23} - e_{33} e_{20} & e_{33} e_{10} - e_{30} e_{13} \\ x_{1} & x_{3} & e_{23} & -e_{13} \\ x_{2} & x_{4} & -e_{20} & e_{10} \end{bmatrix}$$

$$x = e_{10} e_{23} - e_{13} e_{20}$$

$$x_{1} = e_{13} e_{21} - e_{23} e_{11}$$

$$x_{2} = e_{20} e_{11} - e_{10} e_{21}$$

$$x_{3} = e_{13} e_{22} - e_{23} e_{12}$$

$$T = \begin{bmatrix} e_{01} - e_{00} e_{11} / e_{10} & -e_{00} e_{12} / e_{10} & e_{00} / e_{10} & 0 \\ -e_{21} e_{33} / e_{23} & e_{32} - e_{22} e_{33} / e_{23} & 0 & e_{33} / e_{23} \\ -e_{11} / e_{10} & -e_{12} / e_{10} & 1 / e_{10} & 0 \\ -e_{21} / e_{23} & -e_{22} / e_{23} & 0 & 1 / e_{23} \end{bmatrix}$$
10 term Errors in T matrix



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A novel 12-term error term model separating the leakage from the intrinsic device-under-test (DUT) for calibration and actual device measurements; suitable for DUT with different length from calibration standards



$$Y_{\rm CT} = Y_{\rm open||CT} - Y_{\rm open}$$
$$\Delta_Y S = (1 + S_{11})(1 + S_{22}) - S_{21}S_{12}$$
$$\Delta Y = (Y_0 + Y_{11})(Y_0 + Y_{22}) - Y_{21}Y_{12}$$

- 1. Calibrate the system at waveguide ports e.g. 2-port TRL
- 2. Extract probes' S-parameters using SOL
- 3. Measure a dummy pair e.g. Open-Open or Load-Load but not Short-Short having the same distance as a DUT
- 4. Extract the cross-talk matrix

#### Wu et al IEEE MTT 2020





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S-parameters of microwave probe pair on each side. Port 1 is a coaxial port of each probe, and port 2 is a probe tip port of each probe.

S-parameters of a 10-dB attenuator after the calibration of this paper, compared with both of simulation results and that after the calibration of SOLT (conventional 12-term error model).



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greater than 1, which is possible due to the probe launch difference between calibration and measurement.

#### An improved CoF method

- A new 12-term error model
- Only two calibration steps required
- Taking calibration planes to the access of DUTs on chip
- Less stringent standards including an undefined Thru, two undefined Reflect pairs i.e.
   Open-Open and Short-Short and one defined Load pair







Туре	Description	Definition	Quantity
Thru	Matched straight line	not required	1
Open-Open	Identical Open pair	not required	1
Short-Short	Identical Short pair	not required	1
Load-Load	Match pair	Required	1

Wang et al. IEEE MTT 2022 Early Access





Magnitude and phase of  $S_{21}$  of the mismatched attenuator corrected using different methods.

*S*-parameters of the crosstalk network between COF and the new method





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### Summary & future work



- Probe-probe crosstalk/leakage contributes more significantly at mm-Wave
- Accurate error models and calibration algorithms are desperately required
- Calibration standards should be further investigated
- New £2.6M (€3M) test cluster to be launched in April 2023
  - AWG: 128/256 GSa/s, 4/2 channels (67 GHz; extended to 330 GHz)
  - RT Oscilloscope: 128 GSa/s 4 channels (70 GHz; extended to 330 GHz)
  - 50GHz PNA-X: SA, NF, TD etc
  - Noise tuners: 2 GHz-43.5 GHz
  - Loadpull: full band
  - Frequency extender modules to (10 MHz-1.1 THz)
  - 10 inch autoprober



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