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1 **Experimental and numerical studies of press-braked S690 high strength** 2 **steel channel section beams**

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8

9 **Abstract**

10
11 The present paper describes an in-depth experimental and numerical investigation into the
12 flexural responses and strengths of press-braked S690 high strength steel channel section
13 beams bent about the minor principal axes in both the ‘u’ and ‘n’ orientations. The experimental
14 study was performed on eight press-braked channel sections, and comprised twenty-four
15 material flat and corner coupon tests, initial local geometric imperfection measurements, and
16 twelve beam tests in the four-point bending configuration. This was followed by a
17 complementary numerical modelling programme, where finite element models were firstly
18 developed and validated against the test results and afterwards adopted for performing
19 parametric studies to obtain an additional numerical data bank over a wide variety of cross-
20 section geometric sizes. The acquired test and numerical data were then employed to evaluate
21 the applicability of the Eurocode slenderness limits for welded and hot-rolled internal webs (in
22 compression) and outstand flanges (in stress gradients) to their press-braked counterparts,
23 revealing that the Eurocode slenderness limits can be safely extended to cover the
24 classifications of plate elements and cross-sections of press-braked S690 high strength steel
25 channel section beams. Evaluation of the accuracy of the cross-section flexural strengths

26 predicted from various design codes established in Europe, North America and Australia/New
27 Zealand was also made, based on the test and numerical data. The results of the quantitative
28 evaluation generally revealed that (i) all the examined design codes lead to overall conservative
29 and scattered predicted cross-section flexural strengths for press-braked S690 high strength
30 steel channel section beams, and (ii) the European code results in more precise design flexural
31 strengths for beams with relatively stocky channel sections, but less accurate strength
32 predictions for beams with relatively slender channel sections, compared to the North
33 American and Australian/New Zealand standards.

34

35 **Keywords:** Beam tests; Design standards; Finite element modelling; Local buckling; Minor-
36 axis bending; Press-braked channel sections; S690 high strength steel

37

38 **1. Introduction**

39

40 High strength steels (HSSs) are gaining increasing attention in the construction of long-span
41 and high-rise structures subjected to heavy vertical loading, owing to their superior strength-
42 to-weight ratios, allowing structural components to be designed with small cross-section
43 dimensions and light weights. For example, press-braked high strength steel S690 U-shaped
44 chords were used in the roof truss structure of the Friends Arena Stadium in Stockholm, Sweden,
45 and cold-formed high strength steel S690 hollow sections were employed in the Nesenbach
46 Valley Bridge in Stuttgart, Germany. Despite the great advantages of high strength steels over
47 the conventional normal strength mild steels, the lack of efficient design rules and the high
48 vulnerability to global instability have impeded the actual widespread application of high
49 strength steels in construction engineering. Experimental studies have therefore been prompted
50 to verify the structural performances of various types of high strength steel components and

51 develop precise and efficient design methods. The focus of this paper is on the in-plane flexural
52 behaviour and bending resistances of press-braked S690 high strength steel channel section
53 beams, and previous relevant experimental studies are firstly briefly reviewed. Pham and
54 Hancock [1] conducted twenty-four four-point bending tests on cold-formed high strength steel
55 lipped channel sections about the major principal axes to study their local and distortional
56 buckling responses and strengths. Lee et al. [2] carried out both four-point and three-point
57 bending tests on HSB800 and HSA800 steel (with the nominal yield stresses of 800 MPa) I-
58 section beams to examine their in-plane flexural behaviour, strengths and rotation capacities.
59 Wang et al. [3] investigated the local stability and bending strengths of hot-rolled square and
60 rectangular hollow sections fabricated from S460 and S690 high strength steels through
61 twenty-two in-plane bending tests, whilst the structural responses of cold-formed high strength
62 steel (with a range of nominal yield stresses from 700 MPa to 1100 MPa) tubular beams were
63 experimentally examined by Ma et al. [4]. Jiao and Zhao [5] reported experimental studies on
64 cold-formed circular hollow section beams made of high strength steel (with the nominal yield
65 stress equal to 1350 MPa) and assessed the cross-section slenderness limits. The brief review
66 revealed that although experimental investigations have been carried out on high strength steel
67 open and tubular section beams in bending about their symmetric axes, there were no studies
68 on high strength steel beam members bent about an axis that is not one of the symmetric axes.
69
70 This paper describes an experimental and numerical study of the in-plane flexural performance
71 and strengths of press-braked S690 high strength steel channel section beams bent about the
72 minor principal axes. The experimental study was performed on eight plain channel sections,
73 and consisted of twenty-four tensile flat and corner coupon tests, initial local geometric
74 imperfection measurements and twelve beam tests in the four-point bending configuration.
75 This was complemented by a finite element (FE) modelling investigation, in which nonlinear

76 FE models were firstly developed and validated against the experimental observations and
77 subsequently employed for carrying out parametric studies to derive an extended data bank
78 over a broader spectrum of cross-section sizes. The test results and numerical data were
79 compared with the flexural strengths predicted by the European code EN 1993-1-12 [6], North
80 American specification AISI S100 [7] and Australian/New Zealand standard AS/NZS 4600 [8],
81 allowing the accuracy of the established codified local buckling design provisions for press-
82 braked S690 high strength steel channel section beams in minor-axis bending to be assessed.

83

84 **2. Experimental study**

85

86 **2.1 General**

87

88 For the purpose of addressing the lack of test data on press-braked S690 high strength steel
89 channel section beams bent about the minor principal axes, a series of laboratory tests were
90 firstly conducted. Eight plain channel sections (C 60×40×5, C 80×40×5, C 80×50×5, C
91 80×60×5, C 80×80×5, C 100×40×5, C 100×60×5 and C 120×40×5), press-braked from the
92 same batch of hot-rolled grade S700MC high strength steel plates with the nominal material
93 thickness of 5 mm, were adopted in the present experimental investigation. The identifier of
94 each channel section is composed of a letter ‘C’ (indicating a channel section) and the nominal
95 section dimensions in millimetres (outer web height h × outer flange width b × wall thickness
96 t – see Fig. 1). Overall, the experimental programme included twenty-four tensile flat and
97 corner coupon tests to determine the material characteristics of grade S690 high strength steel,
98 initial local imperfection measurements to obtain the geometric deviations of the constituent
99 plate elements of each beam specimen, and twelve four-point bending tests to acquire the

100 flexural strengths of S690 high strength steel channel section beams bent about the minor
101 principal axes and study their in-plane flexural behaviour.

102

103 ***2.2 Material tests***

104

105 The channel section beam specimens studied in this paper were fabricated by press-braking,
106 which induced high localised plastic strains at the corner regions, thus leading to an
107 enhancement in material strength, though accompanied by a reduction in ductility. Material
108 tensile flat and corner coupon tests were both conducted to obtain the stress–strain curves and
109 key material characteristics of the considered press-braked S690 high strength steel channel
110 sections. One flat coupon and one corner coupon were respectively cut along the centrelines of
111 the flat part and corner region of each section in the longitudinal direction; moreover, additional
112 sets of flat and corner coupons were also extracted from channel sections C 80×40×5, C
113 80×60×5, C 80×80×5 and C 100×40×5 for the purpose of carrying out repeated tests. All the
114 flat and corner coupons were machined according to the geometric requirements given in
115 ASTM E8/E8M-15a [9], with the widths of 12.5 mm and gauge lengths of 50 mm. Material
116 tensile coupon tests were performed utilising an INSTRON 250 kN hydraulic testing machine
117 under displacement control, with the initial loading rate of 0.05 mm/min before attainment of
118 the nominal material yield stresses and a higher rate of 0.8 mm/min thereafter until failure of
119 the coupons. Note that flat and V-shaped end clamps were respectively utilised for gripping
120 flat and corner coupons during material testing. The material tensile coupon test setup [10–12]
121 is displayed in Fig. 2, including two strain gauges attached to the mid-height of the coupon and
122 an extensometer mounted onto the central necked portion of the coupon. The measured flat and
123 corner material stress–strain curves of the eight considered press-braked S690 high strength
124 steel plain channel sections are respectively presented in Figs. 3(a) and 3(b), with a summary

