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1 **A non-structural fuzzy decision method developed for**
2 **organic Rankine cycles used in liquid-dominated**
3 **geothermal fields of medium/high temperature**

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Abstract

A reliable decision-making method is of great importance for the designing of a practical and efficient organic Rankine cycle (ORC) system employed to exploit geothermal energy. This paper develops a three-level non-structural fuzzy decision algorithm for the comprehensive evaluation of a geo-fluid driven trans-critical ORC (TORC) system on the basis of a progressive system performance hierarchy, involving environmental characteristics, safety, thermodynamic and techno-economic performance. Two representative geothermal reservoirs with medium (GR-I) and high (GR-II) temperature are investigated to realize and validate the proposed method. Four mathematical models and six working fluids with thirteen indexes are developed to fulfill the performance evaluation and decision-making courses. Parametric analysis results of the decision criteria are conducted including specific net out power (AP_{net}), thermal efficiency (η_t), exergy efficiency (η_e), heat transfer area per net output power (APR) and electricity production cost (EPC), and the different performance of TORC for GR-I and GR-II are fully revealed. As for the GR-I, the result of the three-level fuzzy decision ranking order is R142b, R134a, R290, R1270, R227ea and R143a. In regard to the GR-II, it's R142b, R1270, R134a, R290, R227ea and R143a. Both show that R142b performs best. In the GR-I and GR-II, R142b obtains the maximal AP_{net} of 110.94kW/(kg·s⁻¹) and 198.14kW/(kg·s⁻¹), the maximal η_t of 14.05% and 14.43%, the maximal η_e of 51.42% and 42.90%, the minimal APR of 0.262(m²/kW) and 0.185(m²/kW), the minimal EPC of 0.030(\$/(kW·h)) and 0.022(\$/(kW·h)).

32 Summarily, this three-level fuzzy decision evaluation method can provide
33 important guidance and decisive solution by concisely display the pros and cons for
34 each ORC scheme of geothermal resource utilization.

35 **Keywords:** Geothermal energy; Trans-critical ORC; Three-level performance
36 evaluation; non-structural fuzzy decision method

Introduction

Dramatic increase in energy consumption attributes to the fast population expansion and economic growth. A large proportion of energy supply for electricity is currently generated by the combustion of organic fuels, which leads to the growing greenhouse effect and air pollution concerns. For the purpose of human society sustainable progress, renewable resource like geothermal is capable of providing the majority of activities energy with power production, heating and cooling applications [1]. However, the cumulative installed geothermal power capacity in the globe is only increasing from 7.92GW at 2001 to 13.93GW at 2019, which is far away from the growth rate of solar and wind [2]. The conflict between the huge reserve and exploitation of geothermal resources lies in the expensive initial investments [3]. Besides that, the geothermal utilization also relies on the public awareness of environment protection as well as the efficiency enhancement of technologies [1].

51 The organic Rankine cycle (ORC) has been regarded as a preferred rational
52 solution to harvesting energy from all kinds of heat sources such as waste heat and
53 geothermal reservoirs [4]. Studies on ORC-based waste heat system are devoted to
54 optimizing the engine performance. Liang et al. [5] proposed a small-scale waste
55 heat driven cooling system which integrated supercritical CO₂ power cycle and
56 trans-critical CO₂ refrigeration cycle to recover the waste heat from internal
57 combustion engine and provide cooling energy for refrigerated truck. Li et al. [6]
58 presented a novel framework for analyzing the off-design performance of CO₂
59 trans-critical power cycle and applied in the heavy-duty truck engine. Song et al. [7]
60 conducted a one-dimensional off-design performance analysis of ORC system by
61 optimizing the turbine aerodynamic model. Wang et al. [8] investigated the part-load
62 performance of ORC system based on the engine waste heat recovery with varying
63 evaporation pressure, condensing condition, working fluid and cycle structure,
64 which revealed that the slower the output power decrease, the better the
65 performance.

66 Normally, the geothermal heat is categorized as high, medium and low
67 temperature with temperature ranges of $>220^{\circ}\text{C}$, $220\text{-}100^{\circ}\text{C}$ and $100\text{-}70^{\circ}\text{C}$,
68 respectively [9]. The thermodynamic as well as the techno-economic indicators are
69 the major criteria for making investment decisions, which show direct relevance
70 with the utilization benefit of geothermal energy. Summarizing from previous work
71 about geothermal ORC system, researchers are committed to simulating the actual
72 operating process for improving the system thermodynamic and economic
73 performance. Astolfi et al. [10, 11] completed thermodynamic and techno-economic
74 assessments of the ORCs (subcritical, trans-critical, saturated, superheated,
75 regenerative and non-regenerative) for medium temperature geothermal brines.
76 Regarding cycle efficiency and electricity cost as objective functions, the
77 optimization results suggested deploying different cycle layouts that needed to
78 consider the suitable working conditions and economic parameters simultaneously.
79 Vetter et al. [12] analyzed the potential relevance between the maximal net output
80 power and working fluid critical temperature with geothermal fluid temperature in
81 the subcritical and trans-critical ORC system. It found out the highest net output
82 power appeared when the ratio of working fluid critical temperature and geothermal
83 fluid temperature was 0.8. Additionally, the geothermal ORC combined with
84 different subsystem is a feasible way to make system thermo-economic performance
85 better. Sun et al. [13] investigated the effect of pinch point temperature difference
86 (PPTD) on the geothermal ORC thermo-economic performance. The optimization
87 results showed that the optimal evaporation temperature and the heat transfer area

88 per unit power output decreased with increasing PPTD. The levelized cost of
89 electricity and the dynamic payback period reached minimal when PPTD was 7°C.
90 Meng et al. [14] further explored the interaction between the evaporation and flash
91 temperature on recovering heat from medium temperature geothermal brine. Cakici
92 et al. [15] performed the energy and exergy analysis of trans-critical regenerative
93 ORC system combined with parabolic trough solar collectors. The integrated system
94 net output power increased while the electricity and exergy efficiency decreased
95 compared to single system, and R134a yielded outstanding thermodynamic
96 performance with an increment of the geothermal water inlet temperature and
97 collector areas.

98 Since the ORC system efficiency depends on the refrigerants properties,
99 researchers also have paid much attention on optimal selection of working fluids
100 with thermodynamic laws assessments. Moloney et al. [4] investigated
101 thermodynamic performance of recuperative trans-critical ORC system for a range
102 of medium to high temperature geothermal reservoirs, indicating that R1233zd(E),
103 R600, R601a, R601, R601b performed the best among twenty working fluids when
104 taken plant efficiency as optimization parameters. Wang et al. [16] developed a
105 working fluid selection methodology mainly based on the thermodynamic
106 performance for the subcritical, superheated, and trans-critical ORC system,
107 utilizing supercritical CO₂ as heat extraction medium in the high temperature
108 geothermal reservoir. The working fluid was recommended when the net output
109 power, specific net output power, thermal efficiency and exergy efficiency were
110 simultaneously equal or greater than their median value. Furthermore, some studies
111 adopt evaluation tool which takes account of environmental properties of working
112 fluids. Heberle et al. [17] qualified the potential of low GWP working fluids like
113 R600, R601a, R290, R1233zd, R1234yf as alternatives for fluorinated fluids like
114 R245fa during the life cycle assessment in the binary geothermal power plant.
115 Judging by the exergy and environmental analysis results, the low GWP working
116 fluids had less effect on environment and higher exergy efficiency in comparison to
117 fluorinated fluids, and the two-stage subcritical ORC and trans-critical ORC
118 manifested better than one-stage subcritical ORC system. For the purpose that
119 avoids the occurrence of refrigerant leakage and guarantees the stable working

120 conditions of geothermal ORC system, it depends on selecting working fluids with
121 environmental friendly, safety, low flammability and excellent thermodynamic and
122 techno-economic characteristics.

123 Plenty of investigations are discretely concerned about environmental,
124 thermodynamic and economic performance of geothermal ORC system. But they
125 might neglect the internal relationship between the effective factors. Consequently, a
126 few literatures started to search for multi-objective optimization techniques.
127 Jankowski et al. [18] investigated the influence of geothermal brine salinity on the
128 performance in the subcritical ORC power plant. Taking the minimal heat transfer
129 area and maximal exergy efficiency as the multi-objective parameters under Genetic
130 Algorithm, the Pareto point demonstrated that the heat transfer area increased 8%
131 and exergy efficiency decreased 5% with an increment in salinity. Bina et al. [19]
132 constructed multi-criteria fuzzy TOPSIS decision making method for selecting most
133 favorable cycle configuration in geothermal power plant, covering exergy efficiency,
134 thermal efficiency, net output power, production cost, total cost rate the five
135 indicators. From the thermo-economic perspective and interval Shannon's entropy
136 weighting calculation, the ORC system with internal heat exchanger ranked the first.
137 Wang et al. [20] explored the relationship of pinch point temperature difference
138 (PPTD) between evaporator and condenser in the thermo-economic optimization
139 process of subcritical ORC system. Based on the Analytic Hierarchy Process (AHP)
140 method which cared about the energy output, energy output efficiency and economic
141 criteria, it determined the best working fluid for 150°C hot water was R11 and the
142 optimal ratio of PPTD was from 1.25 to 1.5.

143 Although numerous studies have discussed the optimization and evaluation
144 process, the objective indicators just covered relatively limited side and couldn't
145 give a thorough analysis of the overall ORC system performance. The non-structural
146 fuzzy decision method is widely used as an efficient approach for comprehensive
147 evaluation, which considers the indexes interrelation and provides intuitive
148 comparison of the assessed schemes. Zhou et al. [21] adopted non-structural fuzzy
149 decision method for pre-design process of compact heat exchangers which united
150 the thermodynamic, economic and mechanical the three levels evaluation indexes. In
151 the light of the third level evaluation result, the first alternative for sulfuric acid
152 solution cooler was plate-fin heat exchanger fabricated by PTFE.

153 It can be found that most previous investigations about geothermal ORC
154 system incline to take basis of first and second laws analysis with thermodynamics,
155 focusing on these aspects of thermodynamic and techno-economic performance
156 evaluation, system structure and layout, objective optimization and working fluid
157 selection. Regarding the simulated results of highest net output power or lowest
158 initial investment Cost as criterion to determine the best ORC system scheme.
159 However, the assessment process tends to concentrate on one level decision criteria
160 like thermodynamic indicators, which fails to integrate the comprehensive influence
161 of techno-economic and social benefit indicators on the system whole performance.
162 It may lead the pre-designed scheme to an unachievable goal and cause irretrievable
163 loss to the investors.

164 Thus, this paper aims at developing an efficient and practical decision-making
165 method, i.e. a three-level non-structural fuzzy decision method, based on
166 comprehensive performance evaluation of the ORC employed for typical geothermal
167 reservoirs. During the whole assessment procedures, six working fluids and three
168 levels of performance are investigated, including the safety and environmental
169 property as the first level, thermodynamic performance as the second level and the
170 techno-economic performance as the third level. A non-structural fuzzy
171 decision-making method is then developed based on the three-level assessment to
172 eventually implement practical and reliable decision-making for the geothermally
173 driven ORC systems.

1 System description

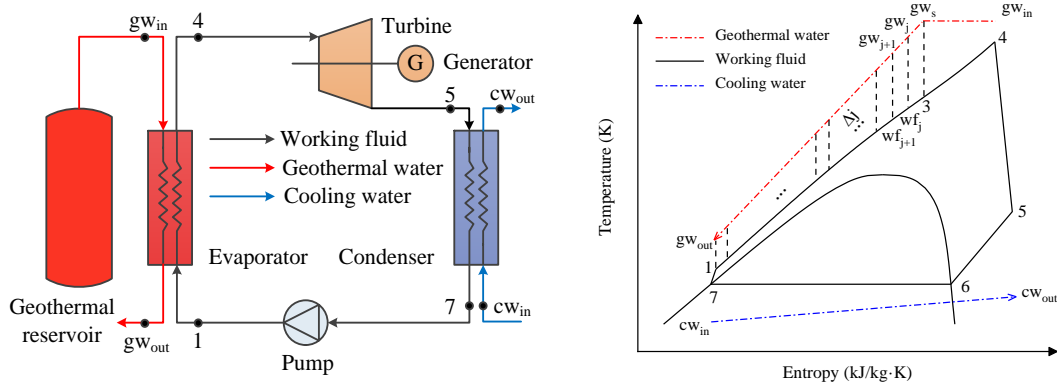


Fig. 1. Schematic and T-s diagram of TORC system

Table 1 Operating conditions of TORC system

Parameter	Value
GR-I wellhead temperature, T_{gwin-1} (°C)	182.23
GR-I wellhead pressure, P_{gw-1} (MPa)	1.06
GR-I wellhead mass flow rate, m_{gw-1} (kg/s)	13.64
GR-II wellhead temperature, T_{gwin-2} (°C)	224.37
GR-II wellhead pressure, P_{gw-2} (MPa)	2.52
GR-II wellhead mass flow rate, m_{gw-2} (kg/s)	11
Condensing temperature, T_{cond} (°C)	35
Cooling water inlet temperature, T_{cwin} (°C)	20
Evaporator pinch point temperature, $T_{pinch-e}$ (°C)	10
Condenser pinch point temperature, $T_{pinch-c}$ (°C)	5
Turbine isentropic efficiency, $\eta_{turbine}$	0.75
Pump isentropic efficiency, η_{pump}	0.7
Dead state temperature, T_{dead} (°C)	20
Dead state pressure, P_{dead} (MPa)	0.101

175 The geothermal reservoirs under investigation in this work are located in the
176 Aluto Langano geothermal field of Ethiopia, which is recognized as a medium/high
177 temperature liquid-dominated geothermal field in eastern Africa. Two typical and
178 active geothermal reservoirs (i.e., Geothermal Reservoir I and Reservoir II) are
179 chosen as heat source for the proposed system. They produced two-phase,
180 fluid-dominated wellhead discharge, and the discharge data from wellhead tests are
181 gathered and listed in Table 1. Wellhead pressure, temperature and mass flow rate
182 are tested in situ. Instead of choosing the basic sub-critical ORC pattern, the
183 trans-critical ORC (TORC) is determined for its higher energy efficiency, lower
184 exergy loss and modest pressure requirement [22]. The primary TORC system
185 working conditions constructed for working fluids in the GR-I (182.23°C) and GR-II
186 (224.37°C) are nearly identical except the investigated evaporation pressure and
187 turbine inlet temperature and flow channels in heat exchangers. Table 1 lists the
188 detailed value of relevant parameters for TORC design and construction. As
189 demonstrated in the semantic definition of TORC, the working fluid is compressed
190 to exceed critical pressure via pump. And it absorbs heat from geothermal water to
191 vaporize until it reaches the highest temperature during the courses of evaporation.
192 Then, the supercritical working fluid discharges into the turbine to produce output
193 shaft work which can be employed for power generation. After expansion, the
194 subcritical overheated vapor is condensed into saturated liquid by cooling water
195 before flowing into the pump to accomplish the next cycle. The schematic and T-s
196 diagram is illustrated in Fig. 1. The T-s diagram also shows the segment-iterative

197 process of seeking pinch point temperature between the heat source and working
198 fluids.

Table 2 Fluid characteristics [4, 16]

Working Fluid	Thermodynamic Property					Environmental Property				
	M /(kg·kmol ⁻¹)	T_b /°C	T_{de} /K	T_{cr} /K	P_{cr} /MPa	Behavior	Safety Level	ALT/Year	ODP	GWP/(100 years)
R227ea	170.0289	-16.341	475	374.9	2.925	dry	A1	38.9	0	3320
R134a	102.032	-26.0738	455	374.21	4.0593	wet	A1	13.4	0	1430
R143a	84.041	-47.2406	650	345.857	3.761	wet	A2L	47.1	0	4470
R290	44.0956	-42.1138	650	369.89	4.2512	wet	A3	0.034	0	5
R1270	42.0797	-47.6192	575	364.211	4.555	wet	A3	0.001	0	1.8
R142b	100.495	-9.1233	470	410.26	4.055	isentropic	A2	17.2	0.065	2310

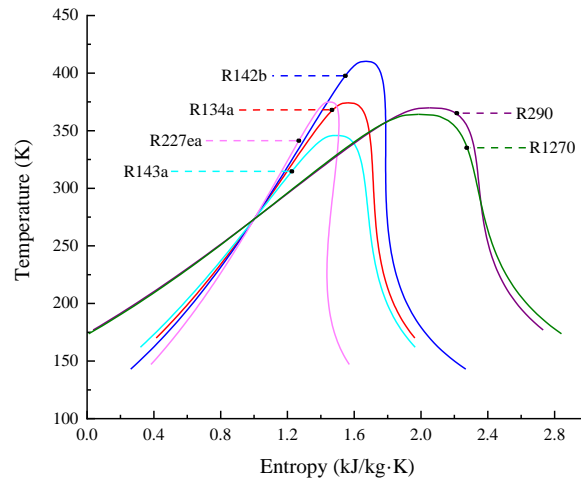


Fig. 2. T-s diagram of selected working fluids

199 The operating process of TORCs for two geothermal reservoirs are simulated in
 200 MATLAB with six picked working fluids, the environmental and thermodynamic
 201 characteristics of each working fluid are displayed in Table 2 and Fig. 2. The
 202 principals for selecting working fluids are subject to the safety level, atmospheric
 203 life time (ALT), ozone depletion potential (ODP) and global warming potential
 204 (GWP).

205 For the safety level, A and B imply the toxicity grades while B is higher than A.
206 Number 1, 2, 2L and 3 indicate flammability level and increase progressively. ALT
207 represents existing time at the atmosphere if leakage of refrigerant happens, ODP
208 means the ozone consumption with refrigerant diffusing into ozone layer, and GWP
209 indicates the potential of temperature increase in the global world caused by
210 inappropriately release of refrigerant. With regard to the four environmental
211 indicators, the smaller value the better performance. And the iteration ranges of
212 turbine inlet temperature are higher than critical temperature but lower than working
213 fluids decomposition temperature. Furthermore, the assumptions stated as below are
214 taken into consideration:

- 215 ● Each TORC system is operating steadily.
- 216 ● No impurity like silica exists in the geothermal water, as result its outlet
217 temperature is allowed for lower than 70°C.
- 218 ● The pressure drop and heat losses are neglected during each part of
219 performing process.
- 220 ● The ambient temperature and pressure are 20°C and 101kPa.
- 221 ● The pinch point temperature in the evaporator and condenser are 10°C and
222 5°C respectively.

2 Mathematical modelling

2.1 Thermodynamic model

Based on the first and second laws of thermodynamics, the following formulas are introduced to calculate thermodynamic assessment indexes.

The heat transfer flow rate in the evaporator:

$$Q_{evaporator} = m_{wf} (h_4 - h_1) \quad (1)$$

The heat transfer flow rate in the condenser:

$$Q_{condenser} = m_{wf} (h_5 - h_7) \quad (2)$$

The consumed power of pump:

$$P_{pump} = m_{wf} (h_1 - h_7) \quad (3)$$

The turbine output shaft power:

$$P_{turbine} = m_{wf} (h_4 - h_5) \quad (4)$$

The net output power of TORC system:

$$P_{net} = P_{turbine} - P_{pump} \quad (5)$$

The specific net output power:

$$AP_{net} = P_{net} / m_{gw} \quad (6)$$

The thermal efficiency of TORC system:

$$\eta_t = P_{net} / Q_{evaporator} \times 100\% \quad (7)$$

Where m_{wf} and m_{gw} are the mass flow rate of working fluid and geothermal water, while h_i represents the specific state enthalpy with $i = 1 \dots 7$ as shown in Fig.

1.

244 The exergy of each state point:

245
$$E_i = m[(h_i - h_0) - T_0(s_i - s_0)] \quad (8)$$

246 Where m is the mass flow rate of objective fluid, while s_i represents the
247 state point entropy with $i = 1 \dots 7$, and the subscript 0 implies the ambient condition.

248 The exergy losses of pump:

249
$$I_{pump} = m_{wf} T_0 (s_1 - s_7) \quad (9)$$

250 The exergy losses of evaporator:

251
$$I_{evaporator} = (E_{gwin} + E_1) - (E_{gwout} + E_4) \quad (10)$$

252 The exergy losses of turbine:

253
$$I_{turbine} = m_{wf} T_0 (s_5 - s_4) \quad (11)$$

254 The exergy losses of condenser:

255
$$I_{condenser} = (E_{cwin} + E_5) - (E_{cwout} + E_7) \quad (12)$$

256 The exergy losses caused by cooling water flows out:

257
$$I_{out}^{cooling\ water} = E_{cwout} - E_{cwin} \quad (13)$$

258 The total exergy losses of TORC system:

259
$$I_{system} = I_{pump} + I_{evaporator} + I_{turbine} + I_{condenser} + I_{out}^{cooling\ water} \quad (14)$$

260 The net exergy that geothermal water flows into system:

261
$$E_{in}^{gw} = P_{net} + I_{system} \quad (15)$$

262 The exergy efficiency of TORC system:

263
$$\eta_e = P_{net} / E_{in}^{gw} \quad (16)$$

264 The subscript *in* and *out* refers to the inlet and outlet state for objective

265 fluid.

Before calculating the overall heat transfer coefficient and area of heat exchangers, the primary task is to identify the mass flow rate of working fluid. The inlet temperature (T_{gwin}) and mass flow rate of geothermal water (m_{gw}) are constant. Besides that, the minimal temperature difference is set larger than 10°C between the evaporator inlet temperature of geothermal water and outlet temperature of working fluid.

First of all, referring to the Pinch Point Temperature Difference method, the evaporator outlet temperature of geothermal water (T_{gwout}) is assumed to get the outlet enthalpy (h_{gwout}) and calculate initial value of working fluid mass flow rate (m_{wf}):

$$m_{wf} = m_{gw} (h_{gwin} - h_{gwout}) / (h_4 - h_1) \quad (17)$$

Secondly, the single-phase flow region of geothermal water from gw_s to gw_{out} point is divided into one hundred segments as shown in Fig. 1. Thus the temperature difference of each segment can be determined. As a result, it could deduce the next state point temperature (T_{gwj}) from the beginning of T_{gws} .

$$T_{gwj} = T_{gws} - (T_{gws} - T_{gwout}) / 100j \quad (18)$$

The subscript j denotes the divided segments which range from 1 to 100.

Thirdly, based on the acquired variables of h_{gwj} , h_{gwout} , m_{wf} , the enthalpy (h_{gwj}) and temperature (T_{gwj}) of each state point for working fluids from 1 to 3 point can be obtained by using the first laws of thermodynamics.

$$h_{wff} = h_1 + m_{gw} (h_{gwj} - h_{gwout}) / m_{wf} \quad (19)$$

287 Lastly, the actual temperature difference between geothermal water and
288 working fluids of each segment can be calculated. And the minimal temperature
289 difference (ΔT_{act}) could be found out. Comparing it with 10°C, if the discrepancy
290 satisfies the accuracy requirement (1%), it demonstrates that the assumed evaporator
291 outlet temperature of geothermal water is reasonable. Otherwise, it needs to go back
292 to the first step to presume another outlet temperature until meets the accuracy
293 requirement.

