## LHCb

## The LHCb collaboration

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AbStract: The multihadron decays $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$are observed in data corresponding to an integrated luminosity of $3 \mathrm{fb}^{-1}$, collected in proton-proton collisions at centre-of-mass energies of 7 and 8 TeV by the LHCb detector. Using the decay $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$as a normalisation channel, the ratio of branching fractions is measured to be

$$
\frac{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}\right)}{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}\right)} \times \frac{\mathcal{B}\left(D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}\right)}{\mathcal{B}\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right)}=(5.35 \pm 0.21 \pm 0.16) \%,
$$

where the first uncertainty is statistical and the second systematic. The ratio of branching fractions for the $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decays is found to be

$$
\frac{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}\right)}{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}\right)} \times\left(\mathcal{B}\left(D^{*+} \rightarrow D^{+} \pi^{0}\right)+\mathcal{B}\left(D^{*+} \rightarrow D^{+} \gamma\right)\right)=(61.3 \pm 4.3 \pm 4.0) \%
$$

Keywords: B Physics, Branching fraction, Flavour Physics, Hadron-Hadron Scattering

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## 1 Introduction

Nonleptonic decays with multiple hadrons, such as $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{-} \pi^{+} \pi^{-}$, are a useful platform for testing non-perturbative quantum chromodynamics (QCD) approaches such as QCD factorisation (QCDF). At the quark level these $\Lambda_{b}^{0}$ baryon decays are mediated by the weak $b \rightarrow c \bar{c} s$ and $b \rightarrow c \bar{u} d$ transitions. ${ }^{1}$ Calculating the rates for these decays is more challenging than for their semileptonic $b \rightarrow c \ell^{-} \bar{\nu}_{\ell}$ partners, since strong interactions are present in both the hadronic initial and final states. Despite these difficulties, which are due to QCD effects, substantial progress has been made in computing hadronic two-body and quasi-two-body decays; earlier calculations [1-4] have been refined in refs. [5, 6]. These theory predictions agree well with both the CDF measurement of $\Lambda_{b}^{0}$ production and decays [7], and a similar LHCb measurement [8]. Formulated within the framework of QCDF, these predictions are calculated for several decay modes, $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+}\left(\pi^{-}, \rho^{-}, a_{1}^{-}\right)$, including exclusive modes where the intermediate resonance decays into a final state with multiple pions, e.g. $a_{1}^{-} \rightarrow \pi^{-} \pi^{-} \pi^{+}$[5]. Such decay channels contribute to the multihadron $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{-} \pi^{+} \pi^{-}$decay analysed in this study.

Final state protons and charm mesons are of particular interest in multihadron decays of beauty baryons, where the $c$-quark from the $b \rightarrow c$ transition hadronises into the final state separate from the baryon, i.e. a charm meson and a proton. This topology is not only important for charm baryon and meson spectroscopy, but also sensitive to QCD

[^0]effects in beauty baryons as well as charm-quark hadronisation. However, this topology has not been widely studied. Currently, only a few decay modes of beauty baryons with the final state configuration described above are known: $\Lambda_{b}^{0} \rightarrow D^{0} p \pi^{-}[9-11], \Lambda_{b}^{0} \rightarrow D^{0} p K^{-}$ and $\Xi_{b}^{0} \rightarrow D^{0} p K^{-}[11]$. The amplitude analysis of $\Lambda_{b}^{0} \rightarrow D^{0} p K^{-}$decays discovered a rich resonance structure allowing the study of excited charm baryons [12]. Recently, the LHCb collaboration reported an observation of the $\Lambda_{b}^{0} \rightarrow D p K^{-}$channel with a $D \rightarrow K^{\mp} \pi^{ \pm}$decay, where the state $D$ is a superposition of $D^{0}$ and $\bar{D}^{0}$ states [13]. The $C P$ asymmetry in this decay and the ratio of branching fractions for the $\Lambda_{b}^{0} \rightarrow\left(D \rightarrow K^{-} \pi^{+}\right) p K^{-}$and $\Lambda_{b}^{0} \rightarrow\left(D \rightarrow K^{+} \pi^{-}\right) p K^{-}$decays are also measured.

In this paper, the first observation of the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$multihadron decay modes is reported. The measurements are based on proton-proton ( $p p$ ) collision data, corresponding to integrated luminosities of 1 and $2 \mathrm{fb}^{-1}$ collected with the LHCb detector at center-of-mass energies of 7 and 8 TeV , respectively. The following ratios of branching fractions are reported

$$
\begin{align*}
\mathcal{R}_{D^{+}} & \equiv \frac{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}\right)}{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}\right)} \times \frac{\mathcal{B}\left(D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}\right)}{\mathcal{B}\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right)}  \tag{1.1a}\\
\mathcal{R}_{D^{*+}} & \equiv \frac{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}\right)}{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}\right)} \times \mathcal{B}\left(D^{*+} \rightarrow D^{+} \pi^{0} / \gamma\right) \tag{1.1b}
\end{align*}
$$

where $\mathcal{B}\left(D^{*+} \rightarrow D^{+} \pi^{0} / \gamma\right) \quad$ equals $\mathcal{B}\left(D^{*+} \rightarrow D^{+} \pi^{0}\right)+\mathcal{B}\left(D^{*+} \rightarrow D^{+} \gamma\right)$, and the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$mode with the $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$decay is used as the normalisation channel. No theory predictions are currently available for the decay modes $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$.