125 of the key measured material properties reported in Table 1, in which E is the Young's modulus,
126 f_y is the yield stress, f_u is the ultimate stress, f_u/f_y is the material ultimate-to-yield stress ratio,
127 and ε_u and ε_f are respectively the strains at the ultimate stress and fracture. The corner coupons,
128 as expected, exhibit higher material strengths but with reduced ductility, compared with their
129 flat counterparts. It can be seen from Figs. 3(a) and (b) that both the flat and corner coupons
130 display relatively rounded material responses with no obvious yield plateaus and sharply
131 defined yield stresses, and the corresponding 0.2% proof stresses are therefore defined as the
132 material yield stresses [13–15] in Table 1.

133

134 *2.3 Measurements on initial local geometric imperfections*

135

136 The in-plane flexural responses and strengths of beam members can be affected by their initial
137 local geometric imperfections, which were therefore carefully measured for each S690 high
138 strength steel channel section beam specimen prior to the bending tests. The procedure for
139 initial local geometric imperfection measurements was in line with that reported by Schafer
140 and Peköz [16], and the setup is depicted in Fig. 4, in which the beam specimen is mounted on
141 the milling machine bed and two linear variable differential transducers (LVDTs) are fixed to
142 the uniformly movable machine head, with the tips pointing at each constituent plate element
143 of the channel section beam specimen to record the local deviations along two representative
144 lines in the longitudinal direction. For each plate element, the measured data points from
145 LVDTs were then fitted by a linear regression surface, with the initial local geometric
146 imperfection amplitude taken as the largest derivation from the linear regression surface to the
147 original measured data points [17–19], as reported in Table 2, where ω_w , ω_{f1} and ω_{f2}
148 respectively denote the initial local geometric imperfection amplitudes of the internal web and

149 two outstand flanges, whilst the initial local geometric imperfection amplitude of the beam
150 specimen ω_0 is given as the maximum of ω_w , ω_{f1} and ω_{f2} .

151

152 ***2.4 Four-point bending tests***

153

154 A total of twelve four-point bending tests were performed to study the in-plane flexural
155 behaviour and resistances of press-braked S690 high strength steel channel section beams about
156 the minor principal axes. Specifically, for each of the eight examined channel sections, one
157 four-point bending test was performed about the minor principal axis in the ‘n’ orientation,
158 which induces the maximum tensile stress in the flange tip – see Fig. 5(a), whilst additional
159 four-point bending tests were also carried out on channel sections C 80×40×5, C 80×60×5, C
160 80×80×5 and C 100×40×5 in the ‘u’ orientation, which results in the maximum compressive
161 stress in the flange tip – see Fig. 5(b). All the beam tests were performed by using an INSTRON
162 2000 kN hydraulic testing frame at a fixed loading rate of 1 mm/min. Fig. 6 displays the four-
163 point bending test setup, in which the beam specimen is simply supported between two steel
164 rollers while a spreader beam is utilised to transfer load at the third-points of the flexural span
165 between the two steel rollers [20–23], underpinning bolts (inserted between the inner faces of
166 the two flanges) are used together with G-clamps (clamped onto the outer faces of the flanges)
167 at the two supports and two loading points for the purpose of precluding local bearing and
168 crushing failure at these positions, and three line transducers are arranged below the channel
169 section beam specimen to measure the vertical deflections at the mid-span and two loading
170 points. The readings from the three line transducers were used to derive the curvature of the
171 constant moment span between the loading points κ through Eq. (1) [24], where D_M and D_L are
172 the measured vertical deflections at the mid-span and two loading points, respectively, and L_0
173 is length of the constant moment span. In the present testing programme, the nominal length of

174 each beam specimen L was selected to be 1000 mm, and the flexural span between the two end
 175 steel rollers L_f was equal to 900 mm, leading to the length of the constant moment span L_0 of
 176 300 mm; the resulting span-to-height ratios of the beam specimens fell between 10 and 25,
 177 ensuring that all the beam specimens fail by in-plane flexure with negligible influence from
 178 shear. Table 2 reports the measured geometric dimensions of each press-braked S690 high
 179 strength steel channel section beam specimen, in which r denotes the internal corner radius of
 180 the channel section. The beam specimen ID begins with the cross-section identifier and ends
 181 with a letter ‘n’ or ‘u’ (indicating the bending orientation).

$$182 \quad \kappa = \frac{8(D_M - D_L)}{4(D_M - D_L)^2 + L_0^2} \quad (1)$$

183
 184 The key results acquired from the four-point bending tests are presented in Table 3, where
 185 $M_{u,test}$ is the failure moment, κ_f is the curvature at the failure moment, and $M_{u,test}/M_{pl}$ and
 186 $M_{u,test}/M_{el}$ are respectively the ratios of the experimental failure moment to the cross-section
 187 plastic and elastic moment resistances, in which $M_{pl}=W_{pl}f_y$ and $M_{el}=W_{el}f_y$ are given as the
 188 products of the material yield stress and the plastic and elastic section moduli, respectively;
 189 note that W_{el} and W_{pl} are determined about the elastic neutral axis (ENA) and plastic neutral
 190 axis (PNA) along the minor principal axis direction – see Fig. 5. The moment–curvature curves
 191 for press-braked S690 high strength steel channel section beam specimens bent in the ‘n’ and
 192 ‘u’ orientations are plotted in Fig. 7(a) and 7(b), respectively. Note that channel section beams
 193 are more susceptible to local buckling for the cases of ‘u’-orientation bending, and thus display
 194 steeper post-ultimate moment–curvature responses as well as lower failure moments and
 195 smaller curvatures at the failure moments than those obtained from the same channel section
 196 beams bent in the ‘n’ orientation. All the tested press-braked S690 high strength steel channel
 197 section beam specimens exhibited visible in-plane bending deformation, and more obvious

198 local buckling failure was observed for those specimens bent in the ‘u’ orientation; typical
199 deformed failure modes of the beam specimens C 80×60×5-n and C 80×60×5-u bent about the
200 minor principal axes in the ‘n’ orientation and in the ‘u’ orientation are respectively shown in
201 Figs. 8 and 9.

202

203 **3. Numerical modelling**

204

205 *3.1 General*

206

207 This section presents a parallel numerical modelling investigation into the flexural behaviour
208 of press-braked S690 high strength steel channel section beams, carried out by nonlinear FE
209 analysis package ABAQUS [25]. Development and validation of press-braked S690 high
210 strength steel channel section beam FE models were firstly detailed in Sections 3.2, followed
211 by parametric studies, which were performed based on the validated FE models to acquire an
212 extended numerical data bank over a wider range of cross-section sizes.