294 2.2 Heat transfer model

295 The plate heat exchanger is selected as evaporator and condenser for its
296 excellent heat transfer performance and compact structure. The geometric structure
297 and dimension of plate heat exchanger are summarized in Table 3.

Table 3 Geometry of plate heat exchanger

Parameter	Value
Chevron angle, β (°)	60
Plate width, L_w (m)	0.65
Plate thickness, t (m)	0.0005
Corrugation pitch, Λ (m)	0.0085
Corrugation depth, b (m)	0.0025
Surface enlargement factor, ϕ	1.19
Hydraulic diameter, D_h (m)	0.0042
Equivalent diameter, D_{eq} (m)	0.005
Coefficient of thermal conductivity, λ_{PHE} (kW/(m·K))	0.0163

298 The heat transfer process in the evaporation and condenser are both divided
 299 into two sections. As illustrated above, the evaporator separates into single-phase
 300 flow and two-phase flow region according to the thermo-physical state of
 301 geothermal water. Similarly, the heat transfer area of condenser is divided into
 302 cooling and condensing region on the basis of the thermo-physical state of working
 303 fluid.

304 For the single-phase flow of geothermal water in the evaporator and cooling
 305 water in the condenser, the Leveque correlation [23] is used to calculate the heat
 306 transfer coefficient, which are α_{sgw} and α_{cw} respectively.

307 The Wang and Zhao correlation [24] is applied for calculation of geothermal
 308 water two-phase flow heat transfer coefficient (α_{tgw}) in the evaporator.

$$309 \quad Nu = 0.00115(\text{Re}_l/H)^{0.983} \text{Pr}_l^{0.33} (\rho_l/\rho_v)^{0.248} \quad (20)$$

$$310 \quad \alpha_{tgw} = Nu\lambda_l/D_{eq} \quad (21)$$

$$311 \quad \text{Re}_l = G_{gw}(1-x_0)D_{eq}/\mu_l \quad (22)$$

$$312 \quad \text{Pr}_l = c_{p,l}\mu_l/\lambda_l \quad (23)$$

$$313 \quad H = c_{p,l}(T_{ave} - T_{wall}) / (i_{fg} + 0.68c_{p,l}(T_{ave} - T_{wall})) \quad (24)$$

Where the indicators with subscript l are calculated based on the mean temperature of steam and wall temperature (T_{ave}), and the indicators with subscript v are calculated based on the average steam temperature, λ represents the thermal conductivity of objective water, G_{gw} implies the total mass flux of geothermal water, x_0 is the vapor quality at the end state of two-phase flow region which sets as 0, D_{eq} is the equivalent diameter of plate heat exchanger, and i_{fg} represents the latent heat of water from liquid to vapor state.

As for the trans-critical working fluids in evaporator, Jackson correlation [25] is adopted to calculate the heat transfer coefficient ($\alpha_{tc, wf}$).

$$Nu = 0.0183 Re^{0.82} Pr^{0.5} (\rho_{wall} / \rho)^{0.3} (\bar{c}_p / c_p)^n \quad (25)$$

$$\alpha_{tc, wf} = Nu \lambda / D_h \quad (26)$$

$$\bar{c}_p = (h_{wall} - h_c) / (T_{wall} - T_c) \quad (27)$$

$$Re = \rho v D_h / \mu \quad (28)$$

$$Pr = c_p \mu / \lambda \quad (29)$$

$$\begin{aligned} n &= 0.4, T_c < T_{wall} < T_{cri}, 1.2T_{cri} < T_c < T_{wall} \\ n &= 0.4 + 0.2 \left[(T_{wall} / T_{cri}) - 1 \right], T_c < T_{cri} < T_{wall} \\ n &= 0.4 + 0.2 \left[(T_{wall} / T_{cri}) - 1 \right] \left[1 - 5 (T_c / T_{cri} - 1) \right], T_{cri} < T_c < 1.2T_{cri}, T_c < T_{wall} \end{aligned} \quad (30)$$

Where T_c is the characteristic temperature of working fluid and h_c is obtained based on it. Additionally, other indexes like ρ_{wall} and h_{wall} are acquired under the condition of plate heat exchanger wall-side temperature (T_{wall}), T_{cri} is the critical temperature of working fluid, and D_h is hydraulic diameter which calculated by $D_h = 2b/\phi$.

For the cooling part in the condenser, the Chisholm correlation [26] is employed for calculating the working fluid heat transfer coefficient (α_{swf}).

For the condensing part in the condenser, the Kandlikar correlation [27] is used to calculate the working fluid heat transfer coefficient (α_{twf}).

$$\alpha_l = 0.2092(\lambda_l/D_h) \text{Re}_l^{0.78} \text{Pr}_l^{0.33} (\mu/\mu_{wall})^{0.14} \quad (31)$$

$$\text{Re}_l = G_{wf} D_h / \mu_l \quad (32)$$

$$\text{Pr}_l = c_{p,l} \mu_l / \lambda_l \quad (33)$$

$$Co = (\rho_v / \rho_l)(1/x_m - 1)^{0.8} \quad (34)$$

$$Fr_l = G_{wf}^2 / (\rho_l^2 g D_h) \quad (35)$$

$$Bo = q / G_{wf} i_{fg} \quad (36)$$

$$\alpha_{twf} = \alpha_l (0.25 Co^{-0.45} Fr_l^{0.25} + 75 Bo^{0.75}) \quad (37)$$

Where g implies the acceleration of gravity which is $9.8(\text{m/s}^2)$, G_{wf} is the total mass flow rate of working fluid, and x_m is the vapor quality which sets 0.5.

After acknowledging the heat transfer coefficient of each section, the heat exchanger areas (A) are derived from the following equations.

$$A = Q / U / \Delta T_m \quad (38)$$

$$1/U = 1/\alpha_{hot-side} + t/\lambda_{PHE} + 1/\alpha_{cold-side} \quad (39)$$

Where Q is the heat transfer mass flow and U is the overall heat transfer coefficient of each part, while ΔT_m is the log mean temperature difference between hot-side and cold-side and λ_{PHE} is the thermal conductivity of plate heat exchanger.

2.3 Techno-economic model

For the purpose of giving an all-around viewpoint on the techno-economic properties of the ORC system, six parameters are collected that covered two aspects of investment and expected return. In detail, which are heat transfer area per net output power (APR), turbine characteristic size parameters (SP), gross cost based on the latest economic indexes ($Cost_{2019}$), electricity production cost (EPC), depreciated payback period (DPP) and saving to investment ratio (SIR).

The APR is employed as evaluation criterion of the heat exchanger compactness, the more compact of the heat exchanger structure, the smaller the APR and the lower the initial investment, which is defined as:

$$APR = (A_e + A_c) / P_{net} \quad (40)$$

The SP is regarded as an indicator of the relative cost of TORC system by measuring the size of turbine, which is defined as:

$$SP = \sqrt{V_5} / \Delta h_{isen}^{0.25} \quad (41)$$

Where V_5 is the volume flow of turbine outlet (state point 5) while Δh_{isen} is isentropic enthalpy drop before and after expansion (state point 4 to 5).

The $Cost_{2019}$ is determined based on the Module Cost Technique [28], It represents the sum of bare module costs of the main components in ORC system, which is given below:

$$Cost_{2019} = C_{BM, pump} + C_{BM, evaporator} + C_{BM, turbine} + C_{BM, condenser} \quad (42)$$

$$Cost_{2019} = Cost_{2001} CEPCI_{2019} / CEPCI_{2001} \quad (43)$$

376 Where $CEPCI$ is the chemical engineering plant cost index while
377 $CEPCI_{2001} = 397$ and $CEPCI_{2019} = 607.5$ [29].

378 As presented in Table 4, the bare module cost (C_{BM}) is defined as the product
379 of purchased cost (C_p) and bare module cost factor (F_{BM}). C_p is related to the
380 capacities ($P_{pump}, P_{turbine}$) and size parameters (A_e, A_c) of each component which are
381 acquired from the optimal results. F_{BM} considers the material factor (F_M) and
382 pressure factor (F_p). The materials for heat exchangers and pump are stainless steel
383 and the pump type is centrifugal. Then, the coefficients like B, C, K could be
384 determined by the arranged configurations.

Table 4 Main components bare module cost equations

Component	Bare module cost equation	Coefficient				
		$K_1/K_2/K_3$	$C_1/C_2/C_3$	B_1/B_2	F_M	F_{BM}
Turbine	$C_{BM, turbine} = C_{p, turbine} F_{BM, turbine}$	$K_{1,t} = 2.626$				
	$\lg C_{p, turbine} = K_{1,t} + K_{2,t} \lg P_t + K_{3,t} (\lg P_t)^2$	$K_{2,t} = 1.440$	/	/	/	3.5
		$K_{3,t} = -0.178$				
Pump	$C_{BM, pump} = C_{p, pump} F_{BM, pump}$	$K_{1,p} = 3.389$	$C_{1,p} = -0.394$			
	$\lg C_{p, pump} = K_{1,p} + K_{2,p} \lg P_p + K_{3,p} (\lg P_p)^2$	$K_{2,p} = 0.054$	$C_{2,p} = 0.396$	$B_{1,p} = 1.89$	2.32	/
	$F_{BM, pump} = B_{1,p} + B_{2,p} F_{M, pump} F_{P, pump}$	$K_{3,p} = 0.155$	$C_{3,p} = -0.002$	$B_{2,p} = 1.35$		
	$\lg F_{p, pump} = C_{1,p} + C_{2,p} \lg P_p + C_{3,p} (\lg P_p)^2$					
Evaporator	$C_{BM, evaporator} = C_{p, evaporator} F_{BM, evaporator}$	$K_{1,e} = 4.666$		$B_{1,e} = 0.96$		
	$\lg C_{p, evaporator} = K_{1,e} + K_{2,e} \lg A_e + K_{3,e} (\lg A_e)^2$	$K_{2,e} = -0.156$	/	$B_{2,e} = 1.21$	2.45	/
	$F_{BM, evaporator} = B_{1,e} + B_{2,e} F_{M, evaporator}$	$K_{3,e} = 0.155$				
Condenser	$C_{BM, condenser} = C_{p, condenser} F_{BM, condenser}$	$K_{1,c} = 4.666$		$B_{1,c} = 0.96$		
	$\lg C_{p, condenser} = K_{1,c} + K_{2,c} \lg A_c + K_{3,c} (\lg A_c)^2$	$K_{2,c} = -0.156$	/	$B_{2,c} = 1.21$	2.45	/
	$F_{BM, condenser} = B_{1,c} + B_{2,c} F_{M, condenser}$	$K_{3,c} = 0.155$				

The EPC demonstrates the relative scales of capital input and output from the perspectives of per unit power generation cost, which is presented as:

$$EPC = (\text{Cost}_{2019} CRF + f_k \text{Cost}_{2019}) / (P_{net} h_{working-time}) \quad (44)$$

$$CRF = i(1+i)^{time} / ((1+i)^{time} - 1) \quad (45)$$

Where CRF is the capital recovery factor, f_k is operation and maintenance factor which sets as 1.65%, $h_{working-time}$ is the working time of each year which assumes to be 8100h, i is the annual interest which regarded as 5% and $time$ is the life cycle assessment time of 15 years.

The DPP gives a clearly projected investment return time of the ORC system, which is defined as:

$$DPP = -\ln(1 - k \text{Cost}_{2019} / F_{n0}) / \ln(1 + k) \quad (46)$$

$$F_{n0} = E_p (P_{net} h_{working-time}) - f_k \text{Cost}_{2019} \quad (47)$$

Where k implies the depreciated ratio which is 5%, F_{n0} is the system net income and E_p is the electricity sale price which sets as 0.1(\$/kW·h) [30]. Moreover, the net output power (P_{net}) is completely regarded as net electricity generation as result that the power generation efficiency sets as 1.

The SIR figures out the proportion of the predicted profit and initial investment, which is defined as:

$$SIR = B_{time} / C_{time} \quad (48)$$

$$B_{time} = \sum_{j=1}^{time} (P_{net} h_{working-time} E_p (1+r)^j / (1+i)^j) \quad (49)$$

$$C_{time} = \sum_{j=0}^{time} ((f_k \text{Cost}_{2019}) (1+r)^j / (1+i)^j) \quad (50)$$

Where B_{time} and C_{time} are the net value of total income and investment during the period of life cycle assessment time which $j = 1 \dots 15$, r is the inflation rate which sets as 2.9%.

2.4 Three-level fuzzy decision model

In the paper, the three-level fuzzy decision model is established based on the properties model of working fluids, the thermodynamic model and the techno-economic model as put forward earlier, which are regarded as the first, second and third level respectively. The development and programming of the method is accomplished by the following four steps:

Step (1) - Acquiring the optimal results of decision criteria by choosing appropriate indicator as the objective function according to the realistic operation requirements.

Step (2) - A pair-wise comparison matrix of each decision criterion for schemes is constructed so as to rank in sequence and assign the semantic score. After the normalization of semantic score, the weighting set of each criterion could be obtained.

Step (3) - Similar to step two, a pair-wise comparison matrix of each decision criterion for three classified levels is built, the weighting set calculation is subject to the relative importance of decision criteria within each level.

Step (4) - After acknowledging the weighting set of each criterion, the weighting matrix for schemes (R_i) and levels (W_i) can be developed. And the evaluation set (B_i) can be calculated by the following equation:

$$B_i = W_i \times R_i \quad (51)$$

For the second level, evaluation result of the first level should be inserted into the R_i as the last row. The original W_i of second level needs to multiply $n/(n+1)$ if n decision criteria are included. Next, a new W_i has to be formed by assigning $1/(n+1)$ in the final position of the former one. For the third level, the same procedure is undergoing repeatedly to gain B_i .

Summarizing the three mathematical models above, Fig. 3 gives a clear flow chart of the construction procedures.

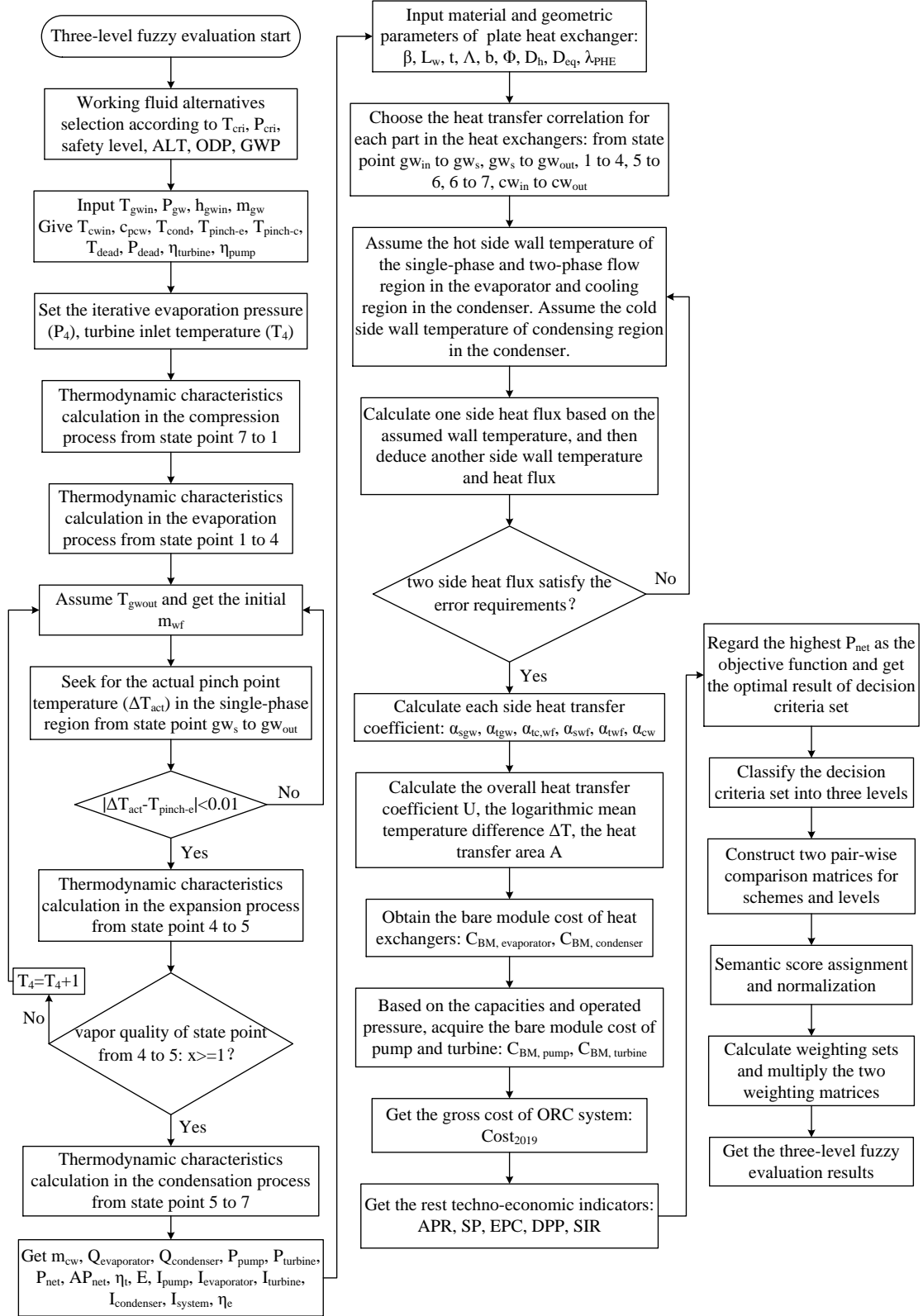


Fig. 3. The three-level fuzzy evaluation procedures

3.1 Thermodynamic performance

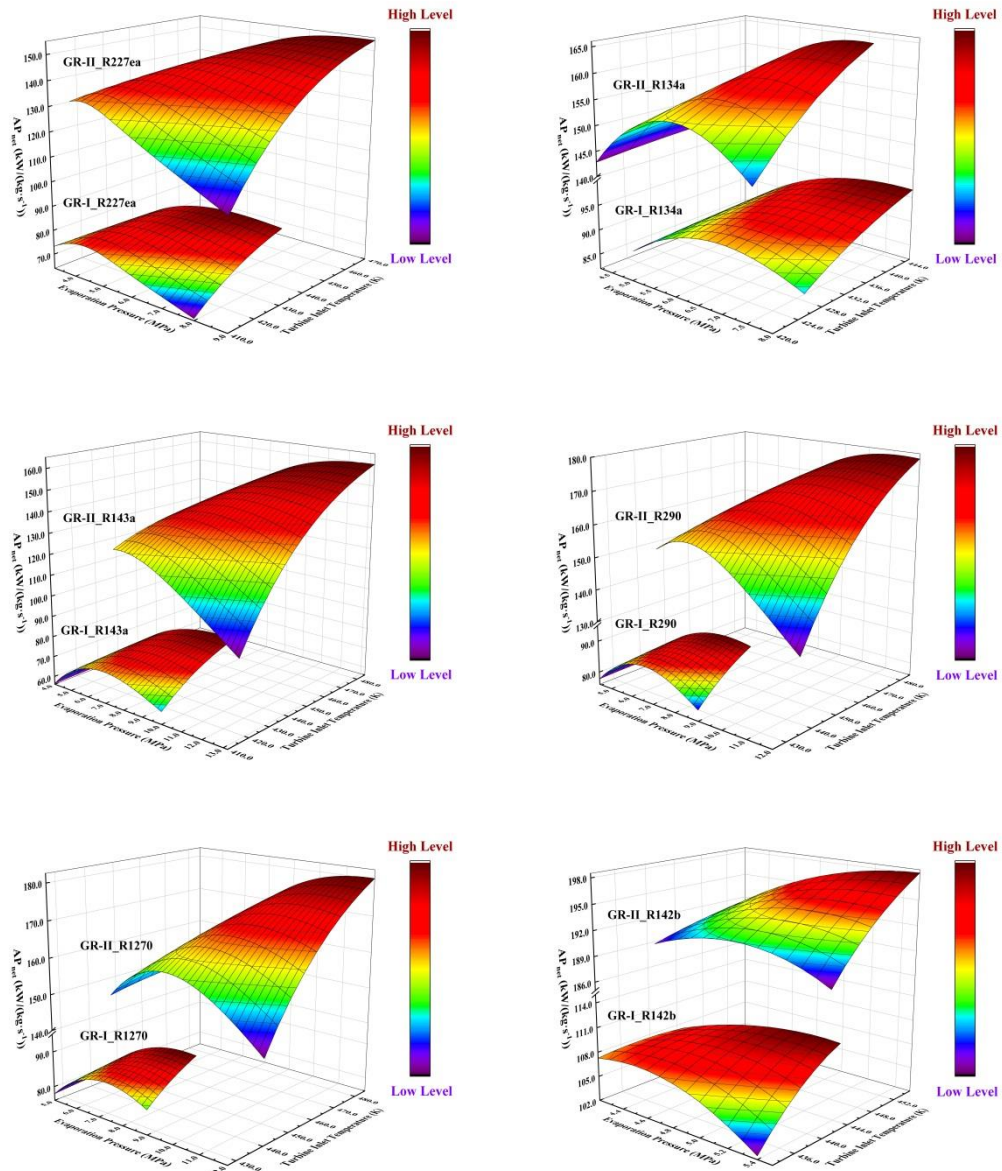


Fig. 4. Specific net output power (AP_{net}) variation in two geothermal reservoirs

438 In this study, the specific net output power (AP_{net}), thermal efficiency (η_t) and
439 exergy efficiency (η_e) are determined to estimate the thermodynamic performance of
440 the TORC system designed for both geothermal reservoirs (GR-I and GR-II). As
441 shown in Figs. 4, 5 and 6, the overall variation of the three indexes shows both
442 similarities and diversities with increasing evaporation pressure (P_4) and turbine
443 inlet temperature (T_4) for each working fluid in two different geothermal reservoirs.
444 Moreover, Fig. 4 indicates AP_{net} of the six selected working fluids in GR-II which
445 ranges from 93.73-198.14kW/(kg·s⁻¹) is apparently higher than that of GR-I which is
446 from 56.46-110.94kW/(kg·s⁻¹), indicting a higher power capacity of GR-II. Besides,
447 Fig. 4 demonstrates AP_{net} increases firstly and then decreases when raising P_4
448 under given T_4 . It is because turbine output shaft power ($P_{turbine}$) enhances
449 obviously while P_4 increases from lower values (but still exceed the critical
450 pressure of the working fluid). And the consumed power of pump (P_{pump}) increases
451 more rapidly than $P_{turbine}$ with further increase of P_4 , which results that the upward
452 trend of AP_{net} gradually slows down until it starts deceasing. In addition, due to the
453 limits of pinch point temperature difference ($T_{pinch-e}$) and decomposition
454 temperature (T_{de}) of working fluids, AP_{net} keeps increasing while T_4 grows up to
455 reach the maximal value under higher P_4 . Furthermore, AP_{net} shows upward
456 tendency firstly and then goes downward when given a lower P_4 . Comparing the
457 optimal results of working fluids in GR-I, R142b is able to acquire the largest AP_{net}
458 of 110.94kW/(kg·s⁻¹) at the condition that the P_4 is 5.2MPa and T_4 is 445K. On
459 the contrary, R143a obtains smallest AP_{net} of 81.77kW/(kg·s⁻¹) in the case of the

460 P_4 is 9.4MPa and T_4 is 445K. With regard to GR-II, R142b maintains the highest
 461 AP_{net} as well, which is 198.14kW/(kg·s⁻¹) when the P_4 is 5.5MPa and T_4 is
 462 455K. And R227ea yields lowest AP_{net} of 154.02kW/(kg·s⁻¹), for the P_4 is
 463 8.6MPa and T_4 is 470K.