## 2 Detector and simulation

The LHCb detector $[14,15]$ is a single-arm forward spectrometer covering the pseudorapidity range $2<\eta<5$, designed for the study of particles containing $b$ or $c$ quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the $p p$ interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm , and silicon-strip detectors and straw drift tubes placed downstream of the magnet. The tracking system provides a measurement of the momentum, $p$, of charged particles with a relative uncertainty that varies from $0.5 \%$ at low momentum to $1.0 \%$ at $200 \mathrm{GeV} / c$. The minimum distance of a track to a primary $p p$ collision vertex (PV), the impact parameter (IP), is measured with a resolution of $\left(15+29 / p_{\mathrm{T}}\right) \mu \mathrm{m}$, where $p_{\mathrm{T}}$ is the component of the momentum transverse to the beam, in $\mathrm{GeV} / c$. Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors. Photons, electrons and hadrons are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers.

The online event selection is performed by a trigger system. The trigger consists of a hardware stage, based on information from the calorimeter and muon systems, followed by
a software stage, which applies a full event reconstruction [16]. The events used in this analysis are selected at the hardware stage by requiring a cluster in the calorimeters with transverse energy greater than 3.6 GeV . The software trigger requires a two-, three- or four-track secondary vertex with a large $p_{\mathrm{T}}$ sum of the particles and a significant displacement from the primary $p p$ interaction vertices (PVs). At least one charged particle should have $p_{\mathrm{T}}>1.7 \mathrm{GeV} / c$ and large $\chi_{\mathrm{IP}}^{2}$ with respect to any PV, where $\chi_{\mathrm{IP}}^{2}$ is defined as the difference in fit $\chi^{2}$ of a given PV reconstructed with and without the considered track. A multivariate algorithm is used for the identification of secondary vertices consistent with the decay of a $b$ hadron [17].

Simulated collision events are used to model the effects of the detector acceptance and the imposed selection requirements for signal decay modes. In the simulation, $p p$ collisions are generated using Pythia [18] with a specific LHCb configuration [19]. The $p_{\mathrm{T}}$ and rapidity spectra of the $\Lambda_{b}^{0}$ baryons in simulation are corrected to match those for the reconstructed $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays, which constitute a large data sample used for normalisation. Decays of unstable particles are described by EvtGen [20], in which final-state radiation is generated using Рнотоs [21]. A four-body phase-space decay model is used for the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decay modes. The decays $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$are simulated as a mixture of decays via intermediate excited $\Sigma_{c}^{(*)}$ resonances $\Lambda_{b}^{0} \rightarrow\left(\Sigma_{c}^{(*)++} \rightarrow \Lambda_{c}^{+} \pi^{+}\right) \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow\left(\Sigma_{c}^{(*) 0} \rightarrow \Lambda_{c}^{+} \pi^{-}\right) \pi^{+} \pi^{-}$; excited $\Lambda_{c}^{+}$baryons $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}(2595)^{+} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-}\right) \pi^{-}$and $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}(2625)^{+} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-}\right) \pi^{-}$; or light unflavoured hadrons $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} a_{1}^{-}, \Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \rho^{0} \pi^{-}$, and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} f_{2}(1270) \pi^{-}$. The decay models are corrected to reproduce the ten two- and three-body mass distributions from the signals observed in data. The corrections are applied subsequently for ten mass distributions in several iterations untill convergence is achieved. The interaction of the generated particles with the detector and its response are implemented using the Geant4 toolkit [22, 23] as described in ref. [24]. To account for imperfections in the simulation of charged-particle reconstruction, the track reconstruction efficiency determined from simulation is corrected using control channels in data [25].

## 3 Event selection

The $\quad \Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-} \quad$ and $\quad \Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-} \quad$ decays are reconstructed using the $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$and $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$decay channels, respectively. The selection begins with good-quality reconstructed charged tracks that are inconsistent with being produced in a $p p$ interaction vertex. Kaons, pions and protons, identified using information from the RICH detectors [26, 27], are selected from well-reconstructed tracks within the acceptance of the spectrometer with $p_{\mathrm{T}}>100 \mathrm{MeV} / c$. To allow for efficient particle identification, kaons and pions are required to have a momentum between 3 and $120 \mathrm{GeV} /$ c, while protons must have momenta between 9 and $120 \mathrm{GeV} / c$.