213

214 *3.2 Development and validation of FE models*

215

216 The shell element S4R, having been extensively used by the authors in the numerical
217 simulations of thin-walled steel open section structural members under various loading
218 conditions [12,15,18–21,26,27], was adopted in the present finite element modelling of press-
219 braked S690 high strength steel channel section beams. The mesh size was selected to be equal
220 to the wall thickness t of the modelled channel section for the flat regions while a finer mesh
221 of four elements was used to discretise the corner portions of the cross-section to capture the
222 rounded geometric profiles, following a prior mesh sensitivity study taking into account both

223 the numerical accuracy and computational efficiency. The measured flat and corner stress–
224 strain curves were converted into the true stress–strain responses and then assigned to the flat
225 regions and corners of the modelled channel section beams. For the ease of setting boundary
226 conditions, the two cross-sections at the supports were respectively coupled to two reference
227 points, which were positioned at the mid-point between the flange tips for the ‘n’-orientation
228 bending cases and at the mid-point of the web for the ‘u’-orientation bending cases; to mimic
229 the same simply-supported boundary condition adopted in the experiments, one reference point
230 was allowed for rotation about the bending axis as well as longitudinal translation, whilst the
231 other reference point was allowed only for rotation about the same bending axis. Besides, the
232 cross-sections at the two loading points were respectively set as rigid planes, allowed to rotate
233 about the bending axis and translate in both the vertical and longitudinal directions, in order to
234 replicate the four-point bending configuration. The initial local geometric imperfections were
235 also included in the FE models. The imperfection distribution profile of each beam model was
236 assumed to be of the first elastic local buckling mode shape [19–21], representing the most
237 unfavourable imperfection pattern of the beam model. Three imperfection amplitudes,
238 including the measured value ω_0 and 1/10 and 1/100 of the measured wall thickness of the
239 channel section, were utilised to factor the imperfection distribution profile of each beam FE
240 model, with the aim of assessing the sensitivity of the developed beam FE models to local
241 imperfection amplitudes. Upon development of the press-braked S690 high strength steel
242 channel section beam FE models, nonlinear static analyses were conducted by applying vertical
243 displacements at the locations of the two loading points to simulate the same loading procedure
244 and scheme adopted in the experiments.

245

246 The numerically derived results, including the ultimate moments, moment–curvature histories
247 and deformed failure modes, were then compared with the experimental observations to verify

248 the accuracy of the developed beam FE models. Table 4 lists the FE to experimental ultimate
249 moment ratios for the three examined imperfection amplitudes. The results of the comparisons
250 indicated that all the three imperfection amplitudes lead to overall accurate predictions of the
251 test ultimate moments, whilst the imperfection value of 1/100 of the wall thickness yields the
252 best agreement between the experimental and FE ultimate moments. Figs. 10 and 11 present
253 comparisons of the moment–curvature curves obtained from tests with those from nonlinear
254 FE analyses for typical S690 high strength steel channel section beam specimens C 80×60×5-
255 n and C 80×60×5-u bent about the minor principal axes in the ‘n’ orientation and in the ‘u’
256 orientation, respectively, both indicating that the test moment–curvature histories are well
257 represented by the corresponding numerically derived responses. The deformed failure modes
258 displayed by the beam specimens C 80×60×5-n and C 80×60×5-u were also shown to be
259 successfully captured by their numerical counterparts, as depicted in Figs. 8 and 9. Therefore,
260 the beam FE models, developed based on the aforementioned modelling assumptions, are
261 capable of simulating the in-plane flexural behaviour of the test press-braked S690 high
262 strength steel channel section beam specimens, and deemed to be validated.

263

264 *3.3 Parametric studies*

265

266 In this section, the validated FE models were utilised to perform parametric studies for the
267 purpose of generating an additional numerical data bank on press-braked S690 high strength
268 steel channel section beams over a broad range of cross-section geometric sizes. Table 5
269 summarises the cross-section dimensions selected for the present parametric studies. Five
270 cross-section web-to-flange aspect ratios of 1.0, 1.5, 2.0, 2.5 and 3.0 were considered in the
271 present parametric studies through fixing the outer web heights of the modelled channel
272 sections at 150 mm and setting the flange widths to be respectively equal to 150 mm, 100 mm,

273 75 mm, 60 mm and 50 mm. In addition, the selected wall thicknesses fell between 2.8 mm and
274 24 mm, leading to a broad range of non-slender and slender channel sections being considered.
275 The flexural spans of the beam models were kept constant as 900 mm, with the two loading
276 points located at the third-points of the flexural spans. With regards to the modelling of material
277 and imperfections, the measured flat and corner stress–strain curves of channel section C
278 80×60×5 were adopted throughout the present parametric studies, whilst the imperfection
279 distribution pattern of each beam model was assumed to be of the first elastic local buckling
280 mode shape, with the maximum imperfection amplitude equal to 1/100 of the wall thickness.
281 A total of 118 press-braked S690 high strength steel channel section beams bent about the
282 minor principal axes in both the ‘n’ and ‘u’ orientations were modelled.

283

284 **4. Evaluation of existing design standards**

285

286 ***4.1 European code EN 1993-1-12 (EC3)***

287

288 ***4.1.1. General***

289

290 The current EN 1993-1-12 [6] for high strength steel structures with material grades up to S690
291 was developed in line with the corresponding EN 1993-1-1 [28] for normal strength mild steels.
292 Regarding the design of beam members susceptible to in-plane failure, both EN 1993-1-1 [28]
293 and EN 1993-1-12 [6] adopt the framework of cross-section classification, i.e. the flexural
294 strength of a cross-section is dependent on its class. Four cross-section classes were prescribed
295 in the current Eurocodes [6,28]: Class 1 and Class 2 sections, also termed plastic sections, are
296 capable of reaching the plastic moment capacities M_{pl} at failure; Class 3 sections, also known
297 as elastic sections, are able to develop their elastic moment capacities M_{el} at failure; Class 4

298 (slender) sections fail before the yield stresses are attained due to premature local buckling in
299 the slender plate elements, with the cross-section flexural strengths limited to the effective
300 moment capacities M_{eff} . Classification of a cross-section is made according to the class of its
301 most slender constituent plate element, whilst each constituent plate element within the cross-
302 section is categorised by comparing its flat width-to-thickness ratio (c/t) with the specified
303 slenderness limits, in which $c=b-t-r$ for outstand flanges and $c=h-2t-2r$ for internal webs. It is
304 worth noting that the existing European codes EN 1993-1-1 [28] and EN 1993-1-12 [6] only
305 provide slenderness limits for classification of hot-rolled and welded plate elements and cross-
306 sections, with no guidelines on their cold-formed (press-braked) counterparts. Evaluation on
307 the applicability of the Eurocode Class 2 and Class 3 slenderness limits to press-braked S690
308 high strength steel channel sections in bending is firstly made in Section 4.1.2, followed by
309 assessment of the Eurocode cross-section flexural strength predictions in Section 4.1.3.

310

311 *4.1.2 Class 2 and Class 3 slenderness limits*

312

313 The applicability of the EC3 Class 2 and Class 3 slenderness limits for outstand flanges under
314 stress gradients and with tips in compression was evaluated, based on the failure moments
315 obtained from tests and parametric studies on press-braked S690 high strength steel channel
316 section beams bent about the minor principal axes in the ‘u’ orientation. The graphic evaluation
317 results are shown in Figs. 12 and 13, respectively, in which the failure moments are respectively
318 normalised by the cross-section plastic and elastic moment capacities, and then plotted against
319 the $\alpha c/(t\varepsilon)$ and $c/(t\varepsilon k_{\sigma}^{0.5})$ ratios of the flanges, together with the corresponding EC3 Class 2
320 slenderness limit ($\alpha c/(t\varepsilon)=10$) and Class 3 slenderness limit ($c/(t\varepsilon k_{\sigma}^{0.5})=21$) for outstand flanges
321 under stress gradients and with tips in compression, where $\varepsilon=(235/f_y)^{0.5}$ is a material parameter,
322 α is the ratio of the width of the compressive portion of the flange to the flat width of the flange,