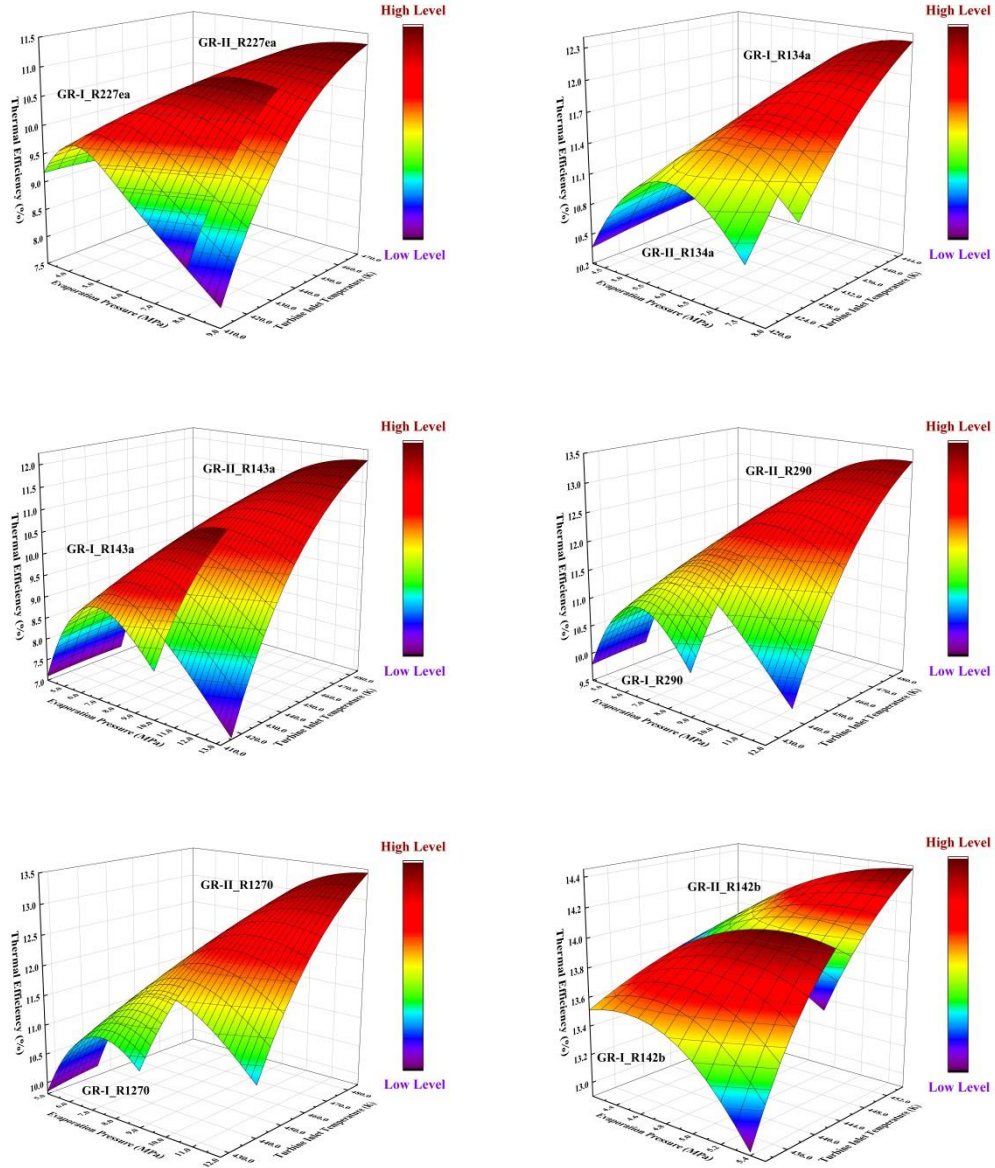


Fig. 5. Thermal efficiency (η_t) variation in two geothermal reservoirs

Thermal efficiency (η_t) is defined as the ratio of net power output (P_{net}) to the amount of heat absorbed during the evaporation process, as shown in Eq. (7). The change of η_t by varying evaporation pressure (P_4) and turbine inlet temperature (T_4) is illustrated in Fig. 5. As far as the η_t of each working fluid is concerned, there exists regions that are partially overlapped between GR-I and GR-II, which ranges from 7.10-14.05% and 7.04-14.43%, indicating that even though geothermal reservoirs have different power capacities, they could have similar energy conversion efficiency ranges applying TORC. Specifically, it is observed that η_t of all selected working fluids can be described as increasing and dropping later with an increase of P_4 under investigated T_4 . The alteration of η_t is similar with AP_{net} . For this reason, the η_t rises faster at lower P_4 and stabilizes till it decreases as P_4 increases further. Additionally, with the restrictions of $T_{pinch-e}$ and T_{de} , η_t represents an inclination of rising up continuously with increasing T_4 to the maximum under higher P_4 . The reason can be explained from that, although the enthalpy difference ($h_4 - h_5$) becomes larger and the mass flow rate of working fluids (m_{wf}) is declining in the course of expansion, the turbine output shaft power ($P_{turbine}$) still increases and the pump power consumption (P_{pump}) decreases as T_4 continues increasing. In the meanwhile, when the system operates at a lower P_4 , η_t behaves in a trend of increasing first and then diminishes as T_4 grows up. The maximum results of η_t for working fluids in GR-I and GR-II are both R142b which are 14.05% and 14.43% respectively, for the P_4 and T_4 are 5.1MPa, 445K and 5.5MPa, 455K. To the opposite, R143a and R227ea have the minimal η_t in GR-I and GR-II with

486 the values of 10.66% and 11.32%.

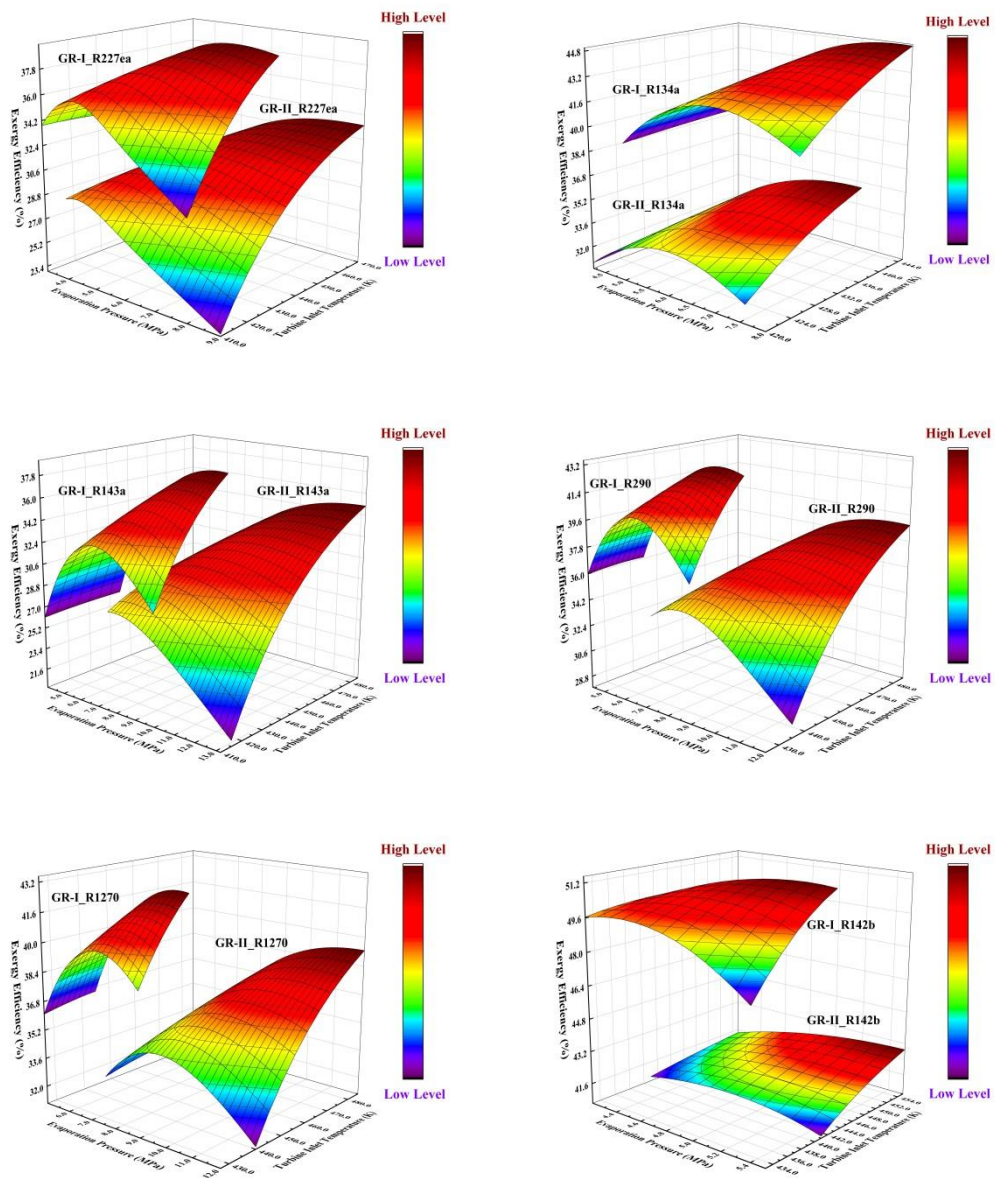


Fig. 6. Exergy efficiency (η_e) variation in two geothermal reservoirs

487 Exergy signifies the greatest beneficial output power that geothermal system
488 possesses. The exergy efficiency (η_e) is employed for assessing the exergy
489 utilization, which is characterized as the ratio of net output power (P_{net}) to the net
490 exergy flows into the system (E_{in}^{gw}), as given in Eq. (16). Typically, it can be noticed
491 from Fig. 6 that the η_e in GR-I is normally higher than GR-II. The ranges are
492 26.11-51.42% for GR-I and 23.14-42.89% for GR-II, which indicates that although
493 GR-I has smaller power capacity, the exergy is fully utilized compared to GR-II.
494 Particularly, Fig. 6 denotes that the arc-surface changing trend of η_e is familiar with
495 that of AP_{net} and η_t . Increasing of η_e is owing to the thermal matching
496 performance becomes better between heat sources and working fluids and the exergy
497 loss (I_{system}) reduces constantly with an increment of lower evaporation pressure
498 (P_4). Instead, the reduction of P_{net} is more markedly than the I_{system} decreases
499 with further increase of P_4 , leading to the downward tendency for η_e . What's more,
500 the η_e shows a trend of growing up for that P_{net} keeps increasing while I_{system}
501 turns into dropping by improving turbine inlet temperature (T_4) under investigated
502 P_4 . According to optimal results of the working fluids, R142b achieves the biggest
503 η_e of 51.42% and 42.90% in the GR-I and GR-II, with the P_4 and T_4 are 5.2MPa,
504 445K and 5.5MPa, 455K. And R143a and R227ea get lowest exergy efficiency of
505 38.30% and 33.42% for the two geothermal reservoirs.

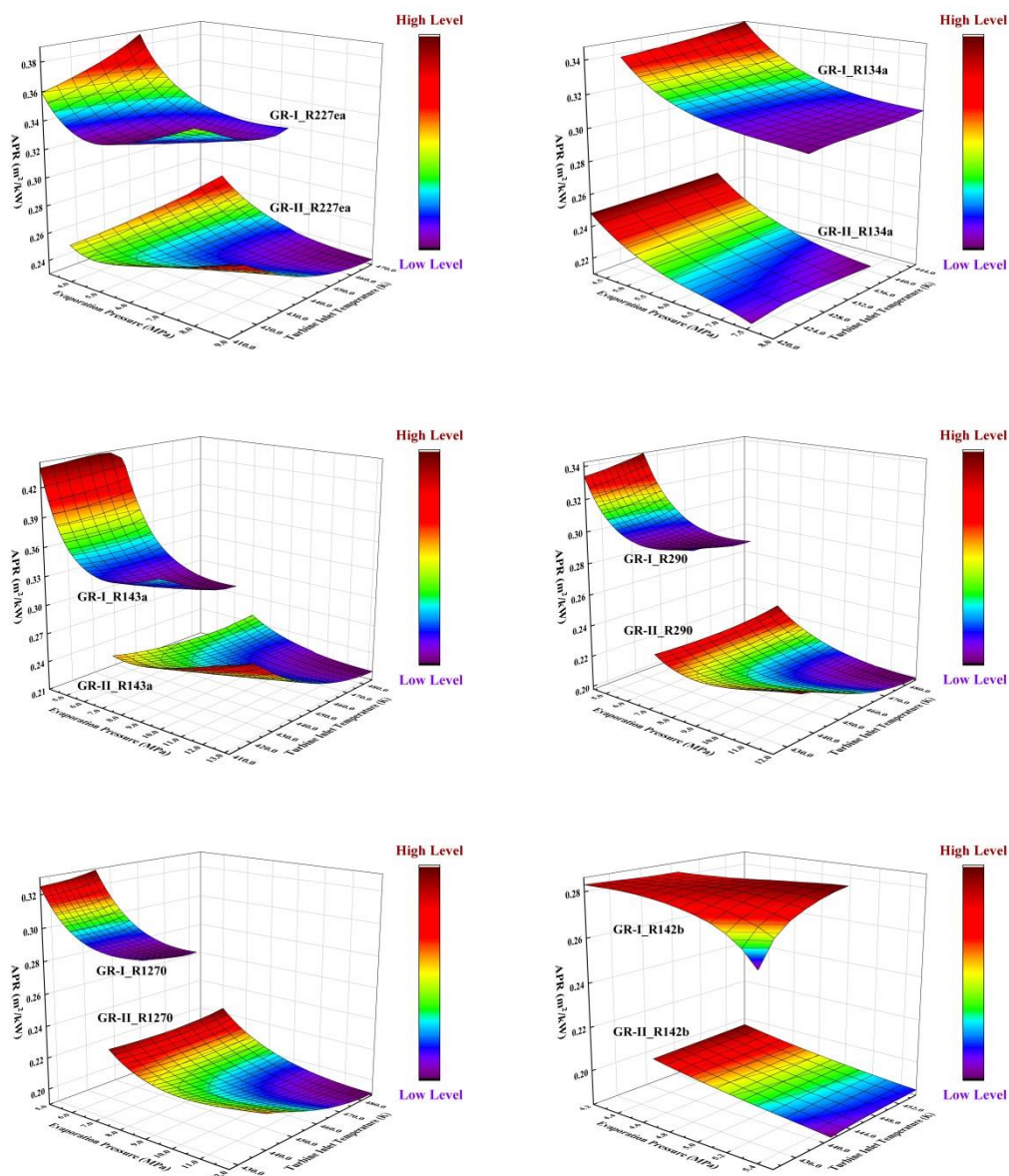


Fig. 7. Heat transfer area per net output power (APR) variation in two geothermal reservoirs

Utilizing the techno-economic evaluation model established previously, the heat transfer area per net output power (APR) and electricity production cost (EPC) are adopted for detailed illustration of the techno-economic properties of TORC system. First of all, as depicted in Figs. 7 and 8, the map alteration of two indexes for each working fluid (except R142b) expresses consistent changing trend under the influence of evaporation pressure (P_4) and turbine inlet temperature (T_4) in the both two geothermal reservoirs. The APR and EPC values in GR-I is commonly above those of GR-II. As for GR-I and GR-II, APR ranges from 0.262-0.444(m²/kW) and 0.185-0.290(m²/kW). EPC ranges from 0.030-0.054(\$/(kW·h)) and 0.022-0.055(\$/(kW·h)), indicating that GR-II is more profitable in the techno-economic perspective. Furthermore, APR implies the compactness of heat exchangers structure which refers to the ratio of hear transfer areas of all heat exchangers to net output power. For the purpose of cutting down the overall cost of the whole system, it's better to achieve the APR as low as possible. Then, it can be seen form Fig. 7 that APR of R227ea, R143a, R290 and R1270 decreases initially before increasing in both two geothermal reservoirs when increasing P_4 under given T_4 . Since the net output power (P_{net}) first increases and then decreases for the four working fluids with which trend of variation is more dramatically than the heat transfer areas change. Regarding the APR of R134a and R142b, it's decreasing yet with an increment of P_4 under given T_4 . The difference of R134a and R142b from other four alternatives accounts for the downward trend of heat transfer areas varies more significantly than that of P_{net} . Moreover, the region of minimum APR for the

529 working fluids (expect R142b in GR-I) begins to appear when further increasing P_4
530 and T_4 simultaneously. Summarily, concluding from the optimal results under the
531 operated conditions. R142b acquires the lowest APR of 0.262(m²/kW) and
532 0.185(m²/kW) in GR-I and GR-II, for 5.4MPa, 433K and 5.5MPa, 441K of the P_4
533 and T_4 . Additionally, R227ea obtains higher APR of 0.331(m²/kW) and
534 0.234(m²/kW) respectively, for 5.8MPa, 425K and 9.0MPa, 470K.

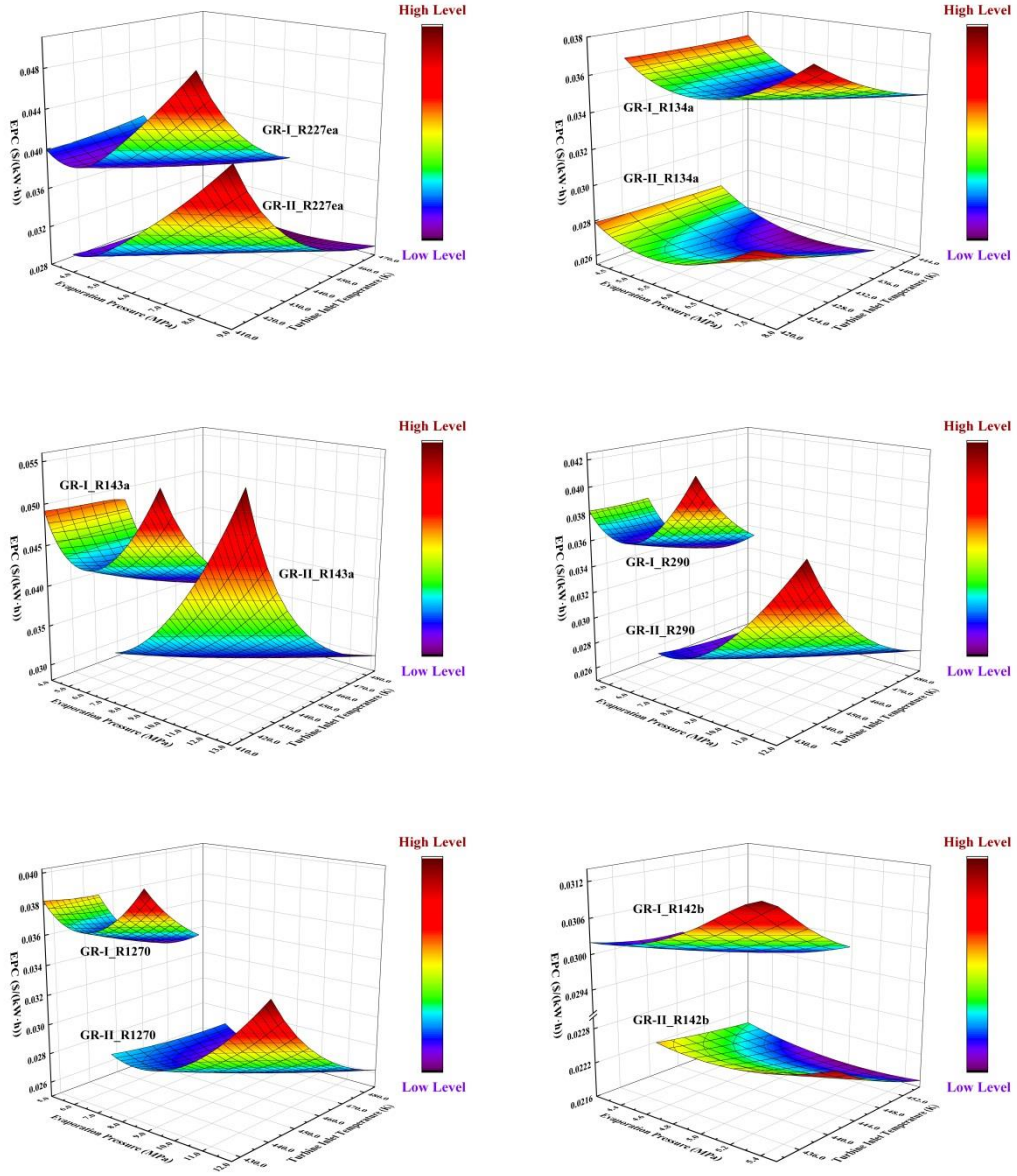


Fig. 8. Electricity production cost (EPC) variation in two geothermal reservoirs

535 EPC is directly proportional to the gross cost (Cost_{2019}) and inversely to the net
536 output power (P_{net}) and the whole working time ($h_{working-time}$) of the TORC system.
537 Hence, in the case of a certain $h_{working-time}$ with increasing the evaporation pressure
538 (P_4) under given turbine inlet temperature (T_4), Fig. 8 shows that EPC exhibits a
539 trend of decrease initially and increase afterwards for the reason that P_{net} increases
540 first and then decreases, meanwhile, the pressure tolerance of components is
541 required to enhance which leads to an inevitable increase in Cost_{2019} . Similarly, the
542 EPC decreases firstly and then increases when increasing T_4 under lower P_4 . The
543 explanation for this variation is similar with ranging P_4 but the discrepancy exists
544 that overall heat transfer areas keep increasing which draws an increase in Cost_{2019} .
545 When considering the limits of the maximal T_4 under higher P_4 , the upward
546 tendency of EPC would not appear anymore. By comparing the optimal results
547 between working fluids, the lowest EPC appears at R142b of 0.030(\$/(kW·h)) and
548 0.022(\$/(kW·h)) when the P_4 and T_4 are 4.6MPa, 445K and 5.1MPa, 455K in
549 GR-I and GR-II. Moreover, R143a gets higher EPC of 0.040(\$/(kW·h)) and
550 0.0285(\$/(kW·h)) for 7.6MPa, 445K and 9.4MPa, 485K of P_4 and T_4 .