The $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$and $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$candidates are reconstructed from selected kaon, pion and proton candidates requiring $K^{-} \pi^{+} \pi^{+}$and $p K^{-} \pi^{+}$combinations to form a good quality three-prong common vertex, which is significantly separated from any PV. A reconstructed mass for the $D^{+}$and $\Lambda_{c}^{+}$candidates is required to be within $\pm 34$ and $\pm 24 \mathrm{MeV} / c^{2}$ mass windows around the known masses of the $D^{+}$and $\Lambda_{c}^{+}$hadrons [28],
respectively. These mass ranges correspond to approximately $\pm 4 \sigma_{m}$ regions, where $\sigma_{m}$ is the mass resolution. Three-track combinations are also formed of $p \pi^{-} \pi^{-}$and $\pi^{+} \pi^{-} \pi^{-}$ particle triplets, and are required to have a good-quality common vertex that is distinct from the PV. The mass of these $p \pi^{-} \pi^{-}$and $\pi^{+} \pi^{-} \pi^{-}$combinations are required to be below 4 and $3 \mathrm{GeV} / c^{2}$, respectively.

The reconstructed $D^{+}$and $\Lambda_{c}^{+}$candidates are combined with selected $p \pi^{-} \pi^{-}$and $\pi^{-} \pi^{+} \pi^{-}$candidates to form $\Lambda_{b}^{0}$ candidates. Only $\Lambda_{b}^{0}$ candidates with a transverse momentum above $3 \mathrm{GeV} / c$ are selected for further analysis. To improve the mass resolution for the $\Lambda_{b}^{0}$ candidates, a kinematic fit is performed [29], which constrains the mass of the $D^{+}$and $\Lambda_{c}^{+}$hadron candidates to their known masses [28] and requires the $\Lambda_{b}^{0}$ candidate to originate from its associated PV. A requirement on the $\chi^{2}$ from this fit further suppresses background. The reconstructed $\Lambda_{b}^{0}$ decay vertex is required to be distinct from the PV, with the proper decay time of the $\Lambda_{b}^{0}$ candidate restricted to be above $100 \mu \mathrm{~m} / c$. The proper decay time of the $D^{+}$and $\Lambda_{c}^{+}$candidates calculated with respect to the reconstructed $\Lambda_{b}^{0}$ decay vertex is required to be positive within the resolution. These two requirements reduce the background contributions from charmed hadrons produced directly in the $p p$ interaction, and random combinations of tracks forming fake $D^{+}$or $\Lambda_{c}^{+}$candidates. At least one track from the selected $\Lambda_{b}^{0}$ candidate must be matched with a high energy deposit in the calorimeter system, used in the hardware-trigger stage. The mass distributions for selected $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$ and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$candidates are shown in figures 1 and 2 , respectively.

## 4 Signal determination

The $D^{+} p \pi^{-} \pi^{-}$mass distribution shown in figure 1 exhibits a narrow peak corresponding to the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decay. In addition, a structure around $5.4-5.5 \mathrm{GeV} / c^{2}$ is visible. This structure corresponds to the $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decay followed by the decay of the $D^{*+}$ meson into $D^{+} \pi^{0}$ or $D^{+} \gamma$ states, where the neutral particle is not reconstructed. An extended unbinned maximum-likelihood fit to the $D^{+} p \pi^{-} \pi^{-}$mass distribution is performed using a function consisting of a sum of the four following contributions.

- A $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$component, parameterised by a modified Gaussian function with power-law tails on both sides of the distribution [30, 31]. The tail parameters are fixed to values obtained from simulation, while the width and peak position are allowed to vary in the fit.
- A $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$component, followed by $D^{*+} \rightarrow D^{+} \pi^{0}$ and $D^{*+} \rightarrow D^{+} \gamma$ decays. The shape of the component is taken from simulation and modified by a first order positive polynomial which accounts for the unknown $\Lambda_{b}^{0}$ decay model. The parameters of the polynomial function are allowed to vary in the fit.
- A $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-} \pi^{0}$ component, where the $\pi^{0}$ meson is undetected. The shape is also taken from simulation.
- A combinatorial-background component, parameterised with a positive monotonicallydecreasing third-order polynomial function.


Figure 1. Mass distribution for selected $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$candidates. The projection of an unbinned likelihood fit, described in the text, is superimposed.

The fit result is overlaid on figure 1. The signal yields for the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays are presented in table 1. A similar four-component function is used to describe the $\Lambda_{c}^{+} \pi^{+} \pi^{+} \pi^{-}$mass spectrum.

- A $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$component, parameterised with a modified Gaussian function with power-law tails on both sides of the distribution [30, 31]. The tail parameters are fixed to values obtained from simulation, while the width and position are allowed to vary in the fit.
- A $\Lambda_{b}^{0} \rightarrow \Sigma_{c}^{(*)+} \pi^{+} \pi^{-} \pi^{-}$component, followed by a $\Sigma_{c}^{(*)+} \rightarrow \Lambda_{c}^{+} \pi^{0}$ decay with an undetected $\pi^{0}$ meson. The shape is taken from simulation.
- A $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-} \pi^{0}$ component, where the $\pi^{0}$ meson is undetected. The shape is taken from simulation based on a phase-space decay model.
- A combinatorial-background component, parameterised with a positive monotonicallydecreasing third-order polynomial function.