323 and k_σ is the plate buckling coefficient and equal to $0.57 - 0.21\psi + 0.07\psi^2$ for outstand flanges
324 under stress gradients and with tips in compression [29], in which ψ is the end tensile to
325 compressive stress ratio of the flat part of the flange. It was generally found from Fig. 12 that
326 the test and FE data points intersect with the unity line at the $ac/(t\varepsilon)$ ratio of around 10 and are
327 accurately captured by the current Eurocode Class 2 slenderness limit ($ac/(t\varepsilon)=10$). However,
328 the test and FE data, depicted in Fig. 13, intersect with the unity line at the $c/(t\varepsilon k_\sigma^{0.5})$ ratio of
329 around 38, revealing that the current Eurocode Class 3 slenderness limit ($c/(t\varepsilon k_\sigma^{0.5})=21$) is
330 excessively conservative. In sum, the results of the evaluation indicate that the current
331 Eurocode Class 2 slenderness limit ($ac/(t\varepsilon)=10$) can be safely and accurately used for the
332 classification of the outstand flanges of press-braked S690 channel sections bent about the
333 minor principal axes in the ‘u’ orientation, while the Class 3 slenderness limit ($c/(t\varepsilon k_\sigma^{0.5})=21$)
334 is excessively conservative.

335

336 On the basis of the experimental and numerical data on S690 high strength steel channel section
337 beams bent about the minor principal axes in the ‘n’ orientation, the applicability of the
338 Eurocode Class 2 and Class 3 slenderness limits for internal plate elements in compression
339 were also evaluated. Figs. 14 and 15 present the normalised experimental and numerical
340 ultimate moments (by the cross-section plastic and elastic moment capacities, respectively)
341 plotted against the web flat width-to-thickness ratios $c/(t\varepsilon)$, together with the Eurocode Class 2
342 and Class 3 slenderness limits ($c/(t\varepsilon)=38$ and $c/(t\varepsilon)=42$) for internal plate elements in
343 compression. Similar conclusions can be made that the EC3 Class 2 slenderness limit ($c/(t\varepsilon)=38$)
344 for internal plate elements in compression is capable of precisely differentiating Class 1 and
345 Class 2 internal webs of press-braked S690 high strength steel channel sections from their Class
346 3 counterparts, while the Class 3 slenderness limit ($c/(t\varepsilon)=42$) leads to safe but rather
347 uneconomic classification results.

348

349 *4.1.3 Cross-section flexural strength predictions*

350

351 In this section, the EC3 cross-section flexural strength predictions of press-braked S690 high
352 strength steel channel section beams bent about the minor principal axes in both the ‘n’ and ‘u’
353 orientations were evaluated through comparisons against the acquired test and numerical
354 failure moments. The design cross-section flexural strengths, as specified in EN 1993-1-12 [6],
355 are given as the plastic ($M_{pl}=W_{pl}f_y$), elastic ($M_{el}=W_{el}f_y$) and effective ($M_{eff}=W_{eff}f_y$) moment
356 capacities for Class 1 (or Class 2), Class 3 and Class 4 channel sections, respectively, in which
357 W_{eff} is the effective section modulus and determined based on the effective cross-section area
358 excluding the ineffective area due to local buckling. The effective area of each constituent plate
359 element of the channel section consists of (i) the full area of the tensile portion and (ii) the
360 effective area of the compressive portion, calculated as the product of the wall thickness t and
361 the effective width of the compressive portion $b_{eff}=\rho b_c$, in which b_c is equal to the full width of
362 the compressive portion of the plate element and ρ is the reduction factor (accounting for loss
363 of effectiveness of the compressive portion of the plate element due to local buckling), with
364 the formulae shown by Eqs. (2) and (3) for outstand flanges and internal webs, respectively, in
365 which $\bar{\lambda}_p$ is the plate element slenderness and determined as $\sqrt{f_y/f_{cr}}$, where f_{cr} is the elastic
366 local buckling stress of the plate element, as given by Eq. (4); note that the plate buckling
367 coefficient k_σ is equal to 4.0 for internal webs in pure compression, but taken as $0.57 - 0.21\psi$
368 $+ 0.07\psi^2$ for outstand flanges under stress gradients and with tips in compression [29]. Upon
369 calculation of the effective areas of all the slender plate elements of the Class 4 channel section
370 in bending, the effective section modulus W_{eff} can then be derived; it is worth noting that
371 cumbersome iterations may be involved in the calculation of W_{eff} due to the shift in effective
372 neutral axis along with each round of calculation.

373
$$\rho = \frac{1}{\bar{\lambda}_p} - \frac{0.188}{\bar{\lambda}_p^2} \leq 1.0 \quad \text{for } \bar{\lambda}_p > 0.748 \quad (2)$$

374
$$\rho = \frac{1}{\bar{\lambda}_p} - \frac{0.055(3+\psi)}{\bar{\lambda}_p^2} \leq 1.0 \quad \text{for } \bar{\lambda}_p > 0.673 \quad (3)$$

375
$$f_{cr} = \frac{k_\sigma \pi^2 E}{12(1-\nu^2)} \left(\frac{t}{c}\right)^2 \quad (4)$$

376

377 The mean ratios of the experimental (and numerical) failure moments M_u to the flexural
 378 strengths predicted by EN 1993-1-12 [6] $M_{u,EC3}$ are reported in Table 6(a). The mean $M_u/M_{u,EC3}$
 379 ratios are respectively equal to 1.04, 1.79 and 1.78 for Class 1 (or Class 2), Class 3 and Class
 380 4 press-braked S690 high strength steel channel section beams bent in the ‘n’ orientation, with
 381 the coefficients of variation (COVs) of 0.03, 0.02 and 0.03, while the mean ratios of $M_u/M_{u,EC3}$
 382 are equal to 1.12, 1.82 and 2.00 for those Class 1 (or Class 2), Class 3 and Class 4 channel
 383 section beams bent in the ‘u’ orientation, respectively, with the COVs of 0.06, 0.04 and 0.08.
 384 The results of the quantitative assessment revealed that the existing EN 1993-1-12 [6] generally
 385 yields relatively accurate flexural strength predictions for Class 1 and Class 2 press-braked
 386 S690 high strength steel channel section beams in minor-axis bending, but results in
 387 excessively conservative design flexural strengths for their Class 3 and Class 4 counterparts,
 388 and that the EC3 flexural strength predictions are more conservative and scattered for the cases
 389 of ‘u’-orientation bending than for the cases of ‘n’-orientation bending. This is also evident in
 390 Figs. 16(a) and 16(b), where the failure moments for channel section beams bent in the ‘n’ and
 391 ‘u’ orientations, normalised by the design flexural strength predictions, are plotted against the
 392 flat width-to-thickness ratios of the webs and flanges, respectively.