3.3 Three-level fuzzy evaluation

As illustrated in maps of thermodynamic and techno-economic parameters above, the iteration outcomes can be exported by varying the tested evaporation pressure (P_4) and turbine inlet temperature (T_4) for each working fluid alternative. In the meantime, the case study regards the maximal P_{net} as objective function to obtain the optimal results for GR-I and GR-II. As listed in Tables 5 and 6, the values of the rest indexes such as η_t or APR are acknowledged under the same values of P_4 and T_4 when P_{net} gets the maximum. In this paper, the available options of scheme included R227ea (D1), R134a (D2), R143a (D3), R290 (D4), R1270 (D5) and R142b (D6). The decision criteria set is comprised of Safety Level (C1), ALT (C2), ODP (C3), GWP (C4), P_{net} (C5), η_t (C6), η_e (C7), APR (C8), SP (C9), $Cost_{2019}$ (C10), EPC (C11), DPP (C12) and SIR (C13).

563 Judging by the rules of criteria for higher-the-better such as C5, C6, C7 and
564 C12 or lower-the-better involving C1, C2, C3, C4, C8, C9, C10, C11 and C13, a
565 pair-wise comparison matrix of the P_{net} (C5) for schemes in GR-I is constructed
566 for instance. As depicted in Table 7, it can be seen that the values on diagonal line
567 are all 0.5 in the matrix on account of the P_{net} of each scheme is identical to itself.
568 When it comes to comparing the P_{net} of D1 to D2, the result is 0, because of the
569 value of P_{net} in D1 is lower than D2. Conversely, 1 is appeared when comparing
570 D2 with D1 for the P_{net} of D2 is higher than D1. The sum of each row is got after
571 the consistence checking between all the schemes. Arranging the sum of schemes in
572 a descending order, those are D6, D2, D4, D5, D1 and D3. Furthermore, since the
573 ranking is based on an interval of 0.5, D6 acquires the highest of 5.5 at the first
574 position and the semantic score is assigned 1. D2 obtains 4.5 and scored 0.818 in the
575 third place. The weighting is calculated by means of the semantic score for each
576 scheme dividing the sum semantic scores for all schemes in the normalization
577 process. Then, the weighting set for other twelve criteria are derived from the same
578 procedures. Tables 8 and 9 list the results of weighting matrix for all schemes (R_i)
579 after normalization in GR-I and GR-II.

Table 5 Simulated optimal results of GR-I

Working Fluid	P_4 /MPa	T_4 /K	P_{net} /kW	η_t /%	η_e /%	APR(m ² /kW)	SP/m	Cost ₂₀₁₉ (10 ⁵ \$)	EPC(\$/(kW·h))	DPP/Year	SIR	Scheme
R227ea	6.6	445	1158.13	10.78	39.40	0.338	0.068	31.84	0.038	4.062	3.115	D1
R134a	7.6	445	1318.65	12.31	44.91	0.308	0.064	32.59	0.034	3.589	3.466	D2
R143a	9.4	445	1115.41	10.64	38.29	0.325	0.052	32.69	0.041	4.380	2.923	D3
R290	7.6	445	1265.92	11.93	43.25	0.298	0.070	32.62	0.036	3.766	3.324	D4
R1270	8.6	445	1256.59	11.90	43.00	0.291	0.064	32.58	0.036	3.794	3.303	D5
R142b	5.2	445	1513.27	14.04	51.42	0.285	0.087	32.74	0.030	3.084	3.959	D6

Table 6 Simulated optimal results of GR-II

Working Fluid	P_4 /MPa	T_4 /K	P_{net} /kW	η_t /%	η_e /%	APR(m ² /kW)	SP/m	Cost ₂₀₁₉ (10 ⁵ \$)	EPC(\$/(kW·h))	DPP/Year	SIR	Scheme
R227ea	8.6	470	1694.22	11.31	33.42	0.234	0.067	34.94	0.029	2.923	4.153	D1
R134a	7.4	440	1821.87	12.12	35.90	0.214	0.064	34.08	0.026	2.621	4.578	D2
R143a	13	485	1760.56	12.01	34.96	0.219	0.051	37.82	0.030	3.060	3.988	D3
R290	11.2	485	1966.04	13.28	38.92	0.199	0.068	36.98	0.026	2.637	4.554	D4
R1270	11.8	485	1981.99	13.43	39.28	0.191	0.063	37.14	0.026	2.626	4.571	D5
R142b	5.5	455	2179.54	14.43	42.89	0.187	0.087	33.98	0.022	2.146	5.494	D6

Table 7 Consistence checking, semantic score assignment and weighting calculation of net output power (P_{net}) for scheme

C5	D1	D2	D3	D4	D5	D6	Sum	Score	Weighting
D1	0.5	0	1	0	0	0	1.5	0.429	0.1133
D2	1	0.5	1	1	1	0	4.5	0.818	0.2161
D3	0	0	0.5	0	0	0	0.5	0.333	0.088
D4	1	0	1	0.5	1	0	3.5	0.667	0.1762
D5	1	0	1	0	0.5	0	2.5	0.538	0.1422
D6	1	1	1	1	1	0.5	5.5	1	0.2642

Table 8 Weighting of decision criteria for each scheme after normalization of semantic score in GR-I

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13
D1	0.2383	0.1133	0.1806	0.1133	0.1133	0.1133	0.1133	0.088	0.1422	0.2642	0.1133	0.1133	0.1133
D2	0.2383	0.1762	0.1806	0.1762	0.2161	0.2161	0.2161	0.1422	0.2161	0.1762	0.2161	0.2161	0.2161
D3	0.1429	0.088	0.1806	0.088	0.088	0.088	0.088	0.1133	0.2642	0.1133	0.088	0.088	0.088
D4	0.1022	0.2161	0.1806	0.2161	0.1762	0.1762	0.1762	0.1762	0.1133	0.1422	0.1762	0.1762	0.1762
D5	0.1022	0.2642	0.1806	0.2642	0.1422	0.1422	0.1422	0.2161	0.1762	0.2161	0.1422	0.1422	0.1422
D6	0.1761	0.1422	0.097	0.1422	0.2642	0.2642	0.2642	0.2642	0.088	0.088	0.2642	0.2642	0.2642

Table 9 Weighting of decision criteria for each scheme after normalization of semantic score in GR-II

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13
D1	0.2383	0.1133	0.1806	0.1133	0.088	0.088	0.088	0.088	0.1422	0.1762	0.1133	0.1133	0.1133
D2	0.2383	0.1762	0.1806	0.1762	0.1422	0.1422	0.1422	0.1422	0.1762	0.2161	0.2161	0.2161	0.2161
D3	0.1429	0.088	0.1806	0.088	0.1133	0.1133	0.1133	0.1133	0.2642	0.088	0.088	0.088	0.088
D4	0.1022	0.2161	0.1806	0.2161	0.1762	0.1762	0.1762	0.1762	0.1133	0.1422	0.1422	0.1422	0.1422
D5	0.1022	0.2642	0.1806	0.2642	0.2161	0.2161	0.2161	0.2161	0.2161	0.1133	0.1762	0.1762	0.1762
D6	0.1761	0.1422	0.097	0.1422	0.2642	0.2642	0.2642	0.2642	0.088	0.2642	0.2642	0.2642	0.2642

580 According to the property diversities of the thirteen decision criteria, they can
581 be divided into three levels. The first level considers safety and environmental
582 friendly properties which contains C1~C4. The second level concerns with
583 thermodynamic qualities including C5~C7. As for the third level, it is made up of
584 C8~C13 with concentrating on techno-economic characteristics. Differential from
585 the semantic score assignment and weighting calculation of criteria in pair-wise
586 matrix established for schemes as shown in Table 7, Table 10 summarizes the
587 pair-wise matrix built for the three levels in GR-I and GR-II, in which the criteria
588 are compared within the same hierarchy. E.g., ranking the relative importance
589 among criteria in the first level, that is C3, C4, C2, and C1. Namely, when
590 comparing C1 with C2, the result is 0 because of C1 is less significant than C2. After
591 the consistency checking of C1~C4 in the first level and arranging the sum of each
592 criterion in descending order, in which the ranking is identical to the importance
593 sequence. Moreover, it is because that the ranking is based on an interval of 1.0, thus,
594 C3 ranks first for getting 3.5 and assigned the semantic score of 1. C4 ranks second
595 and scored 0.919 due to a sum of 2.5. For the criteria in levels two and three, the
596 relative importance rankings are C7, C6, C5 and C11, C13, C12, C10, C8, C9
597 respectively. Similarly, the semantic score assignment and weighting calculation are
598 performed the same as the first level demonstrated earlier.

Table 10 Consistence checking, semantic score assignment and weighting calculation of decision criteria for three levels

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	Sum	Score	Weighting
C1	0.5	0	0	0										0.5	0.739	0.2135
C2	1	0.5	0	0										1.5	0.818	0.2363
C3	1	1	0.5	1										3.5	1	0.2888
C4	1	1	0	0.5										2.5	0.905	0.2614
C5					0.5	0	0							0.5	0.818	0.3004
C6					1	0.5	0							1.5	0.905	0.3324
C7					1	1	0.5							2.5	1	0.3672
C8								0.5	1	0	0	0	0	1.5	0.667	0.141
C9								0	0.5	0	0	0	0	0.5	0.6	0.1269
C10								1	1	0.5	0	0	0	2.5	0.739	0.1563
C11								1	1	1	0.5	1	1	5.5	1	0.2114
C12								1	1	1	0	0.5	0	3.5	0.818	0.173
C13								1	1	1	0	1	0.5	4.5	0.905	0.1914

599 Referring to the last step of three-level fuzzy decision method, the final
600 evaluation results can be acquired by multiplying the weighting matrix of criteria for
601 three levels (W_i) and the weighting matrix for schemes (R_i). What accounts more is
602 that the first level result should be inserted as last row in R_i of the second level.
603 Furthermore, W_i for second level is multiplying 3/4 as well. And then the
604 equivalent weight needs to be assigned as 1/4 and added in the fourth position of
605 W_i in order to keep the weighting matrix dimension consistency. Repeatedly, the
606 result for the third level can be obtained by substituting 3/4 and 1/4 with 6/7 and 1/7.

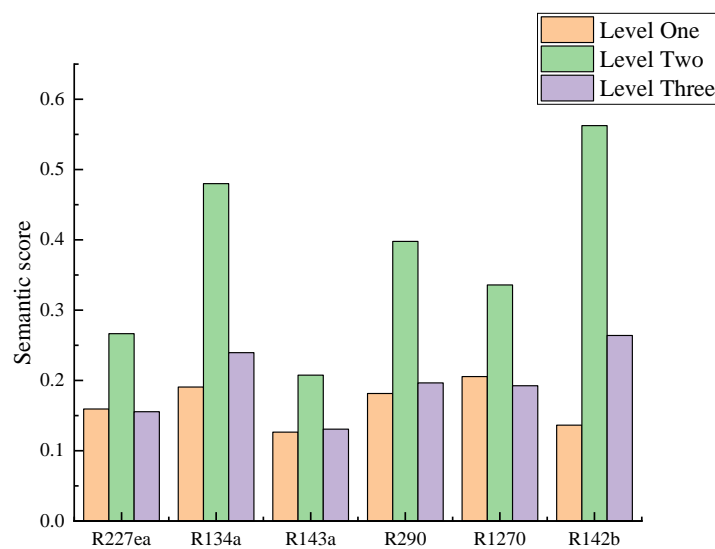


Fig. 9. Results of three-level fuzzy evaluation for GR-I

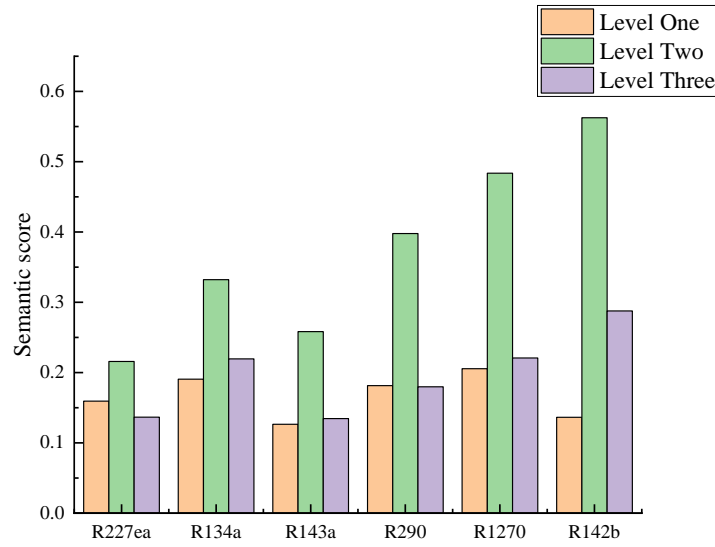


Fig. 10. Results of three-level fuzzy evaluation for GR-II

607 Figs. 9 and 10 exhibit the comparisons of the three-level evaluation results for
 608 GR-I and GR-II. It is concluded that the first level evaluation result are equally in
 609 the two geothermal reservoirs. R1270 possess the best reliability when only
 610 concerns about safety and environmental friendly properties. The second and third
 611 level evaluation results show that R142b is the optimal one which behaves excellent
 612 thermodynamic and techno-economic performance among selected working fluids.
 613 To the opposite, R143a is not much appropriate for the geothermal operation process
 614 according to the three-level evaluation results.

615 What's more, it is noteworthy that the third level evaluation result for GR-I in
 616 Fig.9 is consistent with the optimal ranking result of P_{net} in Table 5. However,
 617 comparing the result in Fig.10 and Table 6, which exerts difference between the
 618 evaluation and optimal raking order with respect to GR-II. It is implied that the
 619 impact of techno-economic indexes on the overall system performance is more
 620 apparent at high temperatures.

4 Conclusions

Based on the constructed environmental, thermodynamic and techno-economic assessment models, this paper develops a three-level fuzzy decision method for TORC system used in medium and high temperature geothermal reservoirs. The optimal results of the geothermal TORC system are obtained when P_{net} reaches the maximum. The evaluation results are gained by semantic score assignment, weighting calculation and order ranking. Both of results contribute to the following conclusions:

1. According to the first level evaluation result, the ranking of the working fluid is R1270, R134a, R290, R227ea, R142b and R143a which is identical to both GR-I and GR-II.

2. The second level takes into account the first level result and thermodynamic characteristics, ranking like R142b, R134a, R290, R1270, R227ea, R143a for GR-I and R142b, R1270, R290, R134a, R143a, R227ea for GR-II. It is concluded that R142b is both the most suitable working fluid for its maximal net output power. By contrast of the second level evaluation results for R134a in the two geothermal reservoirs, the heat source with lower temperature and pressure in GR-I is more compatible with it.

3. In terms of the third level, it takes the former two levels results and techno-economic properties into consideration. The evaluation ranking is R142b, R134a, R290, R1270, R227ea and R143a for GR-I. For GR-II ranks R142b, R1270, R134a, R290, R227ea and R143a. From the comprehensive standpoint of the three-level evaluation results, R142b is recommended as best one for the geothermal TORC systems.

The three-level fuzzy decision method developed in this work can effectively figure out the influence of a former level decision criteria on the latter one. The designers can decide on strategies and solutions according to practical requirements by adjusting weighting on indexes. It also helps the investors make whole-scale judgements in the pre-design stage of geothermal ORC system. As for the future work employed with this methodology, it can be extended to analyze the optimization process and make reliable design decisions for different ORC layout.

Acknowledgements

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Reference

- [1] Anderson A, Rezaie B. Geothermal technology: Trends and potential role in a sustainable future. *Appl Energy* 2019; 248:18-34.
<https://doi.org/10.1016/j.apenergy.2019.04.102>.
- [2] Statistical review of world energy,
<https://www.bp.com/en/global/corporate/energy-economics/statistical-review-of-world-energy.html>; 2020.
- [3] Limberger J, Boxem T, Pluymaekers M et al. Geothermal energy in deep aquifers: A global assessment of the resource base for direct heat utilization. *Renew Sustain Energy Rev* 2018; 82:961-975.
<https://doi.org/10.1016/j.rser.2017.09.084>.
- [4] Moloney F, Almatrafi E, Goswami DY. Working fluid parametric analysis for recuperative supercritical organic Rankine cycles for medium geothermal reservoir temperatures. *Renew Energy* 2020; 147:2874-2881.
<https://doi.org/10.1016/j.renene.2018.09.003>.
- [5] Liang Y, Sun Z, Dong M et al. Investigation of a refrigeration system based on combined supercritical CO₂ power and transcritical CO₂ refrigeration cycles by waste heat recovery of engine. *Int J Refrig* 2020; 118:470-482.
<https://doi.org/10.1016/j.ijrefrig.2020.04.031>.
- [6] Li XY, Shu GQ, Tian H. Integrating off-design performance in designing CO₂ power cycle systems for engine waste heat recovery. *Energy Conver Manage* 2019; 201:112146. <https://doi.org/10.1016/j.enconman.2019.112146>.
- [7] Song J, Gu CW, Ren XD. Parametric design and off-design analysis of organic Rankine cycle (ORC) system. *Energy Conver Manage* 2016; 112:157-165.
<https://doi.org/10.1016/j.enconman.2015.12.085>.

-
- [8] Wang X, Shu GQ, Tian H et al. Effect factors of part-load performance for various Organic Rankine cycles using in engine waste heat recovery. *Energy Conver Manage* 2018; 174:504-515.
<https://doi.org/10.1016/j.enconman.2018.08.024>.
- [9] Madhawa Hettiarachchi HD, Golubovic M, Worek WM, Ikegami Y. Optimum design criteria for an Organic Rankine cycle using low-temperature geothermal heat sources. *Energy* 2007; 32:1698-1706.
<https://doi.org/10.1016/j.energy.2007.01.005>.
- [10] Astolfi M, Romano MC, Bombarda P, Macchi E. Binary ORC (organic Rankine cycles) power plants for the exploitation of medium–low temperature geothermal sources – Part A: Thermodynamic optimization. *Energy* 2014; 66:423-434. <https://doi.org/10.1016/j.energy.2013.11.056>.
- [11] Astolfi M, Romano MC, Bombarda P, Macchi E. Binary ORC (Organic Rankine Cycles) power plants for the exploitation of medium–low temperature geothermal sources – Part B: Techno-economic optimization. *Energy* 2014; 66:435-446. <https://doi.org/10.1016/j.energy.2013.11.057>.
- [12] Vetter C, Wiemer HJ, Kuhn D. Comparison of sub- and supercritical Organic Rankine Cycles for power generation from low-temperature/low-enthalpy geothermal wells, considering specific net power output and efficiency. *Appl Therm Eng* 2013; 51:871-879.
<https://doi.org/10.1016/j.applthermaleng.2012.10.042>.
- [13] Sun J, Liu Q, Duan Y. Effects of evaporator pinch point temperature difference on thermo-economic performance of geothermal organic Rankine cycle systems. *Geothermics* 2018; 75:249-258.
<https://doi.org/https://doi.org/10.1016/j.geothermics.2018.06.001>.
- [14] Meng D, Liu Q, Ji Z. Performance analyses of regenerative organic flash cycles for geothermal power generation. *Energy Conver Manage* 2020; 224:113396. <https://doi.org/https://doi.org/10.1016/j.enconman.2020.113396>.

-
- [15] Cakici DM, Erdogan A, Colpan CO. Thermodynamic performance assessment of an integrated geothermal powered supercritical regenerative organic Rankine cycle and parabolic trough solar collectors. *Energy* 2017; 120:306-319. <https://doi.org/10.1016/j.energy.2016.11.083>.
- [16] Wang XC, Levy EK, Pan CJ et al. Working fluid selection for organic Rankine cycle power generation using hot produced supercritical CO₂ from a geothermal reservoir. *Appl Therm Eng* 2019; 149:1287-1304. <https://doi.org/10.1016/j.applthermaleng.2018.12.112>.
- [17] Heberle F, Schifflechner C, Bruggemann D. Life cycle assessment of Organic Rankine Cycles for geothermal power generation considering low-GWP working fluids. *Geothermics* 2016; 64:392-400. <https://doi.org/10.1016/j.geothermics.2016.06.010>.
- [18] Jankowski M, Borsukiewicz A, Wisniewski S, Hooman K. Multi-objective analysis of an influence of a geothermal water salinity on optimal operating parameters in low-temperature ORC power plant. *Energy* 2020; 202. <https://doi.org/10.1016/j.energy.2020.117666>.
- [19] Mohammadzadeh Bina S, Jalilinasrabady S, Fujii H. Thermo-economic evaluation of various bottoming ORCs for geothermal power plant, determination of optimum cycle for Sabalan power plant exhaust. *Geothermics* 2017; 70:181-191. <https://doi.org/10.1016/j.geothermics.2017.06.007>.
- [20] Wang JS, Diao MZ, Yue KH. Optimization on pinch point temperature difference of ORC system based on AHP-Entropy method. *Energy* 2017; 141:97-107. <https://doi.org/10.1016/j.energy.2017.09.052>.
- [21] Zhou GY, Wu E, Tu ST. Optimum selection of compact heat exchangers using non-structural fuzzy decision method. *Appl Energy* 2014; 113:1801-1809. <https://doi.org/10.1016/j.apenergy.2013.07.041>.

-
- [22] Manente G, Da Lio L, Lazzaretto A. Influence of axial turbine efficiency maps on the performance of subcritical and supercritical Organic Rankine Cycle systems. *Energy* 2016; 107:761-772.
<https://doi.org/10.1016/j.energy.2016.04.063>.
- [23] Martin H. A theoretical approach to predict the performance of chevron-type plate heat exchangers. *Chem Eng Process* 1996; 35:301-310.
[https://doi.org/10.1016/0255-2701\(95\)04129-x](https://doi.org/10.1016/0255-2701(95)04129-x).
- [24] Wang Z-Z, Zhao Z-N. Analysis of Performance of Steam Condensation Heat Transfer and Pressure Drop in Plate Condensers. *Heat Transfer Eng* 1993; 14:32-41. <https://doi.org/10.1080/01457639308939809>.
- [25] Pioro IL, Khartabil HF, Duffey RB. Heat transfer to supercritical fluids flowing in channels—empirical correlations (survey). *Nucl Eng Des* 2004; 230:69-91. <https://doi.org/10.1016/j.nucengdes.2003.10.010>.
- [26] Imran M, Usman M, Park BS, Yang Y. Comparative assessment of Organic Rankine Cycle integration for low temperature geothermal heat source applications. *Energy* 2016; 102:473-490.
<https://doi.org/10.1016/j.energy.2016.02.119>.
- [27] Kuo WS, Lie YM, Hsieh YY, Lin TF. Condensation heat transfer and pressure drop of refrigerant R-410A flow in a vertical plate heat exchanger. *Int J Heat Mass Transf* 2005; 48:5205-5220.
<https://doi.org/10.1016/j.ijheatmasstransfer.2005.07.023>.
- [28] Turton R, Shaeiwitz JA, Bhattacharyya D, Whiting WB. Analysis, synthesis, and design of chemical processes. 5th ed; 2018.
- [29] Jenkins S. 2019 Chemical engineering plant cost index annual average, <https://www.chemengonline.com/2019-chemical-engineering-plant-cost-index-annual-average/>; 2020.

-
- [30] Zhang C, Liu C, Wang S et al. Thermo-economic comparison of subcritical organic Rankine cycle based on different heat exchanger configurations. Energy 2017; 123:728-741. <https://doi.org/10.1016/j.energy.2017.01.132>.