Figure 2. Mass distribution for selected $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$candidates. The projection of an unbinned likelihood fit, described in the text, is superimposed.

| Decay mode | $N^{\mathrm{fit}}$ | $N^{\mathrm{cor}}$ |
| :--- | :---: | :---: |
|  |  |  |
| $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$ | $1933 \pm 56$ | $1542 \pm 60$ |
| $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$ | $862 \pm 55$ | $875 \pm 55$ |
| $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$ | $(26.51 \pm 0.18) \times 10^{3}$ | $(25.91 \pm 0.18) \times 10^{3}$ |

Table 1. Yields, $N^{\text {fit }}$, for the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}, \Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays evaluated from fits to the $D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$mass spectra. The yields with all corrections described in the text, $N^{\text {cor }}$, are also given. The uncertainties are statistical only.

The fit result is overlaid on figure 2 and the signal yield for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays is presented in table 1.

Several corrections, described below, are applied to the fitted yields. Since the $D^{+} p \pi^{-} \pi^{-}$ channel with a $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$decay and the $\Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$channel with a $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$ decay consist of the same final state particles, there can be cross-feed between the two
where true $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays are misreconstructed as $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decays. This contribution is studied using background-subtracted $p K^{-} \pi^{+}$mass distributions from $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decays. The sPlot technique [32] is applied to the result of the fit described above, using the $D^{+} p \pi^{-} \pi^{-}$mass as the discriminating variable. The resulting background-subtracted $p K^{-} \pi_{1,2}^{+}$mass spectra from the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$channel with $D^{+} \rightarrow K^{-} \pi_{1}^{+} \pi_{2}^{+}$decays are shown in figure 3. The peaks at the known mass of the $\Lambda_{c}^{+}$baryon correspond to true $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays reconstructed as $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decays. Fits are performed to these distributions with a function consisting of the following two terms.

- The $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right) \pi^{+} \pi^{-} \pi^{-}$contribution is modelled by a Gaussian function with the mean value and width taken from the fit to the $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$signal from $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right) \pi^{+} \pi^{-} \pi^{-}$decays.
- A first-order polynomial term models the baseline background from $\Lambda_{b}^{0}$ baryon decays without a $\Lambda_{c}^{+}$baryon in the final state.

This fit yields $395 \pm 23$ misreconstructed $\Lambda_{b}^{0} \rightarrow\left(D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}\right) p \pi^{-} \pi^{-}$candidates, which are subtracted from the total fit yield of the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$mode. No analogous pattern is observed in the background-subtracted $p K^{-} \pi^{+}$mass spectra from $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays. Possible cross-feed from $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$decays in the $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right) \pi^{+} \pi^{-} \pi^{-}$normalisation signal is found to be negligible.

The background-subtracted $\pi^{+} \pi^{-} \pi^{-}$mass spectrum from $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays is shown in figure 4 (left), where background subtraction is performed with the sPlot technique using the $\Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$mass as the discriminating variable. A small contribution from $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} D_{s}^{-}$decays, followed by the $D_{s}^{-} \rightarrow \pi^{+} \pi^{-} \pi^{-}$decay, is visible in the $\pi^{+} \pi^{-} \pi^{-}$mass spectrum [33]. A fit to the background-subtracted $\pi^{+} \pi^{-} \pi^{-}$mass distribution is performed with a Gaussian function summed with a positive first-order polynomial function. The Gaussian mean is set to the known mass of the $D_{s}^{-}$meson [28], while the resolution is taken from the fit to a larger data sample available at an earlier stage of the selection. The polynomial function models the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays without an intermediate $D_{s}^{-}$meson. The fit yields $176 \pm 25 \Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} D_{s}^{-}$decays, which are subtracted from the total fitted yield of the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays.

A small fraction of $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi_{1}^{+}\right) \pi_{2}^{+} \pi^{-} \pi^{-}$decays satisfies all selection criteria after the interchange of two positive pions, $\pi_{1}^{+} \leftrightarrow \pi_{2}^{+}$, causing the same six-track combination to be reconstructed twice. This effect is studied using the background-subtracted $p K^{-} \pi_{2}^{+}$mass distribution from the selected $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi_{1}^{+}\right) \pi_{2}^{+} \pi^{-} \pi^{-}$decays, shown in figure 4 (right). Duplicate candidates appear near the known mass of the $\Lambda_{c}^{+}$baryon. A fit to the $p K^{-} \pi_{2}^{+}$mass distribution is performed using a Gaussian function for the $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi_{2}^{+}\right) \pi_{1}^{+} \pi^{-} \pi^{-}$decays and a first-order polynomial function for the $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi_{1}^{+}\right) \pi_{2}^{+} \pi^{-} \pi^{-}$decays. The mean and width of the Gaussian function are taken from a fit to the $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$candidates from $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right) \pi^{+} \pi^{-} \pi^{-}$decays. The $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi_{2}^{+}\right) \pi_{1}^{+} \pi^{-} \pi^{-}$yield is $416 \pm 32$, and is subtracted from the total fit yield of the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays.


Figure 3. Background-subtracted $p K^{-} \pi_{1,2}^{+}$mass spectra from the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$channel with $D^{+} \rightarrow K^{-} \pi_{1}^{+} \pi_{2}^{+}$decays.