393

394 **4.2 North American Specification AISI S100 and Australian/New Zealand Standard**
395 **AS/NZS 4600**

396

397 The North American specification AISI S100 [7] and Australian/New Zealand standard
398 AS/NZS 4600 [8] were established specifically for cold-formed steel members with material
399 grades up to S690. Regarding the design of flexural members, both standards adopt the same
400 provisions that the bending moment capacities shall be taken as the minimum of the local
401 buckling, lateral-torsional buckling and distortional buckling strengths. The present study is
402 focusing on S690 high strength steel channel section beams in bending about the minor
403 principal axes, which fail by in-plane local buckling, without any out-of-plane lateral-torsional
404 buckling and distortional buckling. Therefore, the bending moment capacities of the studied
405 S690 high strength steel channel section beams M_{nl} were calculated as the corresponding local
406 buckling strengths. Both AISI S100 [7] and AS/NZS 4600 [8] specify that the design bending
407 moment capacities shall be calculated based on either initiation of yielding or inelastic reserve
408 capacities, with the first approach adopted herein. Specifically, the elastic and effective
409 moment capacities ($M_{el}=W_{el}f_y$ and $M_{eff}=W_{eff}f_y$) were taken as the design bending moment
410 capacities for non-slender and slender sections, respectively. Regarding calculation of the
411 effective section modulus W_{eff} , AISI S100 [7] and AS/NZS 4600 [8] adopt the same procedure
412 as that employed in EN 1993-1-12 [6], but with different reduction factor expressions for
413 internal webs and outstand flanges, as given by Eqs. (5) and (6), respectively,

414
$$\rho = \frac{1}{\lambda} - \frac{0.22}{\lambda^2} \leq 1.0 \quad \text{for } \lambda > 0.673 \quad (5)$$

415
$$\rho = \frac{0.925}{\sqrt{\lambda}} \leq 1.0 \quad \text{for } \lambda > 0.856 \quad (6)$$

416

417 in which $\lambda = \sqrt{f/f_{cr}}$ is the plate element slenderness, where f is the maximum compressive
 418 stress in the considered plate element and derived based on an assumption that the design stress
 419 distribution across the plate element is linear with the yield stress at the initial yielding point;
 420 note that f is less than f_y for the internal webs of channel sections bent in the ‘n’ orientation and
 421 thus the determined AISI (or AS/NZS) plate element slendernesses $\lambda = \sqrt{f/f_{cr}}$ are less than
 422 the corresponding EC3 plate element slendernesses $\bar{\lambda}_p = \sqrt{f_y/f_{cr}}$, and f_{cr} is determined from
 423 Eq. (4), of which the plate buckling coefficient k_σ for outstand flanges under stress gradients
 424 and with tips in compression is determined by an alternative expression prescribed in AISI
 425 S100 [7] and AS/NZS 4600 [8], as given by Eq. (7); note that the resulting AISI (or AS/NZS)
 426 plate element slendernesses $\lambda = \sqrt{f/f_{cr}}$ are also smaller than the EC3 plate element
 427 slendernesses $\bar{\lambda}_p = \sqrt{f_y/f_{cr}}$ for the outstand flanges of channel sections bent in the ‘u’
 428 orientation.

$$k_\sigma = 0.145(b/h) + 1.256 \quad \text{for } 0.1 \leq b/h \leq 1.0 \quad (7)$$

430
 431 Quantitative and graphic comparisons of the design cross-section bending moment capacities
 432 $M_{u,AISI}$ (or $M_{u,AS/NZS}$) with the test and numerical failure moments M_u were conducted and
 433 presented in Table 6(b) and Fig. 17, respectively. The mean ratios of $M_u/M_{u,AISI}$ (or $M_u/M_{u,AS/NZS}$)
 434 are equal to 1.85 and 1.66, with the COVs of 0.05 and 0.03, for non-slender and slender press-
 435 braked S690 high strength steel channel section beams bent in the ‘n’ orientation, respectively,
 436 while the $M_u/M_{u,AISI}$ (or $M_u/M_{u,AS/NZS}$) ratios are equal to 1.77 and 1.09, with the corresponding
 437 COVs of 0.17 and 0.06, for those non-slender and slender channel section beams in ‘u’-
 438 orientation bending, respectively. Compared to EN 1993-1-12 [6], AISI S100 [7] and AS/NZS
 439 4600 [8] were shown to yield excessively more conservative cross-section flexural strength
 440 predictions for non-slender S690 high strength steel channel section beams, owing to the lack

441 of due consideration of plasticity, but more accurate and consistent cross-section flexural
442 strength predictions for slender S690 high strength steel channel section beams, attributed
443 mainly to the adoption of more relaxed (i.e. smaller) plate element slendernesses and more
444 accurate plate element width reduction factors.

445

446 Evaluation of the codified design cross-section bending moment capacities was also carried
447 out, based on the S690 high strength steel channel section beam test results only. Table 3 reports
448 the experimental to predicted failure moment ratios $M_{u,test}/M_{u,pred}$ for each tested beam
449 specimen. EN 1993-1-12 [6] was found to result in an overall higher level of design accuracy
450 but lower degree of design consistency than AISI S100 [7] and AS/NZS 4600 [8].

451

452 **5. Conclusions**

453

454 A thorough testing and numerical modelling programme has been conducted to study the in-
455 plane bending behaviour and capacities of press-braked S690 high strength steel channel
456 section beams. The testing programme was carried out on eight channel sections, and involved
457 twenty-four material flat and corner coupon tests, initial local geometric imperfection
458 measurements and twelve beam tests bent about the cross-section minor principal axes in both
459 the ‘u’ and ‘n’ orientations, while the numerical modelling programme included a simulation
460 study to replicate the structural responses of the tested beams and a parametric study to generate
461 an extended data bank over a wide variety of cross-section geometric sizes. The test and
462 numerical results were firstly employed to assess the applicability of the Eurocode Class 2 and
463 Class 3 slenderness limits for welded and hot-rolled outstand and internal plate elements to
464 their cold-formed (press-braked) counterparts, indicating that the Eurocode slenderness limits
465 can be safely used to perform classifications of plate elements and cross-sections of press-

466 braked S690 high strength steel channel section beams. On the basis of the test and numerical
467 results, the accuracy of the design cross-section bending moment capacities obtained from EN
468 1993-1-12 [6], AISI S100 [7] and AS/NZS 4600 [8] was then evaluated. The evaluation results
469 generally revealed that (i) EN 1993-1-12 [6] yields accurate and consistent cross-section
470 bending moment capacity predictions for stocky (Class 1 and Class 2) S690 high strength steel
471 channel section beams, but conservative and scattered design cross-section bending moment
472 capacities for their non-stocky (Class 3 and Class 4) counterparts, and (ii) AISI S100 [7] and
473 AS/NZS 4600 [8] were shown to result in more conservative bending moment capacity
474 predictions for non-slender S690 high strength steel channel section beams than EN 1993-1-12
475 [6], owing to the lack of due consideration of plasticity, but more accurate and consistent design
476 bending moment capacities for relatively slender S690 high strength steel channel section
477 beams, due to the adoption of more accurate effective width method.

478

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480

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491

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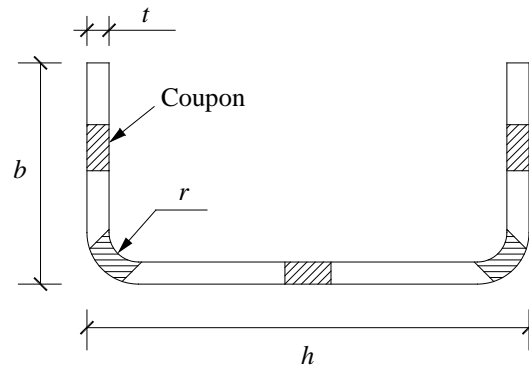


Fig. 1. Notation and locations of coupons.



Fig. 2. Tensile coupon test setup.