1 **A non-structural fuzzy decision method developed for**
2 **organic Rankine cycles used in liquid-dominated**
3 **geothermal fields of medium/high temperature**

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Abstract

A reliable decision-making method is of great importance for the designing of a practical and efficient organic Rankine cycle (ORC) system employed to exploit geothermal energy. This paper develops a three-level non-structural fuzzy decision algorithm for the comprehensive evaluation of a geo-fluid driven trans-critical ORC (TORC) system on the basis of a progressive system performance hierarchy, involving environmental characteristics, safety, thermodynamic and techno-economic performance. Two representative geothermal reservoirs with medium (GR-I) and high (GR-II) temperature are investigated to realize and validate the proposed method. Four mathematical models and six working fluids with thirteen indexes are developed to fulfill the performance evaluation and decision-making courses. Parametric analysis results of the decision criteria are conducted including specific net out power (AP_{net}), thermal efficiency (η_t), exergy efficiency (η_e), heat transfer area per net output power (APR) and electricity production cost (EPC), and the different performance of TORC for GR-I and GR-II are fully revealed. As for the GR-I, the result of the three-level fuzzy decision ranking order is R142b, R134a, R290, R1270, R227ea and R143a. In regard to the GR-II, it's R142b, R1270, R134a, R290, R227ea and R143a. Both show that R142b performs best. In the GR-I and GR-II, R142b obtains the maximal AP_{net} of 110.94kW/(kg·s⁻¹) and 198.14kW/(kg·s⁻¹), the maximal η_t of 14.05% and 14.43%, the maximal η_e of 51.42% and 42.90%, the minimal APR of 0.262(m²/kW) and 0.185(m²/kW), the minimal EPC of 0.030(\$/(kW·h)) and 0.022(\$/(kW·h)).

32 Summarily, this three-level fuzzy decision evaluation method can provide
33 important guidance and decisive solution by concisely display the pros and cons for
34 each ORC scheme of geothermal resource utilization.

35 **Keywords:** Geothermal energy; Trans-critical ORC; Three-level performance
36 evaluation; non-structural fuzzy decision method

Introduction

Dramatic increase in energy consumption attributes to the fast population expansion and economic growth. A large proportion of energy supply for electricity is currently generated by the combustion of organic fuels, which leads to the growing greenhouse effect and air pollution concerns. For the purpose of human society sustainable progress, renewable resource like geothermal is capable of providing the majority of activities energy with power production, heating and cooling applications [1]. However, the cumulative installed geothermal power capacity in the globe is only increasing from 7.92GW at 2001 to 13.93GW at 2019, which is far away from the growth rate of solar and wind [2]. The conflict between the huge reserve and exploitation of geothermal resources lies in the expensive initial investments [3]. Besides that, the geothermal utilization also relies on the public awareness of environment protection as well as the efficiency enhancement of technologies [1].

51 The organic Rankine cycle (ORC) has been regarded as a preferred rational
52 solution to harvesting energy from all kinds of heat sources such as waste heat and
53 geothermal reservoirs [4]. Studies on ORC-based waste heat system are devoted to
54 optimizing the engine performance. Liang et al. [5] proposed a small-scale waste
55 heat driven cooling system which integrated supercritical CO₂ power cycle and
56 trans-critical CO₂ refrigeration cycle to recover the waste heat from internal
57 combustion engine and provide cooling energy for refrigerated truck. Li et al. [6]
58 presented a novel framework for analyzing the off-design performance of CO₂
59 trans-critical power cycle and applied in the heavy-duty truck engine. Song et al. [7]
60 conducted a one-dimensional off-design performance analysis of ORC system by
61 optimizing the turbine aerodynamic model. Wang et al. [8] investigated the part-load
62 performance of ORC system based on the engine waste heat recovery with varying
63 evaporation pressure, condensing condition, working fluid and cycle structure,
64 which revealed that the slower the output power decrease, the better the
65 performance.

Normally, the geothermal heat is categorized as high, medium and low temperature with temperature ranges of $>220^{\circ}\text{C}$, $220\text{-}100^{\circ}\text{C}$ and $100\text{-}70^{\circ}\text{C}$, respectively [9]. The thermodynamic as well as the techno-economic indicators are the major criteria for making investment decisions, which show direct relevance with the utilization benefit of geothermal energy. Summarizing from previous work about geothermal ORC system, researchers are committed to simulating the actual operating process for improving the system thermodynamic and economic performance. Astolfi et al. [10, 11] completed thermodynamic and techno-economic assessments of the ORCs (subcritical, trans-critical, saturated, superheated, regenerative and non-regenerative) for medium temperature geothermal brines. Regarding cycle efficiency and electricity cost as objective functions, the optimization results suggested deploying different cycle layouts that needed to consider the suitable working conditions and economic parameters simultaneously. Vetter et al. [12] analyzed the potential relevance between the maximal net output power and working fluid critical temperature with geothermal fluid temperature in the subcritical and trans-critical ORC system. It found out the highest net output power appeared when the ratio of working fluid critical temperature and geothermal fluid temperature was 0.8. Additionally, the geothermal ORC combined with different subsystem is a feasible way to make system thermo-economic performance better. Sun et al. [13] investigated the effect of pinch point temperature difference (PPTD) on the geothermal ORC thermo-economic performance. The optimization results showed that the optimal evaporation temperature and the heat transfer area

88 per unit power output decreased with increasing PPTD. The levelized cost of
89 electricity and the dynamic payback period reached minimal when PPTD was 7°C.
90 Meng et al. [14] further explored the interaction between the evaporation and flash
91 temperature on recovering heat from medium temperature geothermal brine. Cakici
92 et al. [15] performed the energy and exergy analysis of trans-critical regenerative
93 ORC system combined with parabolic trough solar collectors. The integrated system
94 net output power increased while the electricity and exergy efficiency decreased
95 compared to single system, and R134a yielded outstanding thermodynamic
96 performance with an increment of the geothermal water inlet temperature and
97 collector areas.

98 Since the ORC system efficiency depends on the refrigerants properties,
99 researchers also have paid much attention on optimal selection of working fluids
100 with thermodynamic laws assessments. Moloney et al. [4] investigated
101 thermodynamic performance of recuperative trans-critical ORC system for a range
102 of medium to high temperature geothermal reservoirs, indicating that R1233zd(E),
103 R600, R601a, R601, R601b performed the best among twenty working fluids when
104 taken plant efficiency as optimization parameters. Wang et al. [16] developed a
105 working fluid selection methodology mainly based on the thermodynamic
106 performance for the subcritical, superheated, and trans-critical ORC system,
107 utilizing supercritical CO₂ as heat extraction medium in the high temperature
108 geothermal reservoir. The working fluid was recommended when the net output
109 power, specific net output power, thermal efficiency and exergy efficiency were
110 simultaneously equal or greater than their median value. Furthermore, some studies
111 adopt evaluation tool which takes account of environmental properties of working
112 fluids. Heberle et al. [17] qualified the potential of low GWP working fluids like
113 R600, R601a, R290, R1233zd, R1234yf as alternatives for fluorinated fluids like
114 R245fa during the life cycle assessment in the binary geothermal power plant.
115 Judging by the exergy and environmental analysis results, the low GWP working
116 fluids had less effect on environment and higher exergy efficiency in comparison to
117 fluorinated fluids, and the two-stage subcritical ORC and trans-critical ORC
118 manifested better than one-stage subcritical ORC system. For the purpose that
119 avoids the occurrence of refrigerant leakage and guarantees the stable working

120 conditions of geothermal ORC system, it depends on selecting working fluids with
121 environmental friendly, safety, low flammability and excellent thermodynamic and
122 techno-economic characteristics.

Plenty of investigations are discretely concerned about environmental, thermodynamic and economic performance of geothermal ORC system. But they might neglect the internal relationship between the effective factors. Consequently, a few literatures started to search for multi-objective optimization techniques. Jankowski et al. [18] investigated the influence of geothermal brine salinity on the performance in the subcritical ORC power plant. Taking the minimal heat transfer area and maximal exergy efficiency as the multi-objective parameters under Genetic Algorithm, the Pareto point demonstrated that the heat transfer area increased 8% and exergy efficiency decreased 5% with an increment in salinity. Bina et al. [19] constructed multi-criteria fuzzy TOPSIS decision making method for selecting most favorable cycle configuration in geothermal power plant, covering exergy efficiency, thermal efficiency, net output power, production cost, total cost rate the five indicators. From the thermo-economic perspective and interval Shannon's entropy weighting calculation, the ORC system with internal heat exchanger ranked the first. Wang et al. [20] explored the relationship of pinch point temperature difference (PPTD) between evaporator and condenser in the thermo-economic optimization process of subcritical ORC system. Based on the Analytic Hierarchy Process (AHP) method which cared about the energy output, energy output efficiency and economic criteria, it determined the best working fluid for 150°C hot water was R11 and the optimal ratio of PPTD was from 1.25 to 1.5.

143 Although numerous studies have discussed the optimization and evaluation
144 process, the objective indicators just covered relatively limited side and couldn't
145 give a thorough analysis of the overall ORC system performance. The non-structural
146 fuzzy decision method is widely used as an efficient approach for comprehensive
147 evaluation, which considers the indexes interrelation and provides intuitive
148 comparison of the assessed schemes. Zhou et al. [21] adopted non-structural fuzzy
149 decision method for pre-design process of compact heat exchangers which united
150 the thermodynamic, economic and mechanical the three levels evaluation indexes. In
151 the light of the third level evaluation result, the first alternative for sulfuric acid
152 solution cooler was plate-fin heat exchanger fabricated by PTFE.

153 It can be found that most previous investigations about geothermal ORC
154 system incline to take basis of first and second laws analysis with thermodynamics,
155 focusing on these aspects of thermodynamic and techno-economic performance
156 evaluation, system structure and layout, objective optimization and working fluid
157 selection. Regarding the simulated results of highest net output power or lowest
158 initial investment Cost as criterion to determine the best ORC system scheme.
159 However, the assessment process tends to concentrate on one level decision criteria
160 like thermodynamic indicators, which fails to integrate the comprehensive influence
161 of techno-economic and social benefit indicators on the system whole performance.
162 It may lead the pre-designed scheme to an unachievable goal and cause irretrievable
163 loss to the investors.

164 Thus, this paper aims at developing an efficient and practical decision-making
165 method, i.e. a three-level non-structural fuzzy decision method, based on
166 comprehensive performance evaluation of the ORC employed for typical geothermal
167 reservoirs. During the whole assessment procedures, six working fluids and three
168 levels of performance are investigated, including the safety and environmental
169 property as the first level, thermodynamic performance as the second level and the
170 techno-economic performance as the third level. A non-structural fuzzy
171 decision-making method is then developed based on the three-level assessment to
172 eventually implement practical and reliable decision-making for the geothermally
173 driven ORC systems.

1 System description

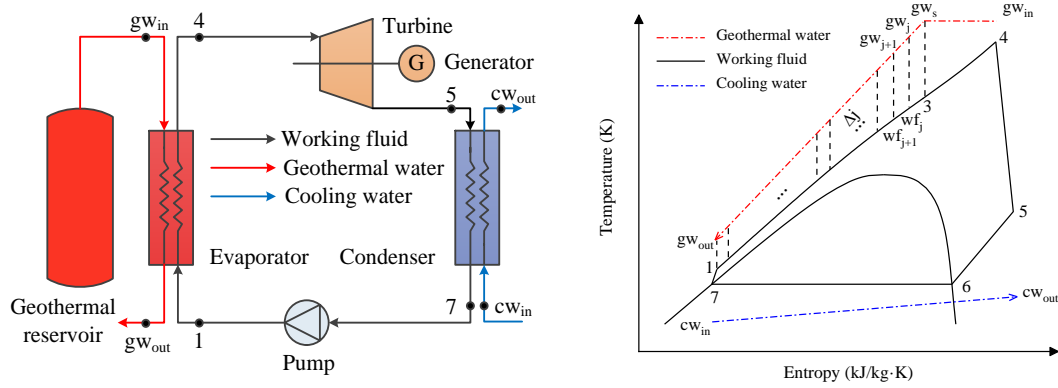


Fig. 1. Schematic and T-s diagram of TORC system

Table 1 Operating conditions of TORC system

Parameter	Value
GR-I wellhead temperature, T_{gwin-1} (°C)	182.23
GR-I wellhead pressure, P_{gw-1} (MPa)	1.06
GR-I wellhead mass flow rate, m_{gw-1} (kg/s)	13.64
GR-II wellhead temperature, T_{gwin-2} (°C)	224.37
GR-II wellhead pressure, P_{gw-2} (MPa)	2.52
GR-II wellhead mass flow rate, m_{gw-2} (kg/s)	11
Condensing temperature, T_{cond} (°C)	35
Cooling water inlet temperature, T_{cwin} (°C)	20
Evaporator pinch point temperature, $T_{pinch-e}$ (°C)	10
Condenser pinch point temperature, $T_{pinch-c}$ (°C)	5
Turbine isentropic efficiency, $\eta_{turbine}$	0.75
Pump isentropic efficiency, η_{pump}	0.7
Dead state temperature, T_{dead} (°C)	20
Dead state pressure, P_{dead} (MPa)	0.101

175 The geothermal reservoirs under investigation in this work are located in the
176 Aluto Langano geothermal field of Ethiopia, which is recognized as a medium/high
177 temperature liquid-dominated geothermal field in eastern Africa. Two typical and
178 active geothermal reservoirs (i.e., Geothermal Reservoir I and Reservoir II) are
179 chosen as heat source for the proposed system. They produced two-phase,
180 fluid-dominated wellhead discharge, and the discharge data from wellhead tests are
181 gathered and listed in Table 1. Wellhead pressure, temperature and mass flow rate
182 are tested in situ. Instead of choosing the basic sub-critical ORC pattern, the
183 trans-critical ORC (TORC) is determined for its higher energy efficiency, lower
184 exergy loss and modest pressure requirement [22]. The primary TORC system
185 working conditions constructed for working fluids in the GR-I (182.23°C) and GR-II
186 (224.37°C) are nearly identical except the investigated evaporation pressure and
187 turbine inlet temperature and flow channels in heat exchangers. Table 1 lists the
188 detailed value of relevant parameters for TORC design and construction. As
189 demonstrated in the semantic definition of TORC, the working fluid is compressed
190 to exceed critical pressure via pump. And it absorbs heat from geothermal water to
191 vaporize until it reaches the highest temperature during the courses of evaporation.
192 Then, the supercritical working fluid discharges into the turbine to produce output
193 shaft work which can be employed for power generation. After expansion, the
194 subcritical overheated vapor is condensed into saturated liquid by cooling water
195 before flowing into the pump to accomplish the next cycle. The schematic and T-s
196 diagram is illustrated in Fig. 1. The T-s diagram also shows the segment-iterative

197 process of seeking pinch point temperature between the heat source and working
198 fluids.

Table 2 Fluid characteristics [4, 16]

Working Fluid	Thermodynamic Property					Environmental Property				
	M /(kg·kmol ⁻¹)	T_b /°C	T_{de} /K	T_{cr} /K	P_{cr} /MPa	Behavior	Safety Level	ALT/Year	ODP	GWP/(100 years)
R227ea	170.0289	-16.341	475	374.9	2.925	dry	A1	38.9	0	3320
R134a	102.032	-26.0738	455	374.21	4.0593	wet	A1	13.4	0	1430
R143a	84.041	-47.2406	650	345.857	3.761	wet	A2L	47.1	0	4470
R290	44.0956	-42.1138	650	369.89	4.2512	wet	A3	0.034	0	5
R1270	42.0797	-47.6192	575	364.211	4.555	wet	A3	0.001	0	1.8
R142b	100.495	-9.1233	470	410.26	4.055	isentropic	A2	17.2	0.065	2310

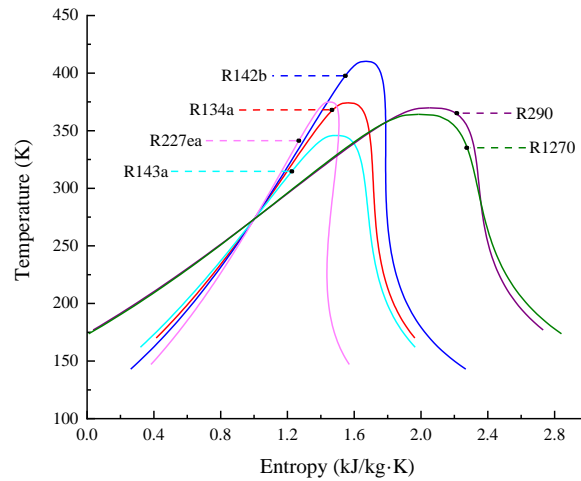


Fig. 2. T-s diagram of selected working fluids

199 The operating process of TORCs for two geothermal reservoirs are simulated in
200 MATLAB with six picked working fluids, the environmental and thermodynamic
201 characteristics of each working fluid are displayed in Table 2 and Fig. 2. The
202 principals for selecting working fluids are subject to the safety level, atmospheric
203 life time (ALT), ozone depletion potential (ODP) and global warming potential
204 (GWP).

205 For the safety level, A and B imply the toxicity grades while B is higher than A.
206 Number 1, 2, 2L and 3 indicate flammability level and increase progressively. ALT
207 represents existing time at the atmosphere if leakage of refrigerant happens, ODP
208 means the ozone consumption with refrigerant diffusing into ozone layer, and GWP
209 indicates the potential of temperature increase in the global world caused by
210 inappropriately release of refrigerant. With regard to the four environmental
211 indicators, the smaller value the better performance. And the iteration ranges of
212 turbine inlet temperature are higher than critical temperature but lower than working
213 fluids decomposition temperature. Furthermore, the assumptions stated as below are
214 taken into consideration:

- 215 ● Each TORC system is operating steadily.
- 216 ● No impurity like silica exists in the geothermal water, as result its outlet
217 temperature is allowed for lower than 70°C.
- 218 ● The pressure drop and heat losses are neglected during each part of
219 performing process.
- 220 ● The ambient temperature and pressure are 20°C and 101kPa.
- 221 ● The pinch point temperature in the evaporator and condenser are 10°C and
222 5°C respectively.

2 Mathematical modelling

2.1 Thermodynamic model

Based on the first and second laws of thermodynamics, the following formulas are introduced to calculate thermodynamic assessment indexes.

The heat transfer flow rate in the evaporator:

$$Q_{evaporator} = m_{wf} (h_4 - h_1) \quad (1)$$

The heat transfer flow rate in the condenser:

$$Q_{condenser} = m_{wf} (h_5 - h_7) \quad (2)$$

The consumed power of pump:

$$P_{pump} = m_{wf} (h_1 - h_7) \quad (3)$$

The turbine output shaft power:

$$P_{turbine} = m_{wf} (h_4 - h_5) \quad (4)$$

The net output power of TORC system:

$$P_{net} = P_{turbine} - P_{pump} \quad (5)$$

The specific net output power:

$$AP_{net} = P_{net} / m_{gw} \quad (6)$$

The thermal efficiency of TORC system:

$$\eta_t = P_{net} / Q_{evaporator} \times 100\% \quad (7)$$

Where m_{wf} and m_{gw} are the mass flow rate of working fluid and geothermal water, while h_i represents the specific state enthalpy with $i = 1 \dots 7$ as shown in Fig.

1.

244 The exergy of each state point:

245
$$E_i = m[(h_i - h_0) - T_0(s_i - s_0)] \quad (8)$$

246 Where m is the mass flow rate of objective fluid, while s_i represents the
247 state point entropy with $i = 1 \dots 7$, and the subscript 0 implies the ambient condition.

248 The exergy losses of pump:

249
$$I_{pump} = m_{wf} T_0 (s_1 - s_7) \quad (9)$$

250 The exergy losses of evaporator:

251
$$I_{evaporator} = (E_{gwin} + E_1) - (E_{gwout} + E_4) \quad (10)$$

252 The exergy losses of turbine:

253
$$I_{turbine} = m_{wf} T_0 (s_5 - s_4) \quad (11)$$

254 The exergy losses of condenser:

255
$$I_{condenser} = (E_{cwin} + E_5) - (E_{cwout} + E_7) \quad (12)$$

256 The exergy losses caused by cooling water flows out:

257
$$I_{out}^{cooling\ water} = E_{cwout} - E_{cwin} \quad (13)$$

258 The total exergy losses of TORC system:

259
$$I_{system} = I_{pump} + I_{evaporator} + I_{turbine} + I_{condenser} + I_{out}^{cooling\ water} \quad (14)$$

260 The net exergy that geothermal water flows into system:

261
$$E_{in}^{gw} = P_{net} + I_{system} \quad (15)$$

262 The exergy efficiency of TORC system:

263
$$\eta_e = P_{net} / E_{in}^{gw} \quad (16)$$

264 The subscript *in* and *out* refers to the inlet and outlet state for objective

265 fluid.

Before calculating the overall heat transfer coefficient and area of heat exchangers, the primary task is to identify the mass flow rate of working fluid. The inlet temperature (T_{gwin}) and mass flow rate of geothermal water (m_{gw}) are constant. Besides that, the minimal temperature difference is set larger than 10°C between the evaporator inlet temperature of geothermal water and outlet temperature of working fluid.

First of all, referring to the Pinch Point Temperature Difference method, the evaporator outlet temperature of geothermal water (T_{gwout}) is assumed to get the outlet enthalpy (h_{gwout}) and calculate initial value of working fluid mass flow rate (m_{wf}):

$$m_{wf} = m_{gw} (h_{gwin} - h_{gwout}) / (h_4 - h_1) \quad (17)$$

Secondly, the single-phase flow region of geothermal water from gw_s to gw_{out} point is divided into one hundred segments as shown in Fig. 1. Thus the temperature difference of each segment can be determined. As a result, it could deduce the next state point temperature (T_{gwj}) from the beginning of T_{gws} .

$$T_{gwj} = T_{gws} - (T_{gws} - T_{gwout}) / 100j \quad (18)$$

The subscript j denotes the divided segments which range from 1 to 100.

Thirdly, based on the acquired variables of h_{gwj} , h_{gwout} , m_{wf} , the enthalpy (h_{gwj}) and temperature (T_{gwj}) of each state point for working fluids from 1 to 3 point can be obtained by using the first laws of thermodynamics.

$$h_{wff} = h_1 + m_{gw} (h_{gwj} - h_{gwout}) / m_{wf} \quad (19)$$

287 Lastly, the actual temperature difference between geothermal water and
 288 working fluids of each segment can be calculated. And the minimal temperature
 289 difference (ΔT_{act}) could be found out. Comparing it with 10°C, if the discrepancy
 290 satisfies the accuracy requirement (1%), it demonstrates that the assumed evaporator
 291 outlet temperature of geothermal water is reasonable. Otherwise, it needs to go back
 292 to the first step to presume another outlet temperature until meets the accuracy
 293 requirement.

294 2.2 Heat transfer model

295 The plate heat exchanger is selected as evaporator and condenser for its
 296 excellent heat transfer performance and compact structure. The geometric structure
 297 and dimension of plate heat exchanger are summarized in Table 3.