Figure 4. Background-subtracted (left) $\pi^{+} \pi^{-} \pi^{-}$mass distribution from $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays and (right) $p K^{-} \pi_{2}^{+}$mass distribution from $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi_{1}^{+}\right) \pi_{2}^{+} \pi^{-} \pi^{-}$decays. The results of the fits described in text are overlaid.

Possible biases in the yields of the $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays from the relevant fits are studied using pseudoexperiments. The largest bias is found for the yield of $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays and it is $1.5 \%$. For the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays the corresponding biases are much smaller. The final yields, after all corrections described above are applied, are given in table 1 for the $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$ and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays.

## 5 Efficiency and ratios of branching fractions

The ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$, defined by eq. (1.1) are calculated as

$$
\begin{equation*}
\mathcal{R}_{D^{+}}=\frac{N_{\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}}^{\text {cor }}}{N_{\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}}^{\text {cor }}} \times \frac{\varepsilon_{\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}}}{\varepsilon_{\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}}} \tag{5.1a}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathcal{R}_{D^{*+}}=\frac{N_{\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}}^{\mathrm{cor}}}{N_{\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}}^{\text {cor }}} \times \frac{\varepsilon_{\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}}}{\varepsilon_{\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}}}, \tag{5.1b}
\end{equation*}
$$

where $N_{X}^{\text {cor }}$ is the corrected signal yield for decay mode $X$, as per table 1 , and $\varepsilon_{X}$ is the corresponding efficiency. This efficiency is defined as a product of the detector acceptance $\varepsilon^{\text {acc }}$, reconstruction and selection efficiency $\varepsilon^{\text {rec\&sel }}$, efficiency of the hardware stage of the trigger $\varepsilon^{\operatorname{trg}}$ and the hadron-identification efficiency $\varepsilon^{\text {PID }}$,

$$
\begin{equation*}
\varepsilon=\varepsilon^{\mathrm{acc}} \varepsilon^{\mathrm{rec} \& s e l} \varepsilon^{\operatorname{trg}} \varepsilon^{\mathrm{PID}}, \tag{5.2}
\end{equation*}
$$

where each subsequent efficiency is defined with respect to the product of previous efficiencies. The detector acceptance, and reconstruction and selection efficiency, are determined using the simulation samples described in section 2. The reconstruction and selection efficiency is corrected for a small difference in the track reconstruction efficiency between data and simulation [25]. The trigger efficiency is calculated from single-particle hadrontrigger efficiencies, which are determined separately for protons, kaons and pions from a large $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right) \pi^{-}$data sample. The hadron-identification efficiency is a combination of single-particle identification efficiencies for protons, kaons and pions determined with large calibration samples of $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}, \Lambda \rightarrow p \pi^{-}, D^{*+} \rightarrow\left(D^{0} \rightarrow K^{-} \pi^{+}\right) \pi^{+}$, $D_{s}^{+} \rightarrow\left(\phi \rightarrow K^{+} K^{-}\right) \pi^{+}$and $K_{\mathrm{S}}^{0} \rightarrow \pi^{+} \pi^{-}$decays in data [27]. The ratios of efficiencies are,

$$
\begin{equation*}
\frac{\varepsilon_{\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}}}{\varepsilon_{\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}}}=1.11 \pm 0.01 \tag{5.3a}
\end{equation*}
$$

and

$$
\begin{equation*}
\frac{\varepsilon_{\Lambda_{b}^{0} \rightarrow D^{*+}+p \pi^{-} \pi^{-}}}{\varepsilon_{\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}}}=0.93 \pm 0.01, \tag{5.3b}
\end{equation*}
$$

where the uncertainties arise from the finite size of the simulation samples. Using the corrected yields from table 1 and efficiencies from eq. (5.3), the ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ are found to be

$$
\begin{equation*}
\mathcal{R}_{D^{+}}=(5.35 \pm 0.21) \% \tag{5.4a}
\end{equation*}
$$

and

$$
\begin{equation*}
\mathcal{R}_{D^{*+}}=(61.3 \pm 4.3) \%, \tag{5.4b}
\end{equation*}
$$

| Source | $\sigma_{\mathcal{R}_{D^{+}}}[\%]$ | $\sigma_{\mathcal{R}_{D^{*+}}}[\%]$ |
| :--- | :---: | :---: |
| Fit model | 1.5 |  |
| Multiple candidates | 0.8 | 5.7 |
| $\Lambda_{b}^{0}$ kinematic spectra | 0.2 | 0.7 |
| $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$decay model | 0.1 | 0.4 |
| $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decay model | 0.3 | 0.2 |
| Hadron identification | 0.7 | - |
| Tracking efficiency | 0.2 | 0.5 |
| Hardware-trigger efficiency | 0.9 | 0.0 |
| Data-simulation difference | 1.9 | 0.5 |
| Simulation samples size | 0.8 | 2.8 |
| Total | 2.9 | 0.9 |

Table 2. Relative systematic uncertainties for the ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$. The total uncertainty is obtained by summing all terms in quadrature.
where the uncertainties are statistical only. Systematic uncertainties are discussed in section 6 .