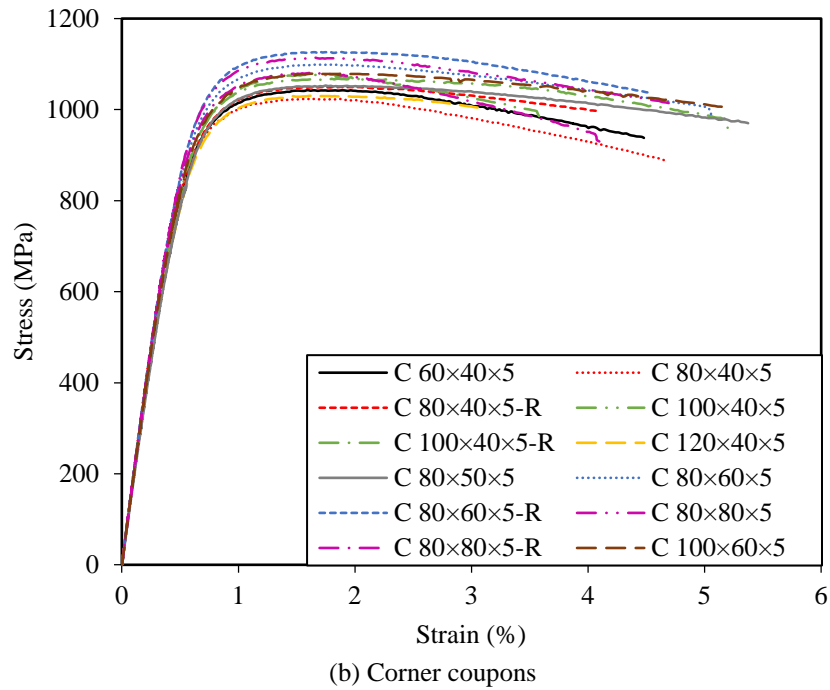
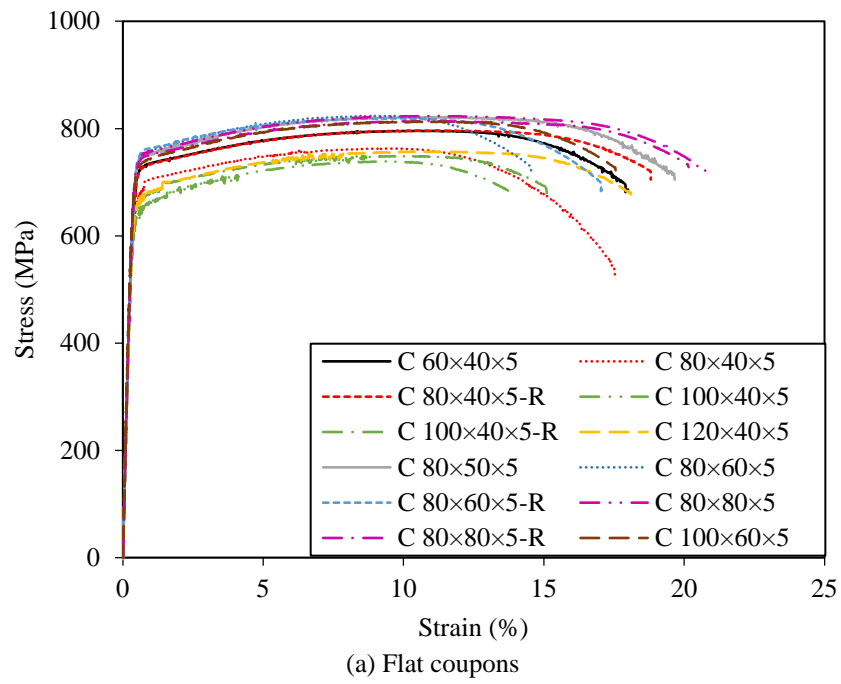
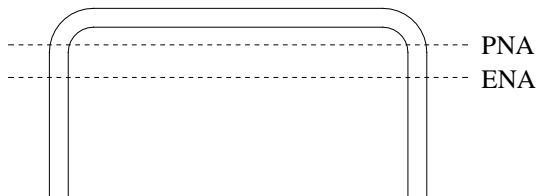


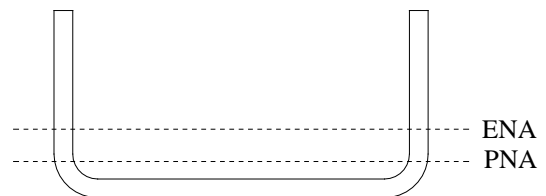
Fig. 3. Stress–strain curves measured from material tensile coupon tests on press-braked S690 high strength steel channel sections.



Fig. 4. Test setups for initial local geometric imperfection measurements.