Table 3 Geometry of plate heat exchanger

Parameter	Value
Chevron angle, β (°)	60
Plate width, L_w (m)	0.65
Plate thickness, t (m)	0.0005
Corrugation pitch, Λ (m)	0.0085
Corrugation depth, b (m)	0.0025
Surface enlargement factor, ϕ	1.19
Hydraulic diameter, D_h (m)	0.0042
Equivalent diameter, D_{eq} (m)	0.005
Coefficient of thermal conductivity, λ_{PHE} (kW/(m·K))	0.0163

298 The heat transfer process in the evaporation and condenser are both divided
 299 into two sections. As illustrated above, the evaporator separates into single-phase
 300 flow and two-phase flow region according to the thermo-physical state of
 301 geothermal water. Similarly, the heat transfer area of condenser is divided into
 302 cooling and condensing region on the basis of the thermo-physical state of working
 303 fluid.

304 For the single-phase flow of geothermal water in the evaporator and cooling
 305 water in the condenser, the Leveque correlation [23] is used to calculate the heat
 306 transfer coefficient, which are α_{sgw} and α_{cw} respectively.

307 The Wang and Zhao correlation [24] is applied for calculation of geothermal
 308 water two-phase flow heat transfer coefficient (α_{tgw}) in the evaporator.

$$309 \quad Nu = 0.00115(\text{Re}_l/H)^{0.983} \text{Pr}_l^{0.33} (\rho_l/\rho_v)^{0.248} \quad (20)$$

$$310 \quad \alpha_{tgw} = Nu\lambda_l/D_{eq} \quad (21)$$

$$311 \quad \text{Re}_l = G_{gw}(1-x_0)D_{eq}/\mu_l \quad (22)$$

$$312 \quad \text{Pr}_l = c_{p,l}\mu_l/\lambda_l \quad (23)$$

$$313 \quad H = c_{p,l}(T_{ave} - T_{wall}) / (i_{fg} + 0.68c_{p,l}(T_{ave} - T_{wall})) \quad (24)$$

Where the indicators with subscript l are calculated based on the mean temperature of steam and wall temperature (T_{ave}), and the indicators with subscript v are calculated based on the average steam temperature, λ represents the thermal conductivity of objective water, G_{gw} implies the total mass flux of geothermal water, x_0 is the vapor quality at the end state of two-phase flow region which sets as 0, D_{eq} is the equivalent diameter of plate heat exchanger, and i_{fg} represents the latent heat of water from liquid to vapor state.

As for the trans-critical working fluids in evaporator, Jackson correlation [25] is adopted to calculate the heat transfer coefficient ($\alpha_{tc, wf}$).

$$Nu = 0.0183 Re^{0.82} Pr^{0.5} (\rho_{wall} / \rho)^{0.3} (\bar{c}_p / c_p)^n \quad (25)$$

$$\alpha_{tc, wf} = Nu \lambda / D_h \quad (26)$$

$$\bar{c}_p = (h_{wall} - h_c) / (T_{wall} - T_c) \quad (27)$$

$$Re = \rho v D_h / \mu \quad (28)$$

$$Pr = c_p \mu / \lambda \quad (29)$$

$$\begin{aligned} n &= 0.4, T_c < T_{wall} < T_{cri}, 1.2T_{cri} < T_c < T_{wall} \\ n &= 0.4 + 0.2 \left[(T_{wall} / T_{cri}) - 1 \right], T_c < T_{cri} < T_{wall} \\ n &= 0.4 + 0.2 \left[(T_{wall} / T_{cri}) - 1 \right] \left[1 - 5 (T_c / T_{cri} - 1) \right], T_{cri} < T_c < 1.2T_{cri}, T_c < T_{wall} \end{aligned} \quad (30)$$

Where T_c is the characteristic temperature of working fluid and h_c is obtained based on it. Additionally, other indexes like ρ_{wall} and h_{wall} are acquired under the condition of plate heat exchanger wall-side temperature (T_{wall}), T_{cri} is the critical temperature of working fluid, and D_h is hydraulic diameter which calculated by $D_h = 2b/\phi$.

For the cooling part in the condenser, the Chisholm correlation [26] is employed for calculating the working fluid heat transfer coefficient (α_{swf}).

For the condensing part in the condenser, the Kandlikar correlation [27] is used to calculate the working fluid heat transfer coefficient (α_{twf}).

$$\alpha_l = 0.2092 (\lambda_l / D_h) \text{Re}_l^{0.78} \text{Pr}_l^{0.33} (\mu / \mu_{wall})^{0.14} \quad (31)$$

$$\text{Re}_l = G_{wf} D_h / \mu_l \quad (32)$$

$$\text{Pr}_l = c_{p,l} \mu_l / \lambda_l \quad (33)$$

$$Co = (\rho_v / \rho_l) (1/x_m - 1)^{0.8} \quad (34)$$

$$Fr_l = G_{wf}^2 / (\rho_l^2 g D_h) \quad (35)$$

$$Bo = q / G_{wf} i_{fg} \quad (36)$$

$$\alpha_{twf} = \alpha_l (0.25 Co^{-0.45} Fr_l^{0.25} + 75 Bo^{0.75}) \quad (37)$$

Where g implies the acceleration of gravity which is $9.8(\text{m/s}^2)$, G_{wf} is the total mass flow rate of working fluid, and x_m is the vapor quality which sets 0.5.

After acknowledging the heat transfer coefficient of each section, the heat exchanger areas (A) are derived from the following equations.

$$A = Q / U / \Delta T_m \quad (38)$$

$$1/U = 1/\alpha_{hot-side} + t/\lambda_{PHE} + 1/\alpha_{cold-side} \quad (39)$$

Where Q is the heat transfer mass flow and U is the overall heat transfer coefficient of each part, while ΔT_m is the log mean temperature difference between hot-side and cold-side and λ_{PHE} is the thermal conductivity of plate heat exchanger.

2.3 Techno-economic model

For the purpose of giving an all-around viewpoint on the techno-economic properties of the ORC system, six parameters are collected that covered two aspects of investment and expected return. In detail, which are heat transfer area per net output power (APR), turbine characteristic size parameters (SP), gross cost based on the latest economic indexes ($Cost_{2019}$), electricity production cost (EPC), depreciated payback period (DPP) and saving to investment ratio (SIR).

The APR is employed as evaluation **criterion** of the heat exchanger compactness, the more compact of the heat exchanger structure, the smaller the APR and the lower the initial investment, which is defined as:

$$APR = (A_e + A_c) / P_{net} \quad (40)$$

The SP is regarded as an indicator of the relative cost of TORC system by measuring the size of turbine, which is defined as:

$$SP = \sqrt{V_5} / \Delta h_{isen}^{0.25} \quad (41)$$

Where V_5 is the volume flow of turbine outlet (state point 5) while Δh_{isen} is isentropic enthalpy drop before and after expansion (state point 4 to 5).

The $Cost_{2019}$ is determined based on the Module Cost Technique [28], It represents the sum of bare module costs of the main components in ORC system, which is given below:

$$Cost_{2001} = C_{BM, pump} + C_{BM, evaporator} + C_{BM, turbine} + C_{BM, condenser} \quad (42)$$

$$Cost_{2019} = Cost_{2001} CEPCI_{2019} / CEPCI_{2001} \quad (43)$$

376 Where $CEPCI$ is the chemical engineering plant cost index while
377 $CEPCI_{2001} = 397$ and $CEPCI_{2019} = 607.5$ [29].

378 As presented in Table 4, the bare module cost (C_{BM}) is defined as the product
379 of purchased cost (C_p) and bare module cost factor (F_{BM}). C_p is related to the
380 capacities ($P_{pump}, P_{turbine}$) and size parameters (A_e, A_c) of each component which are
381 acquired from the optimal results. F_{BM} considers the material factor (F_M) and
382 pressure factor (F_p). The materials for heat exchangers and pump are stainless steel
383 and the pump type is centrifugal. Then, the coefficients like B, C, K could be
384 determined by the arranged configurations.

Table 4 Main components bare module cost equations

Component	Bare module cost equation	Coefficient				
		$K_1/K_2/K_3$	$C_1/C_2/C_3$	B_1/B_2	F_M	F_{BM}
Turbine	$C_{BM, turbine} = C_{p, turbine} F_{BM, turbine}$	$K_{1,t} = 2.626$				
	$\lg C_{p, turbine} = K_{1,t} + K_{2,t} \lg P_t + K_{3,t} (\lg P_t)^2$	$K_{2,t} = 1.440$	/	/	/	3.5
		$K_{3,t} = -0.178$				
Pump	$C_{BM, pump} = C_{p, pump} F_{BM, pump}$	$K_{1,p} = 3.389$	$C_{1,p} = -0.394$			
	$\lg C_{p, pump} = K_{1,p} + K_{2,p} \lg P_p + K_{3,p} (\lg P_p)^2$	$K_{2,p} = 0.054$	$C_{2,p} = 0.396$	$B_{1,p} = 1.89$	2.32	/
	$F_{BM, pump} = B_{1,p} + B_{2,p} F_{M, pump} F_{P, pump}$	$K_{3,p} = 0.155$	$C_{3,p} = -0.002$	$B_{2,p} = 1.35$		
	$\lg F_{p, pump} = C_{1,p} + C_{2,p} \lg P_p + C_{3,p} (\lg P_p)^2$					
Evaporator	$C_{BM, evaporator} = C_{p, evaporator} F_{BM, evaporator}$	$K_{1,e} = 4.666$		$B_{1,e} = 0.96$		
	$\lg C_{p, evaporator} = K_{1,e} + K_{2,e} \lg A_e + K_{3,e} (\lg A_e)^2$	$K_{2,e} = -0.156$	/	$B_{2,e} = 1.21$	2.45	/
	$F_{BM, evaporator} = B_{1,e} + B_{2,e} F_{M, evaporator}$	$K_{3,e} = 0.155$				
Condenser	$C_{BM, condenser} = C_{p, condenser} F_{BM, condenser}$	$K_{1,c} = 4.666$		$B_{1,c} = 0.96$		
	$\lg C_{p, condenser} = K_{1,c} + K_{2,c} \lg A_c + K_{3,c} (\lg A_c)^2$	$K_{2,c} = -0.156$	/	$B_{2,c} = 1.21$	2.45	/
	$F_{BM, condenser} = B_{1,c} + B_{2,c} F_{M, condenser}$	$K_{3,c} = 0.155$				

The EPC demonstrates the relative scales of capital input and output from the perspectives of per unit power generation cost, which is presented as:

$$EPC = (\text{Cost}_{2019} CRF + f_k \text{Cost}_{2019}) / (P_{net} h_{working-time}) \quad (44)$$

$$CRF = i(1+i)^{time} / ((1+i)^{time} - 1) \quad (45)$$

Where CRF is the capital recovery factor, f_k is operation and maintenance factor which sets as 1.65%, $h_{working-time}$ is the working time of each year which assumes to be 8100h, i is the annual interest which regarded as 5% and $time$ is the life cycle assessment time of 15 years.

The DPP gives a clearly projected investment return time of the ORC system, which is defined as:

$$DPP = -\ln(1 - k \text{Cost}_{2019} / F_{n0}) / \ln(1 + k) \quad (46)$$

$$F_{n0} = E_p (P_{net} h_{working-time}) - f_k \text{Cost}_{2019} \quad (47)$$

Where k implies the depreciated ratio which is 5%, F_{n0} is the system net income and E_p is the electricity sale price which sets as 0.1(\$/kW·h) [30]. Moreover, the net output power (P_{net}) is completely regarded as net electricity generation as result that the power generation efficiency sets as 1.

The SIR figures out the proportion of the predicted profit and initial investment, which is defined as:

$$SIR = B_{time} / C_{time} \quad (48)$$

$$B_{time} = \sum_{j=1}^{time} (P_{net} h_{working-time} E_p (1+r)^j / (1+i)^j) \quad (49)$$

$$C_{time} = \sum_{j=0}^{time} ((f_k \text{Cost}_{2019}) (1+r)^j / (1+i)^j) \quad (50)$$

Where B_{time} and C_{time} are the net value of total income and investment during the period of life cycle assessment time which $j=1...15$, r is the inflation rate which sets as 2.9%.

2.4 Three-level fuzzy decision model

In the paper, the three-level fuzzy decision model is established based on the properties model of working fluids, the thermodynamic model and the techno-economic model as put forward earlier, which are regarded as the first, second and third level respectively. The development and programming of the method is accomplished by the following four steps:

Step (1) - Acquiring the optimal results of decision criteria by choosing appropriate indicator as the objective function according to the realistic operation requirements.

Step (2) - A pair-wise comparison matrix of each decision criterion for schemes is constructed so as to rank in sequence and assign the semantic score. After the normalization of semantic score, the weighting set of each criterion could be obtained.

Step (3) - Similar to step two, a pair-wise comparison matrix of each decision criterion for three classified levels is built, the weighting set calculation is subject to the relative importance of decision criteria within each level.

425 Step (4) - After acknowledging the weighting set of each criterion, the
426 weighting matrix for schemes (R_i) and levels (W_i) can be developed. And the
427 evaluation set (B_i) can be calculated by the following equation:

$$428 \quad B_i = W_i \times R_i \quad (51)$$

429 For the second level, evaluation result of the first level should be inserted into
430 the R_i as the last row. The original W_i of second level needs to multiply
431 $n/(n+1)$ if n decision criteria are included. Next, a new W_i has to be formed
432 by assigning $1/(n+1)$ in the final position of the former one. For the third level, the
433 same procedure is undergoing repeatedly to gain B_i .

434 Summarizing the three mathematical models above, Fig. 3 gives a clear flow
435 chart of the construction procedures.

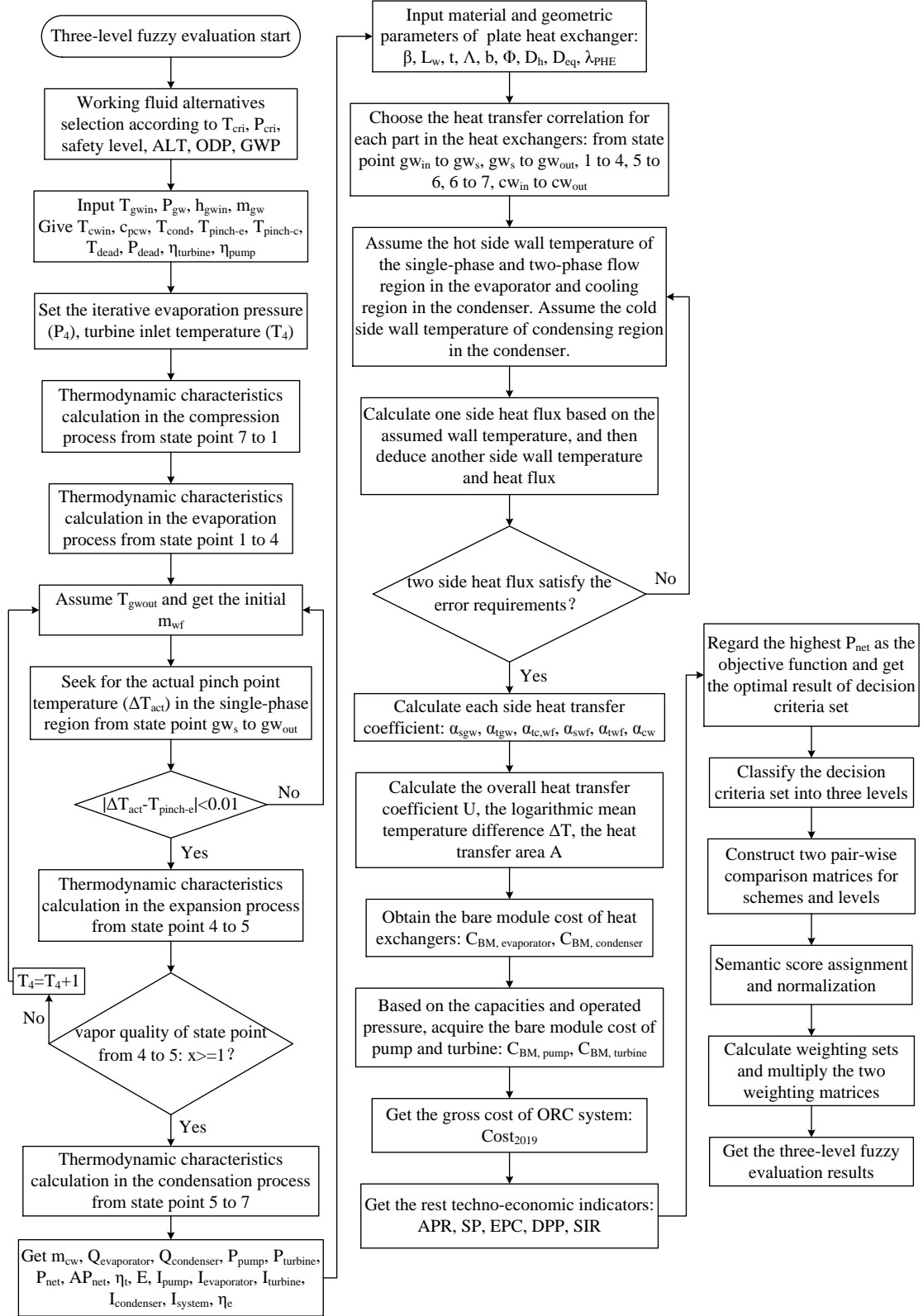


Fig. 3. The three-level fuzzy evaluation procedures

3.1 Thermodynamic performance

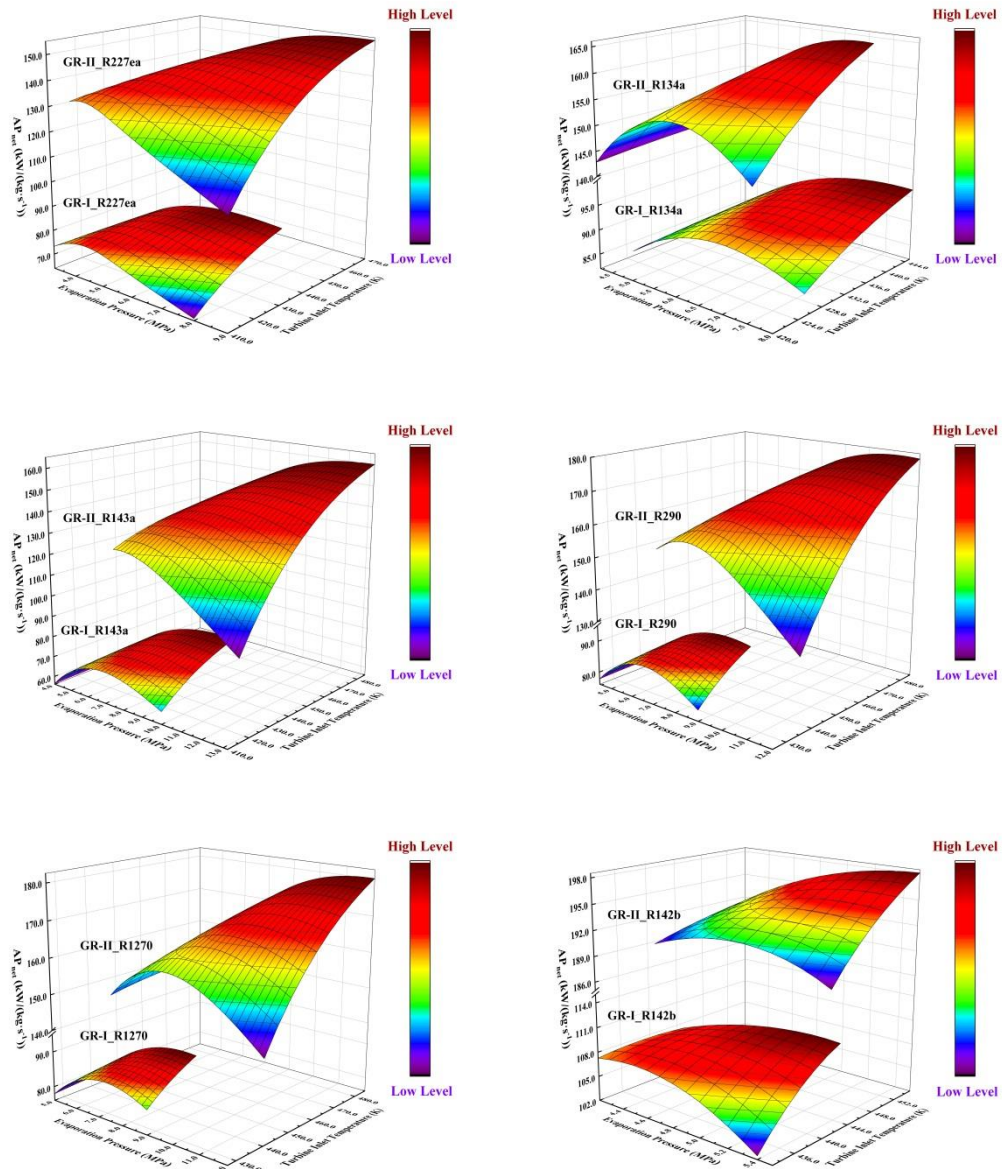


Fig. 4. Specific net output power (AP_{net}) variation in two geothermal reservoirs

438 In this study, the specific net output power (AP_{net}), thermal efficiency (η_t) and
439 exergy efficiency (η_e) are determined to estimate the thermodynamic performance
440 of the TORC system designed for both geothermal reservoirs (GR-I and GR-II). As
441 shown in Figs. 4, 5 and 6, the overall variation of the three indexes shows both
442 similarities and diversities with increasing evaporation pressure (P_4) and turbine
443 inlet temperature (T_4) for each working fluid in two different geothermal reservoirs.
444 Moreover, Fig. 4 indicates AP_{net} of the six selected working fluids in GR-II which
445 ranges from 93.73-198.14kW/(kg·s⁻¹) is apparently higher than that of GR-I which is
446 from 56.46-110.94kW/(kg·s⁻¹), indicting a higher power capacity of GR-II. Besides,
447 Fig. 4 demonstrates AP_{net} increases firstly and then decreases when raising P_4
448 under given T_4 . It is because turbine output shaft power ($P_{turbine}$) enhances
449 obviously while P_4 increases from lower values (but still exceed the critical
450 pressure of the working fluid). And the consumed power of pump (P_{pump}) increases
451 more rapidly than $P_{turbine}$ with further increase of P_4 , which results that the upward
452 trend of AP_{net} gradually slows down until it starts deceasing. In addition, due to the
453 limits of pinch point temperature difference ($T_{pinch-e}$) and decomposition
454 temperature (T_{de}) of working fluids, AP_{net} keeps increasing while T_4 grows up to
455 reach the maximal value under higher P_4 . Furthermore, AP_{net} shows upward
456 tendency firstly and then goes downward when given a lower P_4 . Comparing the
457 optimal results of working fluids in GR-I, R142b is able to acquire the largest AP_{net}
458 of 110.94kW/(kg·s⁻¹) at the condition that the P_4 is 5.2MPa and T_4 is 445K. On
459 the contrary, R143a obtains smallest AP_{net} of 81.77kW/(kg·s⁻¹) in the case of the

460 P_4 is 9.4MPa and T_4 is 445K. With regard to GR-II, R142b maintains the highest
 461 AP_{net} as well, which is 198.14kW/(kg·s⁻¹) when the P_4 is 5.5MPa and T_4 is
 462 455K. And R227ea yields lowest AP_{net} of 154.02kW/(kg·s⁻¹), for the P_4 is
 463 8.6MPa and T_4 is 470K.