The background-subtracted two- and three-body mass spectra from the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$ and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays are shown in figures 5 through 8 with the expectation from phase-space simulated decays overlaid. The sPlot technique [32] is used for background subtraction using the $\Lambda_{b}^{0}$ candidate mass as a discriminating variable. The analogous distributions for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays are shown in appendix A; corresponding distributions from the corrected simulation samples, used for evaluation of the efficiencies, are also shown. Large deviations between data and phase-space based simulation are observed, demonstrating a rich structure of intermediate resonances for the decay of this study.

## 6 Systematic uncertainties

Due to the shared analysis techniques used to determine the yields for the $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$ and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays, many systematic uncertainties cancel for the ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$. The remaining contributions to systematic uncertainty are summarised in table 2 and discussed below.

An important source of systematic uncertainty on the ratios of the branching fractions arises from the imperfect knowledge of the mass shapes of the signal and background components used in the fits. To estimate this uncertainty, several alternative models for the signal and background components are tested. For the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$signal shapes the tail parameters of modified Gaussian functions are varied within uncertainties,


Figure 5. Background-subtracted $D^{+} p, D^{+} \pi^{-} \pi^{-}, p \pi^{-} \pi^{-}, \pi^{-} \pi^{-}$, and maximum and minimum $p \pi^{-}$mass spectra for $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decays. Expectations from phase-space (phsp.) and corrected (corr.) simulation are overlaid.


Figure 6. Background-subtracted maximum and minimum $D^{+} p \pi^{-}$, and maximum and minimum $D^{+} \pi^{-}$mass spectra for $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$decays. Expectations from phase-space (phsp.) and corrected (corr.) simulation are overlaid.


Figure 7. Background-subtracted $D^{+} p, D^{+} \pi^{-} \pi^{-}, p \pi^{-} \pi^{-}, \pi^{-} \pi^{-}$, and maximum and minimum $p \pi^{-}$mass spectra for $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays. Expectations from phase-space (phsp.) and corrected (corr.) simulation are overlaid.


Figure 8. Background-subtracted maximum and minimum $D^{+} p \pi^{-}$, and maximum and minimum $D^{+} \pi^{-}$mass spectra for $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays. Expectations from phase-space (phsp.) and corrected (corr.) simulation are overlaid.
determined from fits to corresponding simulation samples. The order of the positive mono-tonically-decreasing polynomial function, used for modelling of the background components, is varied between two and four. The ratio of branching fractions for the $D^{*+} \rightarrow D^{+} \gamma$ and $D^{*+} \rightarrow D^{+} \pi^{0}$ decays affects the shape of the $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$component. This ratio is varied within the known uncertainty $[28,34,35]$. For the $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$fit component, the polynomial factor that modifies the shape obtained from the simulation is removed. To account for the unknown resonance structure for the $\Lambda_{b}^{0} \rightarrow D^{+} \pi^{+} \pi^{-} \pi^{-} \pi^{0}$, $\Lambda_{b}^{0} \rightarrow \Sigma_{c}^{(*)+} \pi^{+} \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-} \pi^{0}$ decays, the corresponding fit components, determined from simulation, have been modified by the positive-definite linear polynomial functions. The parameters of these polynomial functions are allowed to vary in the fits. For each alternative model the ratio of event yields is determined, and the maximal deviation with respect to the default model is taken as the systematic uncertainty. This uncertainty is $1.5 \%$ and $5.7 \%$ for the ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*}}$, respectively.

A small fraction of events contain multiple $\Lambda_{b}^{0}$ candidates. These $\Lambda_{b}^{0}$ candidates have an approximately uniform mass distribution between 5.3 and $6.0 \mathrm{GeV} / c^{2}$. To estimate the uncertainty associated with the presence of multiple $\Lambda_{b}^{0}$ candidates, a single random $\Lambda_{b}^{0}$ candidate is kept, while the other candidates are discarded and the ratios of the event yields are measured. This procedure is repeated for multiple trials to mitigate the effects of statistical fluctuations. The differences between the original mean values of $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ and the values obtained using randomisation are found to be $0.8 \%$ and $0.7 \%$, respectively. These differences are taken as systematic uncertainty associated with the selection of multiple candidates.

The transverse momentum and rapidity spectra of $\Lambda_{b}^{0}$ baryons in the simulation samples are corrected to reproduce those observed for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$signal in data. This correction is a source of additional uncertainty, which is evaluated with several sets of corrections obtained using different interval schemes for the $p_{\mathrm{T}}$ and rapidity distributions of the $\Lambda_{b}^{0}$ candidates. These corrections are applied to the simulation samples and maximal deviations of $0.2 \%$ and $0.4 \%$ are observed for the ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*}}$, respectively. These deviations are set as the systematic uncertainty due to imperfect knowledge of the production spectra of the $\Lambda_{b}^{0}$ baryons.