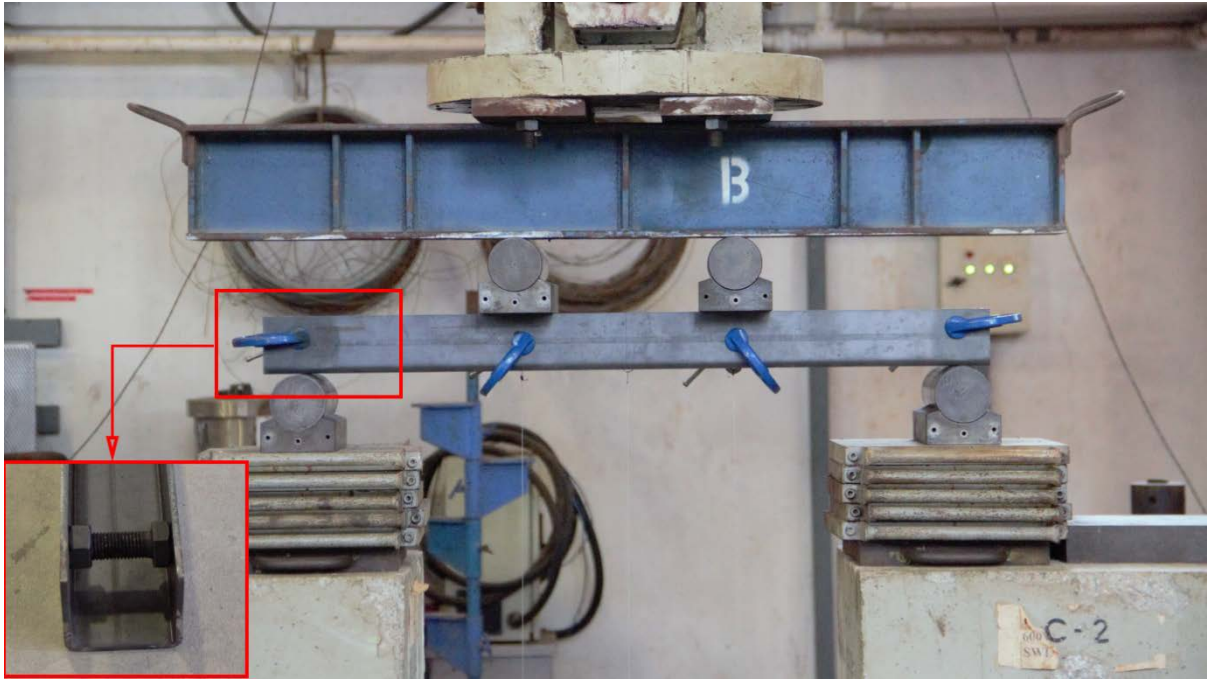


(a) Channel section bent in the 'n' orientation

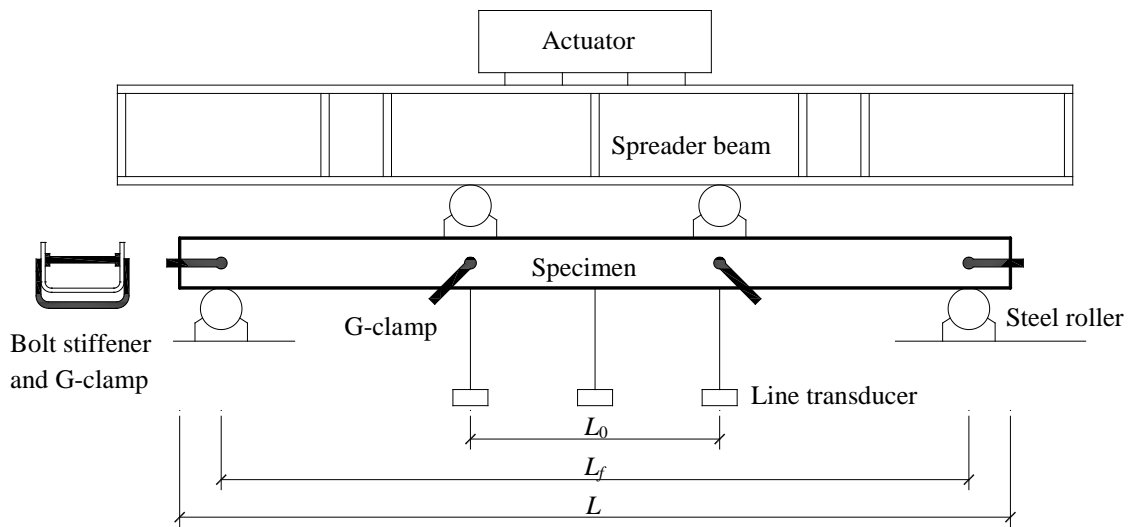


(b) Channel section bent in the 'u' orientation

Fig. 5. Elastic neutral axes, plastic neutral axes and bending orientations for channel sections bent about the minor principal axes.

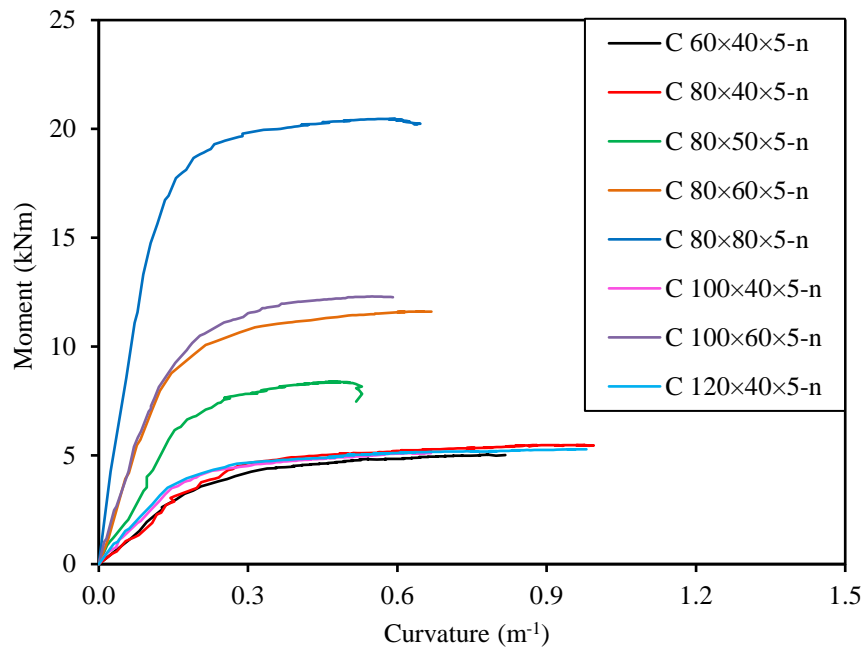


(a) Experimental setup

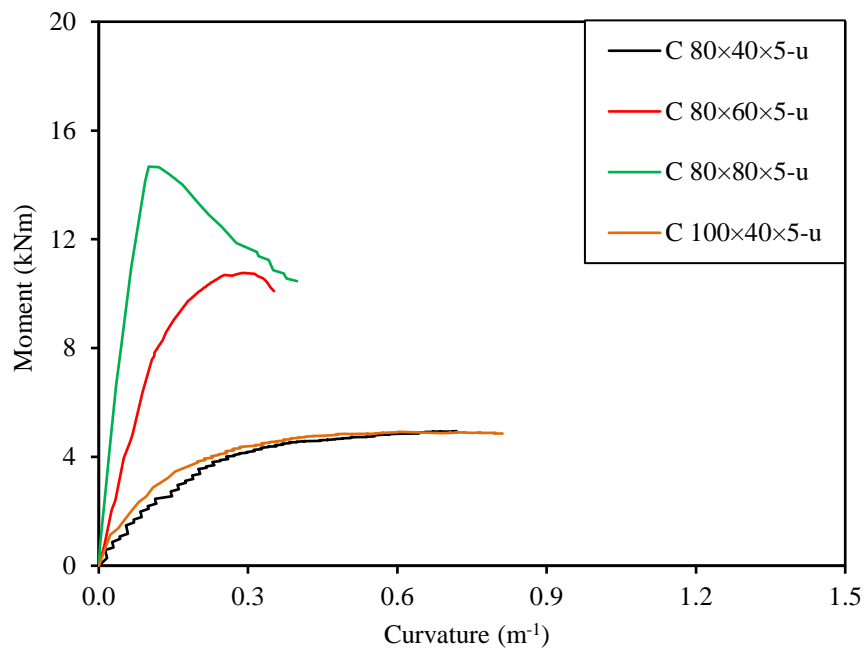


(b) Schematic diagram

Fig. 6. Experimental setup for press-braked S690 high strength steel channel section beams bent about the minor principal axes.



(a) Channel section beams bent in the 'n' orientation



(b) Channel section beams bent in the 'u' orientation

Fig. 7. Moment–curvature curves of the tested press-braked S690 high strength steel channel section beam specimens.



Fig. 8. Experimental and numerical failure modes for press-braked S690 high strength steel channel section beam specimen C 80×60×5-n.



Fig. 9. Experimental and numerical failure modes for press-braked S690 high strength steel channel section beam specimen C 80×60×5-u.

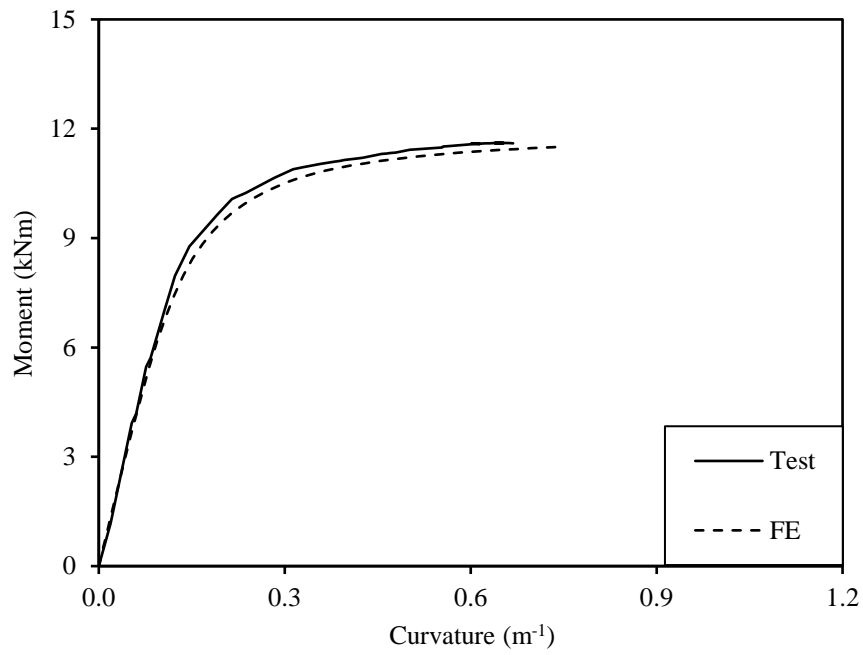


Fig. 10. Experimental and numerical moment–curvature curves for press-braked S690 high strength steel channel section beam specimen C 80×60×5-n.