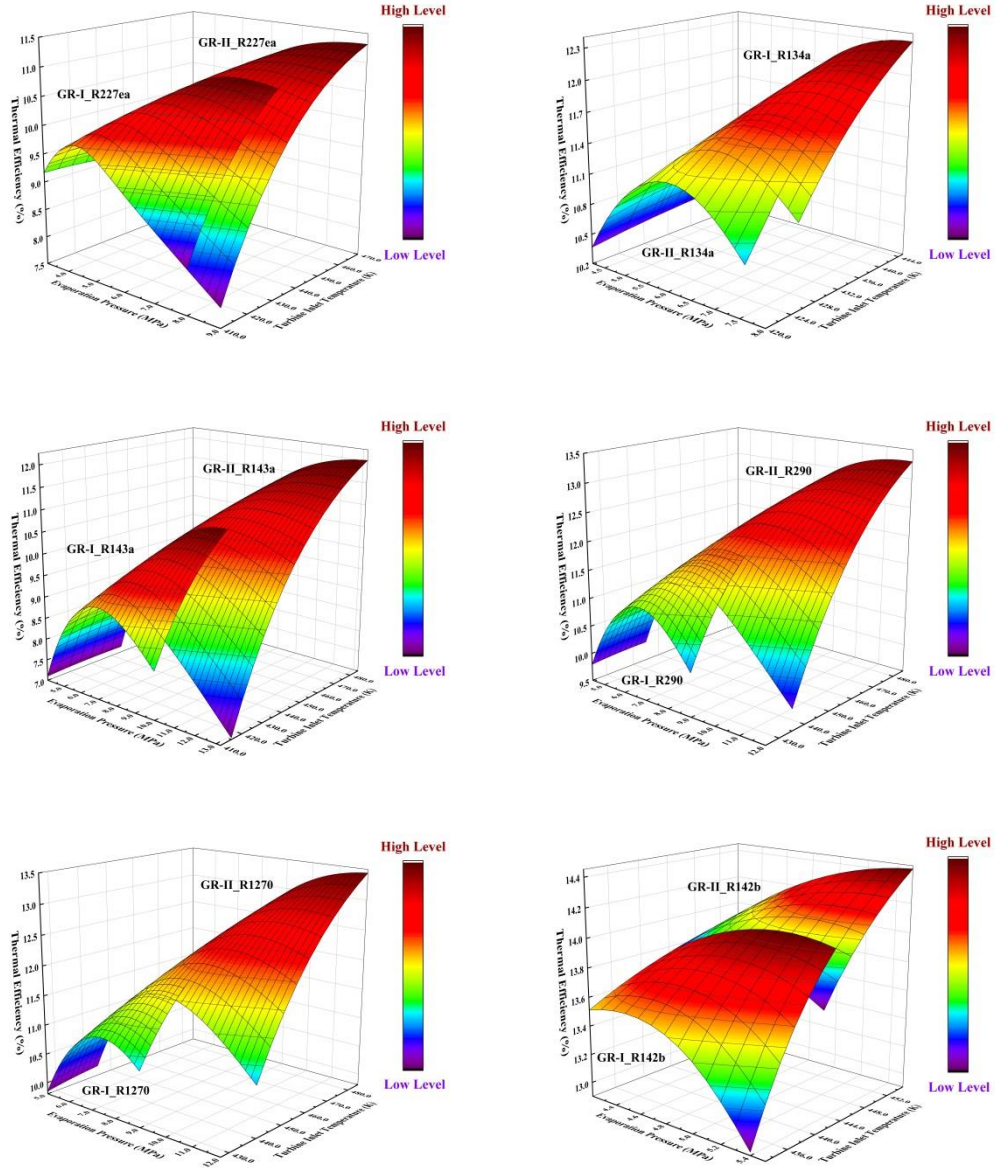


Fig. 5. Thermal efficiency (η_t) variation in two geothermal reservoirs

Thermal efficiency (η_t) is defined as the ratio of net power output (P_{net}) to the amount of heat absorbed during the evaporation process, as shown in Eq. (7). The change of η_t by varying evaporation pressure (P_4) and turbine inlet temperature (T_4) is illustrated in Fig. 5. As far as the η_t of each working fluid is concerned, there exists regions that are partially overlapped between GR-I and GR-II, which ranges from 7.10-14.05% and 7.04-14.43%, indicating that even though geothermal reservoirs have different power capacities, they could have similar energy conversion efficiency ranges applying TORC. Specifically, it is observed that η_t of all selected working fluids can be described as increasing and dropping later with an increase of P_4 under investigated T_4 . The alteration of η_t is similar with AP_{net} . For this reason, the η_t rises faster at lower P_4 and stabilizes till it decreases as P_4 increases further. Additionally, with the restrictions of $T_{pinch-e}$ and T_{de} , η_t represents an inclination of rising up continuously with increasing T_4 to the maximum under higher P_4 . The reason can be explained from that, although the enthalpy difference ($h_4 - h_5$) becomes larger and the mass flow rate of working fluids (m_{wf}) is declining in the course of expansion, the turbine output shaft power ($P_{turbine}$) still increases and the pump power consumption (P_{pump}) decreases as T_4 continues increasing. In the meanwhile, when the system operates at a lower P_4 , η_t behaves in a trend of increasing first and then diminishes as T_4 grows up. The maximum results of η_t for working fluids in GR-I and GR-II are both R142b which are 14.05% and 14.43% respectively, for the P_4 and T_4 are 5.1MPa, 445K and 5.5MPa, 455K. To the opposite, R143a and R227ea have the minimal η_t in GR-I and GR-II with

486 the values of 10.66% and 11.32%.

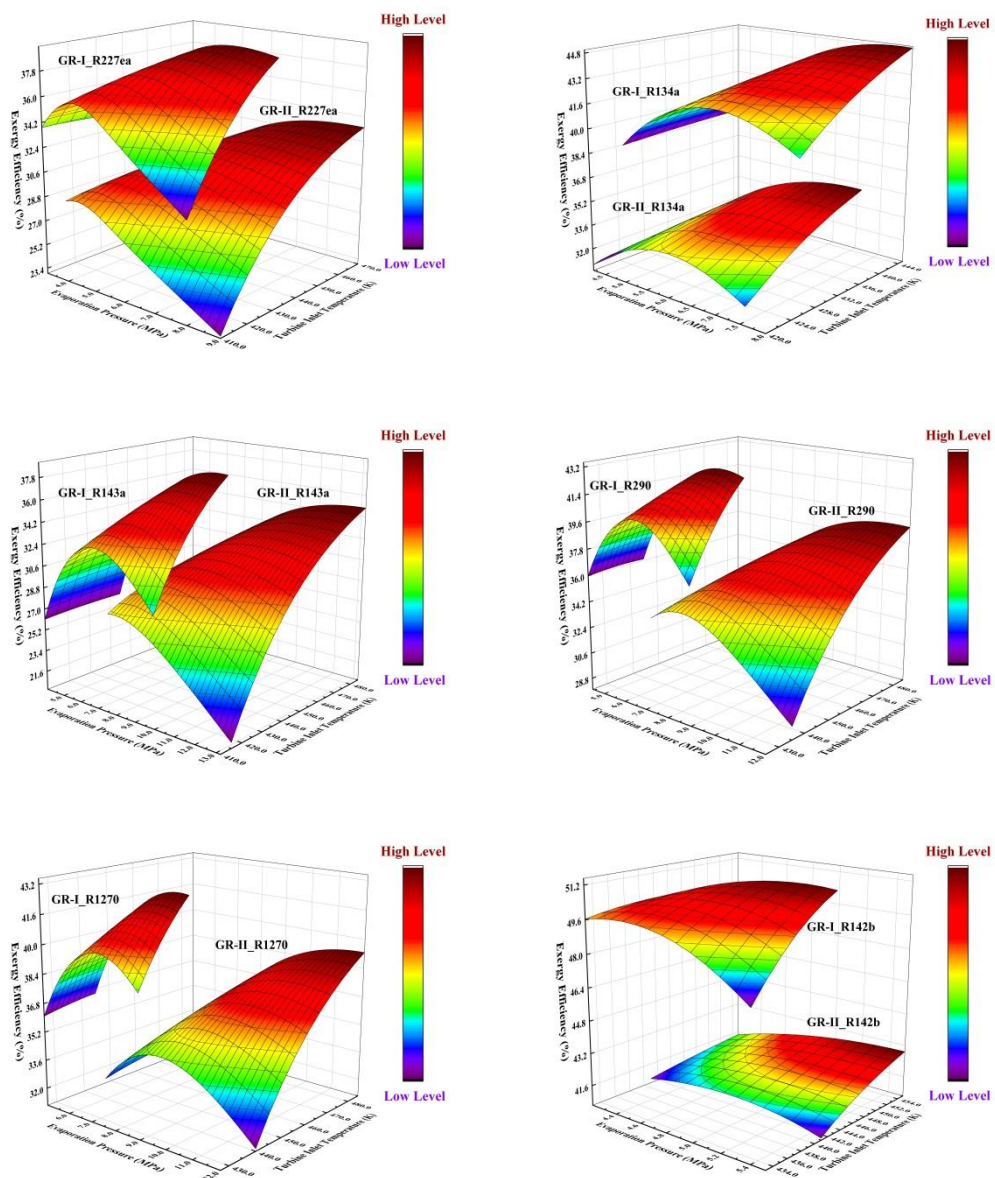


Fig. 6. Exergy efficiency (η_e) variation in two geothermal reservoirs

487 Exergy signifies the greatest beneficial output power that geothermal system
488 possesses. The exergy efficiency (η_e) is employed for assessing the exergy
489 utilization, which is characterized as the ratio of net output power (P_{net}) to the net
490 exergy flows into the system (E_{in}^{gw}), as given in Eq. (16). Typically, it can be noticed
491 from Fig. 6 that the η_e in GR-I is normally higher than GR-II. The ranges are
492 26.11-51.42% for GR-I and 23.14-42.89% for GR-II, which indicates that although
493 GR-I has smaller power capacity, the exergy is fully utilized compared to GR-II.
494 Particularly, Fig. 6 denotes that the arc-surface changing trend of η_e is familiar
495 with that of AP_{net} and η_t . Increasing of η_e is owing to the thermal matching
496 performance becomes better between heat sources and working fluids and the exergy
497 loss (I_{system}) reduces constantly with an increment of lower evaporation pressure
498 (P_4). Instead, the reduction of P_{net} is more markedly than the I_{system} decreases
499 with further increase of P_4 , leading to the downward tendency for η_e . What's more,
500 the η_e shows a trend of growing up for that P_{net} keeps increasing while I_{system}
501 turns into dropping by improving turbine inlet temperature (T_4) under investigated
502 P_4 . According to optimal results of the working fluids, R142b achieves the biggest
503 η_e of 51.42% and 42.90% in the GR-I and GR-II, with the P_4 and T_4 are 5.2MPa,
504 445K and 5.5MPa, 455K. And R143a and R227ea get lowest exergy efficiency of
505 38.30% and 33.42% for the two geothermal reservoirs.

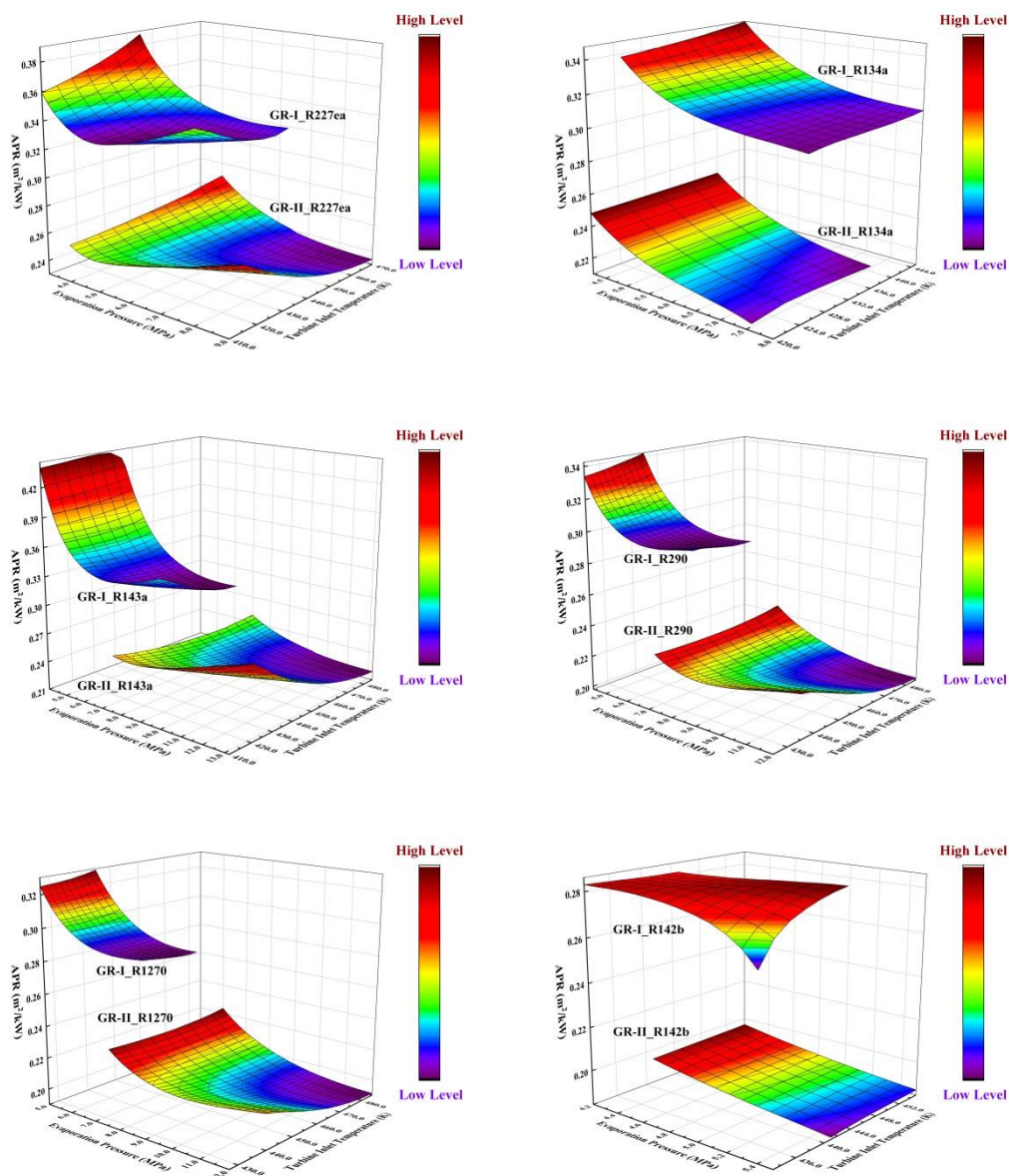


Fig. 7. Heat transfer area per net output power (APR) variation in two geothermal reservoirs

Utilizing the techno-economic evaluation model established previously, the heat transfer area per net output power (APR) and electricity production cost (EPC) are adopted for detailed illustration of the techno-economic properties of TORC system. First of all, as depicted in Figs. 7 and 8, the map alteration of two indexes for each working fluid (except R142b) expresses consistent changing trend under the influence of evaporation pressure (P_4) and turbine inlet temperature (T_4) in the both two geothermal reservoirs. The APR and EPC values in GR-I is commonly above those of GR-II. As for GR-I and GR-II, APR ranges from 0.262-0.444(m²/kW) and 0.185-0.290(m²/kW). EPC ranges from 0.030-0.054(\$/(kW·h)) and 0.022-0.055(\$/(kW·h)), indicating that GR-II is more profitable in the techno-economic perspective. Furthermore, APR implies the compactness of heat exchangers structure which refers to the ratio of heat transfer areas of all heat exchangers to net output power. For the purpose of cutting down the overall cost of the whole system, it's better to achieve the APR as low as possible. Then, it can be seen from Fig. 7 that APR of R227ea, R143a, R290 and R1270 decreases initially before increasing in both two geothermal reservoirs when increasing P_4 under given T_4 . Since the net output power (P_{net}) first increases and then decreases for the four working fluids with which trend of variation is more dramatically than the heat transfer areas change. Regarding the APR of R134a and R142b, it's decreasing yet with an increment of P_4 under given T_4 . The difference of R134a and R142b from other four alternatives accounts for the downward trend of heat transfer areas varies more significantly than that of P_{net} . Moreover, the region of minimum APR for the

529 working fluids (expect R142b in GR-I) begins to appear when further increasing P_4
530 and T_4 simultaneously. Summarily, concluding from the optimal results under the
531 operated conditions. R142b acquires the lowest APR of 0.262(m²/kW) and
532 0.185(m²/kW) in GR-I and GR-II, for 5.4MPa, 433K and 5.5MPa, 441K of the P_4
533 and T_4 . Additionally, R227ea obtains higher APR of 0.331(m²/kW) and
534 0.234(m²/kW) respectively, for 5.8MPa, 425K and 9.0MPa, 470K.

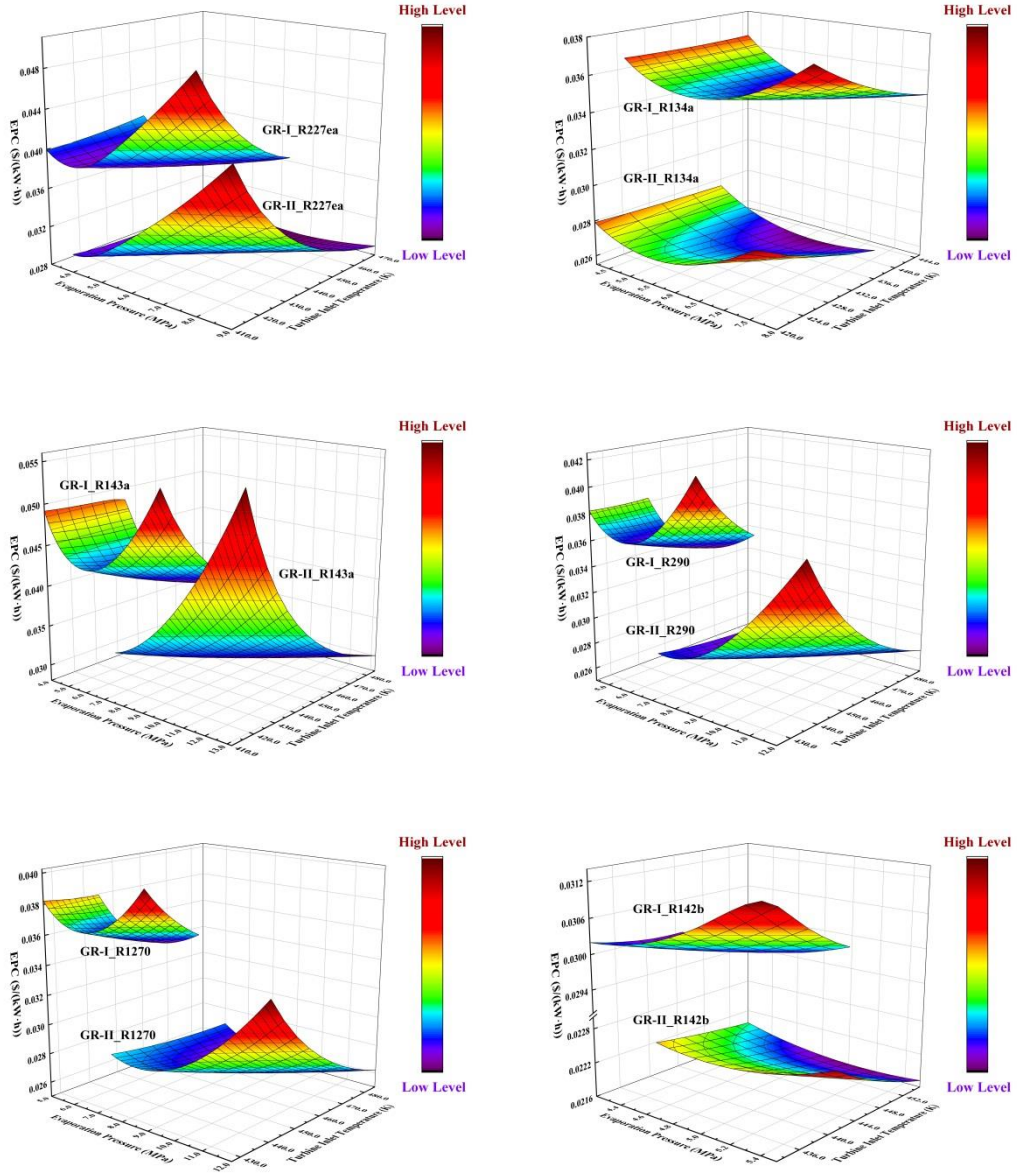


Fig. 8. Electricity production cost (EPC) variation in two geothermal reservoirs

535 EPC is directly proportional to the gross cost (Cost_{2019}) and inversely to the net
536 output power (P_{net}) and the whole working time ($h_{working-time}$) of the TORC system.
537 Hence, in the case of a certain $h_{working-time}$ with increasing the evaporation pressure
538 (P_4) under given turbine inlet temperature (T_4), Fig. 8 shows that EPC exhibits a
539 trend of decrease initially and increase afterwards for the reason that P_{net} increases
540 first and then decreases, meanwhile, the pressure tolerance of components is
541 required to enhance which leads to an inevitable increase in Cost_{2019} . Similarly, the
542 EPC decreases firstly and then increases when increasing T_4 under lower P_4 . The
543 explanation for this variation is similar with ranging P_4 but the discrepancy exists
544 that overall heat transfer areas keep increasing which draws an increase in Cost_{2019} .
545 When considering the limits of the maximal T_4 under higher P_4 , the upward
546 tendency of EPC would not appear anymore. By comparing the optimal results
547 between working fluids, the lowest EPC appears at R142b of 0.030(\$/(kW·h)) and
548 0.022(\$/(kW·h)) when the P_4 and T_4 are 4.6MPa, 445K and 5.1MPa, 455K in
549 GR-I and GR-II. Moreover, R143a gets higher EPC of 0.040(\$/(kW·h)) and
550 0.0285(\$/(kW·h)) for 7.6MPa, 445K and 9.4MPa, 485K of P_4 and T_4 .