The simulated $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}, \Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$samples are corrected to reproduce the two- and three-body signal mass distributions observed in data. Due to a large number of variables and their correlations, the method requires several iterations to converge. The corrections made for binned distributions are illustrated in figures 5 through 8 for the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}, \Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$samples and figures 9 and 10 for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$sample. The correction procedure has been further validated by comparison of simulation and data for multiple randomly constructed linear combinations of the ten mass variables. To estimate the systematic uncertainty related to the imperfect knowledge of the decay model for $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays, the number of iterations is varied. The differences with respect to the baseline results for the $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ ratios are assigned as systematic uncertainty due to the imperfect knowledge of the $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decay models.

The hadron-identification efficiency for protons, kaons and pions is estimated using large calibration samples. The uncertainty due to the finite size of the calibration samples is
propagated to the ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ using pseudoexperiments. The obtained variations of $0.7 \%$ and $0.5 \%$ for the $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ ratios, respectively, are used as the systematic uncertainty associated to the hadron identification.

There are residual differences in the reconstruction efficiency of charged-particle tracks that do not cancel completely in the ratio due to small differences in the kinematic distributions of the final-state particles. The track-finding efficiencies obtained from simulation samples are corrected using calibration modes [25]. The uncertainties related to the efficiency correction factors are propagated to the ratios of the total efficiencies using pseudoexperiments and are determined as $0.2 \%$ and smaller than $0.1 \%$ for the $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ ratios, respectively. These values are taken as the systematic uncertainty associated with the tracking efficiency.

The hardware-trigger efficiency for protons, kaons and pions is estimated using a large $\Lambda_{b}^{0} \rightarrow\left(\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}\right) \pi^{-}$calibration sample. Efficiencies from alternative calibration samples, e.g. $D^{*+} \rightarrow\left(D^{0} \rightarrow K^{-} \pi^{+}\right) \pi^{+}$decays, yield $0.9 \%$ and $0.5 \%$ variations for the $\mathcal{R}_{D^{+}}$ and $\mathcal{R}_{D^{*+}}$ ratios, respectively. These variations are taken as the systematic uncertainty due to the hardware-trigger efficiency.

The stability of the results is checked by changing the selection criteria on transverse momenta for the final state hadrons, the $\chi^{2}$ from the kinematic fit and decay time for $\Lambda_{b}^{0}$ candidates. The ratios $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ vary by up to $1.9 \%$ and $2.8 \%$, respectively, and these variation are conservatively assigned as a systematic uncertainty due to data-simulation differences not considered elsewhere. Finally, the $0.8 \%$ and $0.9 \%$ relative uncertainties from eq. (5.3) are assigned as a systematic uncertainty due to the finite size of the simulated samples for the $\mathcal{R}_{D^{+}}$and $\mathcal{R}_{D^{*+}}$ ratios, respectively.

## 7 Results and summary

The decays $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$are observed using data collected with the LHCb detector in proton-proton collisions corresponding to 1 and $2 \mathrm{fb}^{-1}$ of integrated luminosity at centre-of-mass energies of 7 and 8 TeV , respectively. Both decay modes belong to the relatively unexplored class of beauty-baryon decays where the $c$-quark from the $b \rightarrow c$ transition hadronises into the final state separate from the baryon, i.e. a charm meson and a proton. These multihadron decays exhibit a rich resonance structure.

Using the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decay as a normalisation channel, the ratios of branching fractions defined by eq. (1.1) are measured to be

$$
\mathcal{R}_{D^{+}}=(5.35 \pm 0.21 \pm 0.16) \%
$$

and

$$
\mathcal{R}_{D^{*+}}=(61.3 \pm 4.3 \pm 4.0) \%,
$$

where the first uncertainty is statistical and the second systematic. Using known branching fractions for the $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$and $\Lambda_{c}^{+} \rightarrow p K^{-} \pi^{+}$decays [28] the ratio of branching fractions for the $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays is found to be

$$
\frac{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}\right)}{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}\right)}=(3.58 \pm 0.14 \pm 0.11 \pm 0.19) \%,
$$

where the last uncertainty is due to imprecise knowledge of the branching fractions for the $\Lambda_{c}^{+}$and $D^{+}$hadrons.

The relative rate for $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{+} \pi^{+}$and $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{+} \pi^{+}$decays $r_{D^{*}}$ is defined as

$$
r_{D^{*+}} \equiv \frac{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{+} \pi^{+}\right)}{\mathcal{B}\left(\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{+} \pi^{+}\right)}=\frac{\mathcal{R}_{D^{*+}}}{\mathcal{B}\left(D^{*+} \rightarrow D^{+} \pi^{0} / \gamma\right)} .
$$

Using the known branching fractions of the $D^{*+}$ meson [28], the ratio $r_{D^{*+}}$ is $1.90 \pm 0.19$. For multihadron $b \rightarrow c$ decays with a large energy release, a relative yield of the $D^{*+}$ and $D^{+}$mesons is expected to be similar to one for the $D^{*+}$ and $D^{+}$mesons produced via a charm quark fragmentation in high-energy hadron or $e^{+} e^{-}$interactions. A naïve spin-counting rule $[36,37]$ predicts the ratio $r_{D^{*+}}$ to be as large as 3 . The relative production of $D^{*+}$ and $D^{+}$mesons produced promptly in $p p$ collisions at $\sqrt{s}=5,7$ and 13 TeV is estimated using the cross sections of directly produced $D^{*+}$ and $D^{+}$mesons, $\sigma_{p p \rightarrow D^{*+} X}^{\text {direct }}$ and $\sigma_{p p \rightarrow D^{+}}^{\text {direct }}$, as

$$
r_{D^{*+}}^{p p} \equiv \frac{\sigma_{p p \rightarrow D^{*+X}}^{\text {direct }}}{\sigma_{p p \rightarrow D^{+} X}^{\text {direct }}} \approx \frac{\sigma_{p p \rightarrow D^{*+} X}}{\sigma_{p p \rightarrow D^{+} X}-\mathcal{B}\left(D^{*+} \rightarrow D^{+} \pi^{0} / \gamma\right) \times \sigma_{p p \rightarrow D^{*+} X}},
$$

where $\sigma_{p p \rightarrow D^{*+}}$ and $\sigma_{p p \rightarrow D^{+} X}$ are the measured inclusive cross sections of the promptly produced $D^{*+}$ and $D^{+}$mesons. Assuming an independent fragmentation of the $c$ quark into $D^{*+}$ and $D^{+}$mesons in direct production, and averaging $r_{D^{*+}}^{\mathrm{pp}}$ over the different proton collision energies of 5,7 , and $13 \mathrm{TeV}[38-40]$, the value $r_{D^{*+}}^{p p}$ is $1.5 \pm 0.1$. The obtained value is smaller than the value of $r_{D^{*+}}$ obtained from the $\Lambda_{b}^{0} \rightarrow D^{(*)+} p \pi^{-} \pi^{-}$decays, but consistent within two standard deviations. The value for the ratio of production cross-sections of $D^{*+}$ and $D^{+}$mesons in $e^{+} e^{-}$collisions, $r_{D^{*}}^{e^{+} e^{-}}=1.86 \pm 0.16$, from ref. [37] is obtained from a combination of measurements performed by the CLEO [41], ARGUS [42], ALEPH [43] and VENUS [44] collaborations analysing data from high energy $e^{+} e^{-}$annihilation. The similarity between these values indicates a possible correspondence between direct charm-meson production and fragmentation, and charm-meson production in the multihadron decays of beauty hadrons.

Analysis of the $\Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$spectra shows that $\Lambda_{b}^{0} \rightarrow \Sigma_{c}^{(*)+} \pi^{+} \pi^{-} \pi^{-}$decays are largely suppressed with respect to $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays, see figure 2 . The relative production of charmed $\Sigma_{c}^{(*)+}$ and $\Lambda_{c}^{+}$baryons exhibits the same trend both in $e^{+} e^{-}$annihilation [45] and in high energy hadroproduction [46]. From these measurements, a consistent picture emerges where formation and production of a light isoscalar diquark that is a scalar is more favourable during the hadronisation of heavy charm quarks, than a light isovector diquark that is an axial vector [47-49]. This observation supports the diquark model for heavy-flavor baryon structure and production [50].

In conclusion, $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$and $\Lambda_{b}^{0} \rightarrow D^{*+} p \pi^{-} \pi^{-}$decays are observed for the first time and their relative branching ratios are measured. Both these decays, and the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays used in this analysis as a normalisation channel, demonstrate a rich resonance structure. A similarity between prompt charm-meson production and charm-meson production from multihadron decays of $\Lambda_{b}^{0}$ baryons is observed. In the fu-
ture, the observed decay $\Lambda_{b}^{0} \rightarrow D^{+} p \pi^{-} \pi^{-}$can serve as a normalisation mode for studies of similar rare decays, e.g. $\Xi_{b}^{0} \rightarrow D^{+} p K^{-} \pi^{-}$and $\Xi_{b}^{0} \rightarrow D^{*+} p K^{-} \pi^{-}$decays.

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Figure 9. Background-subtracted maximum and minimum $\Lambda_{c}^{+} \pi^{+} \pi^{-}$, and maximum and minimum $\pi^{+} \pi^{-}$mass spectra for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays. Expectations from uncorrected and corrected (corr.) simulation are overlaid.

## A Mass spectra for $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays

Background-subtracted two- and three-body mass spectra for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays are shown in figures 9 and 10. A rich structure of intermediate resonances is visible.


Figure 10. Background-subtracted $\pi^{-} \pi^{-}, \Lambda_{c}^{+} \pi^{+}, \Lambda_{c}^{+} \pi^{-} \pi^{-}, \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$, and maximum and minimum $\Lambda_{c}^{+} \pi^{-}$mass spectra for the $\Lambda_{b}^{0} \rightarrow \Lambda_{c}^{+} \pi^{+} \pi^{-} \pi^{-}$decays. Expectations from uncorrected and corrected (corr.) simulation are overlaid.

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[^0]:    ${ }^{1}$ The inclusion of charge-conjugate processes is implied throughout the paper.