3.3 Three-level fuzzy evaluation

As illustrated in maps of thermodynamic and techno-economic parameters above, the iteration outcomes can be exported by varying the tested evaporation pressure (P_4) and turbine inlet temperature (T_4) for each working fluid alternative. In the meantime, the case study regards the maximal P_{net} as objective function to obtain the optimal results for GR-I and GR-II. As listed in Tables 5 and 6, the values of the rest indexes such as η_t or APR are acknowledged under the same values of P_4 and T_4 when P_{net} gets the maximum. In this paper, the available options of scheme included R227ea (D1), R134a (D2), R143a (D3), R290 (D4), R1270 (D5) and R142b (D6). The decision criteria set is comprised of Safety Level (C1), ALT (C2), ODP (C3), GWP (C4), P_{net} (C5), η_t (C6), η_e (C7), APR (C8), SP (C9), $Cost_{2019}$ (C10), EPC (C11), DPP (C12) and SIR (C13).

563 Judging by the rules of criteria for higher-the-better such as C5, C6, C7 and
564 C12 or lower-the-better involving C1, C2, C3, C4, C8, C9, C10, C11 and C13, a
565 pair-wise comparison matrix of the P_{net} (C5) for schemes in GR-I is constructed for
566 instance. As depicted in Table 7, it can be seen that the values on diagonal line are
567 all 0.5 in the matrix on account of the P_{net} of each scheme is identical to itself.
568 When it comes to comparing the P_{net} of D1 to D2, the result is 0, because of the
569 value of P_{net} in D1 is lower than D2. Conversely, 1 is appeared when comparing
570 D2 with D1 for the P_{net} of D2 is higher than D1. The sum of each row is got after
571 the consistence checking between all the schemes. Arranging the sum of schemes in
572 a descending order, those are D6, D2, D4, D5, D1 and D3. Furthermore, since the
573 ranking is based on an interval of 0.5, D6 acquires the highest of 5.5 at the first
574 position and the semantic score is assigned 1. D2 obtains 4.5 and scored 0.818 in the
575 third place. The weighting is calculated by means of the semantic score for each
576 scheme dividing the sum semantic scores for all schemes in the normalization
577 process. Then, the weighting set for other twelve criteria are derived from the same
578 procedures. Tables 8 and 9 list the results of weighting matrix for all schemes (R_i)
579 after normalization in GR-I and GR-II.

Table 5 Simulated optimal results of GR-I

Working Fluid	P_4 /MPa	T_4 /K	P_{net} /kW	η_t /%	η_e /%	APR(m ² /kW)	SP/m	Cost ₂₀₁₉ (10 ⁵ \$)	EPC(\$/(kW·h))	DPP/Year	SIR	Scheme
R227ea	6.6	445	1158.13	10.78	39.40	0.338	0.068	31.84	0.038	4.062	3.115	D1
R134a	7.6	445	1318.65	12.31	44.91	0.308	0.064	32.59	0.034	3.589	3.466	D2
R143a	9.4	445	1115.41	10.64	38.29	0.325	0.052	32.69	0.041	4.380	2.923	D3
R290	7.6	445	1265.92	11.93	43.25	0.298	0.070	32.62	0.036	3.766	3.324	D4
R1270	8.6	445	1256.59	11.90	43.00	0.291	0.064	32.58	0.036	3.794	3.303	D5
R142b	5.2	445	1513.27	14.04	51.42	0.285	0.087	32.74	0.030	3.084	3.959	D6

Table 6 Simulated optimal results of GR-II

Working Fluid	P_4 /MPa	T_4 /K	P_{net} /kW	η_t /%	η_e /%	APR(m ² /kW)	SP/m	Cost ₂₀₁₉ (10 ⁵ \$)	EPC(\$/(kW·h))	DPP/Year	SIR	Scheme
R227ea	8.6	470	1694.22	11.31	33.42	0.234	0.067	34.94	0.029	2.923	4.153	D1
R134a	7.4	440	1821.87	12.12	35.90	0.214	0.064	34.08	0.026	2.621	4.578	D2
R143a	13	485	1760.56	12.01	34.96	0.219	0.051	37.82	0.030	3.060	3.988	D3
R290	11.2	485	1966.04	13.28	38.92	0.199	0.068	36.98	0.026	2.637	4.554	D4
R1270	11.8	485	1981.99	13.43	39.28	0.191	0.063	37.14	0.026	2.626	4.571	D5
R142b	5.5	455	2179.54	14.43	42.89	0.187	0.087	33.98	0.022	2.146	5.494	D6

Table 7 Consistence checking, semantic score assignment and weighting calculation of net output power (P_{net}) for scheme

C5	D1	D2	D3	D4	D5	D6	Sum	Score	Weighting
D1	0.5	0	1	0	0	0	1.5	0.429	0.1133
D2	1	0.5	1	1	1	0	4.5	0.818	0.2161
D3	0	0	0.5	0	0	0	0.5	0.333	0.088
D4	1	0	1	0.5	1	0	3.5	0.667	0.1762
D5	1	0	1	0	0.5	0	2.5	0.538	0.1422
D6	1	1	1	1	1	0.5	5.5	1	0.2642

Table 8 Weighting of decision criteria for each scheme after normalization of semantic score in GR-I

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13
D1	0.2383	0.1133	0.1806	0.1133	0.1133	0.1133	0.1133	0.088	0.1422	0.2642	0.1133	0.1133	0.1133
D2	0.2383	0.1762	0.1806	0.1762	0.2161	0.2161	0.2161	0.1422	0.2161	0.1762	0.2161	0.2161	0.2161
D3	0.1429	0.088	0.1806	0.088	0.088	0.088	0.088	0.1133	0.2642	0.1133	0.088	0.088	0.088
D4	0.1022	0.2161	0.1806	0.2161	0.1762	0.1762	0.1762	0.1762	0.1133	0.1422	0.1762	0.1762	0.1762
D5	0.1022	0.2642	0.1806	0.2642	0.1422	0.1422	0.1422	0.2161	0.1762	0.2161	0.1422	0.1422	0.1422
D6	0.1761	0.1422	0.097	0.1422	0.2642	0.2642	0.2642	0.2642	0.088	0.088	0.2642	0.2642	0.2642

Table 9 Weighting of decision criteria for each scheme after normalization of semantic score in GR-II

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13
D1	0.2383	0.1133	0.1806	0.1133	0.088	0.088	0.088	0.088	0.1422	0.1762	0.1133	0.1133	0.1133
D2	0.2383	0.1762	0.1806	0.1762	0.1422	0.1422	0.1422	0.1422	0.1762	0.2161	0.2161	0.2161	0.2161
D3	0.1429	0.088	0.1806	0.088	0.1133	0.1133	0.1133	0.1133	0.2642	0.088	0.088	0.088	0.088
D4	0.1022	0.2161	0.1806	0.2161	0.1762	0.1762	0.1762	0.1762	0.1133	0.1422	0.1422	0.1422	0.1422
D5	0.1022	0.2642	0.1806	0.2642	0.2161	0.2161	0.2161	0.2161	0.2161	0.1133	0.1762	0.1762	0.1762
D6	0.1761	0.1422	0.097	0.1422	0.2642	0.2642	0.2642	0.2642	0.088	0.2642	0.2642	0.2642	0.2642

580 According to the property diversities of the thirteen decision criteria, they can
581 be divided into three levels. The first level considers safety and environmental
582 friendly properties which contains C1~C4. The second level concerns with
583 thermodynamic qualities including C5~C7. As for the third level, it is made up of
584 C8~C13 with concentrating on techno-economic characteristics. Differential from
585 the semantic score assignment and weighting calculation of criteria in pair-wise
586 matrix established for schemes as shown in Table 7, Table 10 summarizes the
587 pair-wise matrix built for the three levels in GR-I and GR-II, in which the criteria
588 are compared within the same hierarchy. E.g., ranking the relative importance
589 among criteria in the first level, that is C3, C4, C2, and C1. Namely, when
590 comparing C1 with C2, the result is 0 because of C1 is less significant than C2. After
591 the consistency checking of C1~C4 in the first level and arranging the sum of each
592 criterion in descending order, in which the ranking is identical to the importance
593 sequence. Moreover, it is because that the ranking is based on an interval of 1.0, thus,
594 C3 ranks first for getting 3.5 and assigned the semantic score of 1. C4 ranks second
595 and scored 0.919 due to a sum of 2.5. For the criteria in levels two and three, the
596 relative importance rankings are C7, C6, C5 and C11, C13, C12, C10, C8, C9
597 respectively. Similarly, the semantic score assignment and weighting calculation are
598 performed the same as the first level demonstrated earlier.

Table 10 Consistence checking, semantic score assignment and weighting calculation of decision criteria for three levels

	C1	C2	C3	C4	C5	C6	C7	C8	C9	C10	C11	C12	C13	Sum	Score	Weighting
C1	0.5	0	0	0										0.5	0.739	0.2135
C2	1	0.5	0	0										1.5	0.818	0.2363
C3	1	1	0.5	1										3.5	1	0.2888
C4	1	1	0	0.5										2.5	0.905	0.2614
C5					0.5	0	0							0.5	0.818	0.3004
C6					1	0.5	0							1.5	0.905	0.3324
C7					1	1	0.5							2.5	1	0.3672
C8								0.5	1	0	0	0	0	1.5	0.667	0.141
C9								0	0.5	0	0	0	0	0.5	0.6	0.1269
C10								1	1	0.5	0	0	0	2.5	0.739	0.1563
C11								1	1	1	0.5	1	1	5.5	1	0.2114
C12								1	1	1	0	0.5	0	3.5	0.818	0.173
C13								1	1	1	0	1	0.5	4.5	0.905	0.1914

599 Referring to the last step of three-level fuzzy decision method, the final
600 evaluation results can be acquired by multiplying the weighting matrix of criteria for
601 three levels (\mathbf{W}_i) and the weighting matrix for schemes (\mathbf{R}_i). What accounts more is
602 that the first level result should be inserted as last row in \mathbf{R}_i of the second level.
603 Furthermore, \mathbf{W}_i for second level is multiplying 3/4 as well. And then the
604 equivalent weight needs to be assigned as 1/4 and added in the fourth position of
605 \mathbf{W}_i in order to keep the weighting matrix dimension consistency. Repeatedly, the
606 result for the third level can be obtained by substituting 3/4 and 1/4 with 6/7 and 1/7.

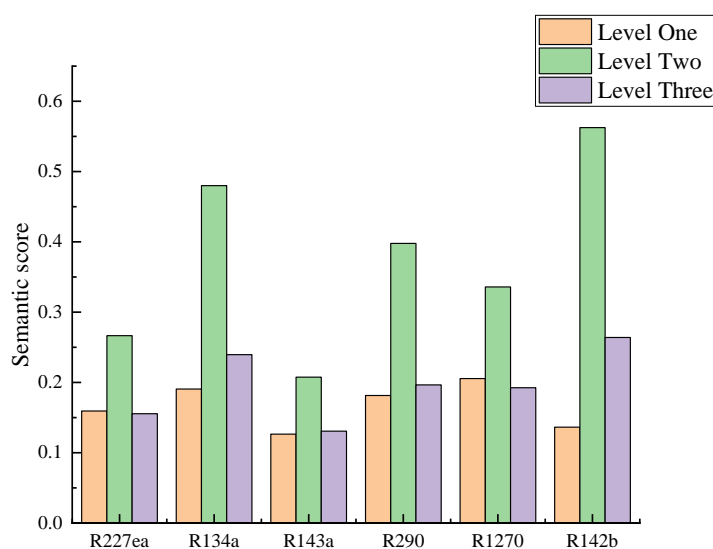


Fig. 9. Results of three-level fuzzy evaluation for GR-I

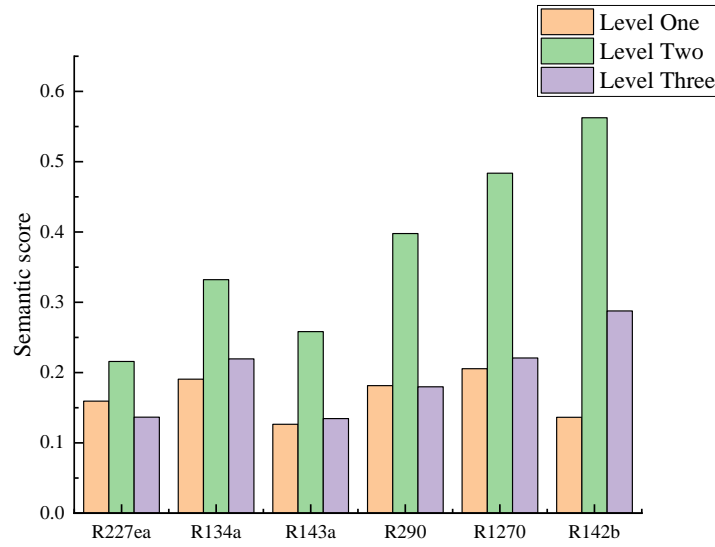


Fig. 10. Results of three-level fuzzy evaluation for GR-II

Figs. 9 and 10 exhibit the comparisons of the three-level evaluation results for GR-I and GR-II. It is concluded that the first level evaluation result are equally in the two geothermal reservoirs. R1270 possess the best reliability when only concerns about safety and environmental friendly properties. The second and third level evaluation results show that R142b is the optimal one which behaves excellent thermodynamic and techno-economic performance among selected working fluids. To the opposite, R143a is not much appropriate for the geothermal operation process according to the three-level evaluation results.

What's more, it is noteworthy that the third level evaluation result for GR-I in Fig.9 is consistent with the optimal ranking result of P_{net} in Table 5. However, comparing the result in Fig.10 and Table 6, which exerts difference between the evaluation and optimal raking order with respect to GR-II. It is implied that the impact of techno-economic indexes on the overall system performance is more apparent at high temperatures.

4 Conclusions

Based on the constructed environmental, thermodynamic and techno-economic assessment models, this paper develops a three-level fuzzy decision method for TORC system used in medium and high temperature geothermal reservoirs. The optimal results of the geothermal TORC system are obtained when P_{net} reaches the maximum. The evaluation results are gained by semantic score assignment, weighting calculation and order ranking. Both of results contribute to the following conclusions:

1. According to the first level evaluation result, the ranking of the working fluid is R1270, R134a, R290, R227ea, R142b and R143a which is identical to both GR-I and GR-II.

2. The second level takes into account the first level result and thermodynamic characteristics, ranking like R142b, R134a, R290, R1270, R227ea, R143a for GR-I and R142b, R1270, R290, R134a, R143a, R227ea for GR-II. It is concluded that R142b is both the most suitable working fluid for its maximal net output power. By contrast of the second level evaluation results for R134a in the two geothermal reservoirs, the heat source with lower temperature and pressure in GR-I is more compatible with it.

3. In terms of the third level, it takes the former two levels results and techno-economic properties into consideration. The evaluation ranking is R142b, R134a, R290, R1270, R227ea and R143a for GR-I. For GR-II ranks R142b, R1270, R134a, R290, R227ea and R143a. From the comprehensive standpoint of the three-level evaluation results, R142b is recommended as best one for the geothermal TORC systems.

The three-level fuzzy decision method developed in this work can effectively figure out the influence of a former level decision criteria on the latter one. The designers can decide on strategies and solutions according to practical requirements by adjusting weighting on indexes. It also helps the investors make whole-scale judgements in the pre-design stage of geothermal ORC system. As for the future work employed with this methodology, it can be extended to analyze the optimization process and make reliable design decisions for different ORC layout.

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Reference

- [1] Anderson A, Rezaie B. Geothermal technology: Trends and potential role in a sustainable future. *Appl Energy* 2019; 248:18-34.
<https://doi.org/10.1016/j.apenergy.2019.04.102>.
- [2] Statistical review of world energy,
<https://www.bp.com/en/global/corporate/energy-economics/statistical-review-of-world-energy.html>; 2020.
- [3] Limberger J, Boxem T, Pluymaekers M et al. Geothermal energy in deep aquifers: A global assessment of the resource base for direct heat utilization. *Renew Sustain Energy Rev* 2018; 82:961-975.
<https://doi.org/10.1016/j.rser.2017.09.084>.
- [4] Moloney F, Almatrafi E, Goswami DY. Working fluid parametric analysis for recuperative supercritical organic Rankine cycles for medium geothermal reservoir temperatures. *Renew Energy* 2020; 147:2874-2881.
<https://doi.org/10.1016/j.renene.2018.09.003>.
- [5] Liang Y, Sun Z, Dong M et al. Investigation of a refrigeration system based on combined supercritical CO₂ power and transcritical CO₂ refrigeration cycles by waste heat recovery of engine. *Int J Refrig* 2020; 118:470-482.
<https://doi.org/10.1016/j.ijrefrig.2020.04.031>.
- [6] Li XY, Shu GQ, Tian H. Integrating off-design performance in designing CO₂ power cycle systems for engine waste heat recovery. *Energy Conver Manage* 2019; 201:112146. <https://doi.org/10.1016/j.enconman.2019.112146>.
- [7] Song J, Gu CW, Ren XD. Parametric design and off-design analysis of organic Rankine cycle (ORC) system. *Energy Conver Manage* 2016; 112:157-165.
<https://doi.org/10.1016/j.enconman.2015.12.085>.

-
- [8] Wang X, Shu GQ, Tian H et al. Effect factors of part-load performance for various Organic Rankine cycles using in engine waste heat recovery. *Energy Conver Manage* 2018; 174:504-515.
<https://doi.org/10.1016/j.enconman.2018.08.024>.
- [9] Madhawa Hettiarachchi HD, Golubovic M, Worek WM, Ikegami Y. Optimum design criteria for an Organic Rankine cycle using low-temperature geothermal heat sources. *Energy* 2007; 32:1698-1706.
<https://doi.org/10.1016/j.energy.2007.01.005>.
- [10] Astolfi M, Romano MC, Bombarda P, Macchi E. Binary ORC (organic Rankine cycles) power plants for the exploitation of medium–low temperature geothermal sources – Part A: Thermodynamic optimization. *Energy* 2014; 66:423-434. <https://doi.org/10.1016/j.energy.2013.11.056>.
- [11] Astolfi M, Romano MC, Bombarda P, Macchi E. Binary ORC (Organic Rankine Cycles) power plants for the exploitation of medium–low temperature geothermal sources – Part B: Techno-economic optimization. *Energy* 2014; 66:435-446. <https://doi.org/10.1016/j.energy.2013.11.057>.
- [12] Vetter C, Wiemer HJ, Kuhn D. Comparison of sub- and supercritical Organic Rankine Cycles for power generation from low-temperature/low-enthalpy geothermal wells, considering specific net power output and efficiency. *Appl Therm Eng* 2013; 51:871-879.
<https://doi.org/10.1016/j.applthermaleng.2012.10.042>.
- [13] Sun J, Liu Q, Duan Y. Effects of evaporator pinch point temperature difference on thermo-economic performance of geothermal organic Rankine cycle systems. *Geothermics* 2018; 75:249-258.
<https://doi.org/https://doi.org/10.1016/j.geothermics.2018.06.001>.
- [14] Meng D, Liu Q, Ji Z. Performance analyses of regenerative organic flash cycles for geothermal power generation. *Energy Conver Manage* 2020; 224:113396. <https://doi.org/https://doi.org/10.1016/j.enconman.2020.113396>.

-
- [15] Cakici DM, Erdogan A, Colpan CO. Thermodynamic performance assessment of an integrated geothermal powered supercritical regenerative organic Rankine cycle and parabolic trough solar collectors. *Energy* 2017; 120:306-319. <https://doi.org/10.1016/j.energy.2016.11.083>.
- [16] Wang XC, Levy EK, Pan CJ et al. Working fluid selection for organic Rankine cycle power generation using hot produced supercritical CO₂ from a geothermal reservoir. *Appl Therm Eng* 2019; 149:1287-1304. <https://doi.org/10.1016/j.applthermaleng.2018.12.112>.
- [17] Heberle F, Schifflechner C, Bruggemann D. Life cycle assessment of Organic Rankine Cycles for geothermal power generation considering low-GWP working fluids. *Geothermics* 2016; 64:392-400. <https://doi.org/10.1016/j.geothermics.2016.06.010>.
- [18] Jankowski M, Borsukiewicz A, Wisniewski S, Hooman K. Multi-objective analysis of an influence of a geothermal water salinity on optimal operating parameters in low-temperature ORC power plant. *Energy* 2020; 202. <https://doi.org/10.1016/j.energy.2020.117666>.
- [19] Mohammadzadeh Bina S, Jalilinasrabady S, Fujii H. Thermo-economic evaluation of various bottoming ORCs for geothermal power plant, determination of optimum cycle for Sabalan power plant exhaust. *Geothermics* 2017; 70:181-191. <https://doi.org/10.1016/j.geothermics.2017.06.007>.
- [20] Wang JS, Diao MZ, Yue KH. Optimization on pinch point temperature difference of ORC system based on AHP-Entropy method. *Energy* 2017; 141:97-107. <https://doi.org/10.1016/j.energy.2017.09.052>.
- [21] Zhou GY, Wu E, Tu ST. Optimum selection of compact heat exchangers using non-structural fuzzy decision method. *Appl Energy* 2014; 113:1801-1809. <https://doi.org/10.1016/j.apenergy.2013.07.041>.

-
- [22] Manente G, Da Lio L, Lazzaretto A. Influence of axial turbine efficiency maps on the performance of subcritical and supercritical Organic Rankine Cycle systems. *Energy* 2016; 107:761-772.
<https://doi.org/10.1016/j.energy.2016.04.063>.
- [23] Martin H. A theoretical approach to predict the performance of chevron-type plate heat exchangers. *Chem Eng Process* 1996; 35:301-310.
[https://doi.org/10.1016/0255-2701\(95\)04129-x](https://doi.org/10.1016/0255-2701(95)04129-x).
- [24] Wang Z-Z, Zhao Z-N. Analysis of Performance of Steam Condensation Heat Transfer and Pressure Drop in Plate Condensers. *Heat Transfer Eng* 1993; 14:32-41. <https://doi.org/10.1080/01457639308939809>.
- [25] Pioro IL, Khartabil HF, Duffey RB. Heat transfer to supercritical fluids flowing in channels—empirical correlations (survey). *Nucl Eng Des* 2004; 230:69-91. <https://doi.org/10.1016/j.nucengdes.2003.10.010>.
- [26] Imran M, Usman M, Park BS, Yang Y. Comparative assessment of Organic Rankine Cycle integration for low temperature geothermal heat source applications. *Energy* 2016; 102:473-490.
<https://doi.org/10.1016/j.energy.2016.02.119>.
- [27] Kuo WS, Lie YM, Hsieh YY, Lin TF. Condensation heat transfer and pressure drop of refrigerant R-410A flow in a vertical plate heat exchanger. *Int J Heat Mass Transf* 2005; 48:5205-5220.
<https://doi.org/10.1016/j.ijheatmasstransfer.2005.07.023>.
- [28] Turton R, Shaeiwitz JA, Bhattacharyya D, Whiting WB. Analysis, synthesis, and design of chemical processes. 5th ed; 2018.
- [29] Jenkins S. 2019 Chemical engineering plant cost index annual average, <https://www.chemengonline.com/2019-chemical-engineering-plant-cost-index-annual-average/>; 2020.

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- [30] Zhang C, Liu C, Wang S et al. Thermo-economic comparison of subcritical organic Rankine cycle based on different heat exchanger configurations. Energy 2017; 123:728-741. <https://doi.org/10.1016/j.energy.2017.01.132>.

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Declaration of interests

☒ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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