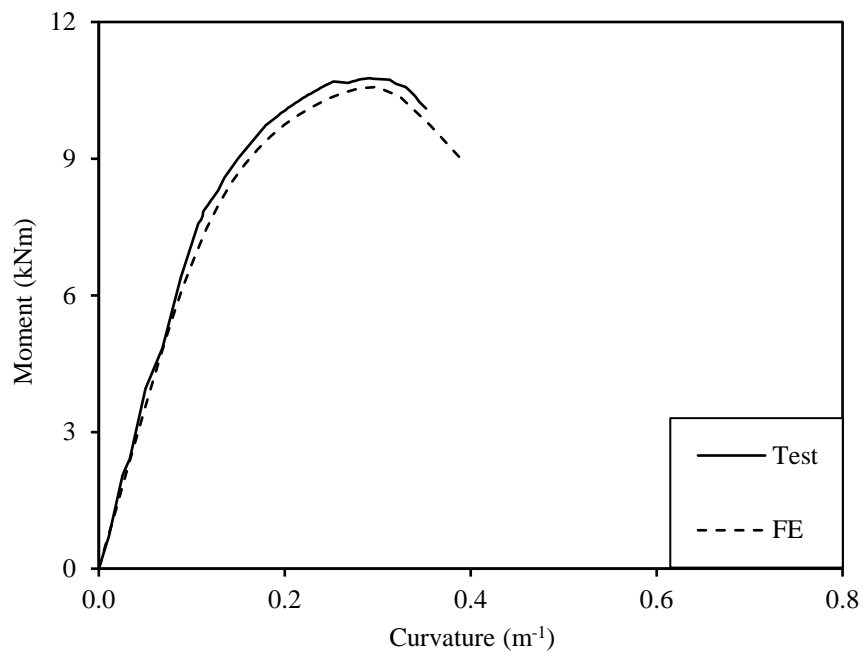


Fig. 11. Experimental and numerical moment–curvature curves for press-braked S690 high strength steel channel section beam specimen C 80×60×5-u.

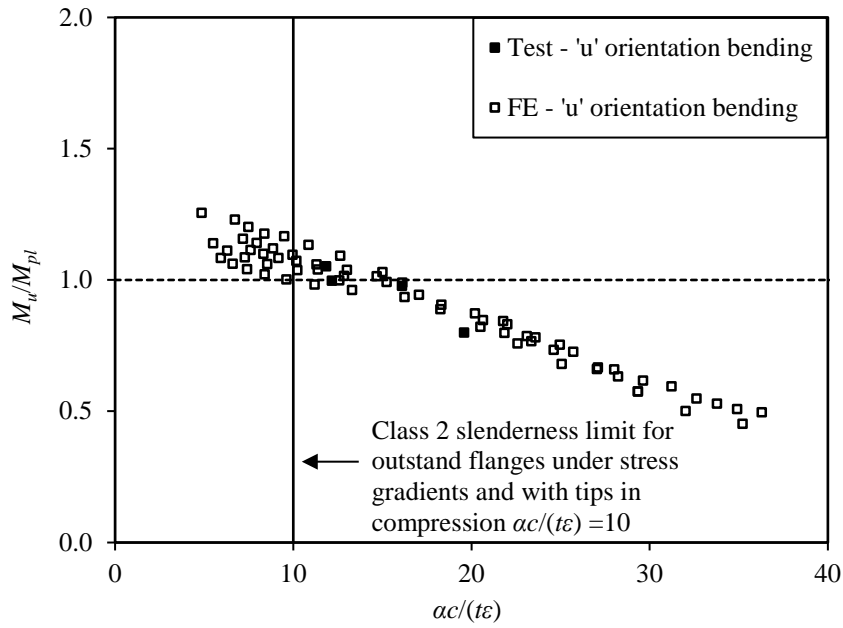


Fig. 12. Assessment of EC3 Class 2 slenderness limit for outstand flanges under stress gradients and with tips in compression.

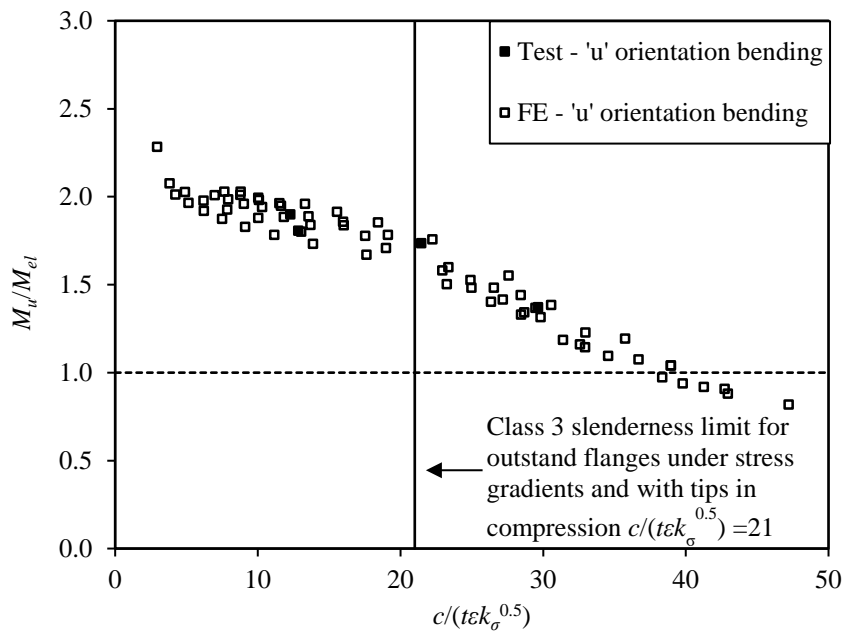


Fig. 13. Assessment of Class 3 slenderness limit for outstand flanges under stress gradients and with tips in compression.

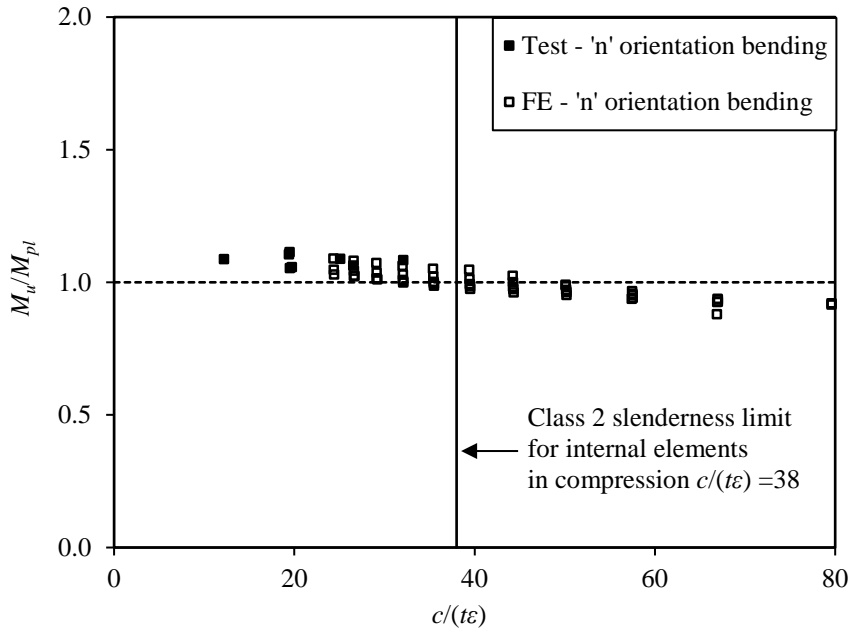


Fig. 14. Assessment of Class 2 slenderness limit for internal elements in compression.

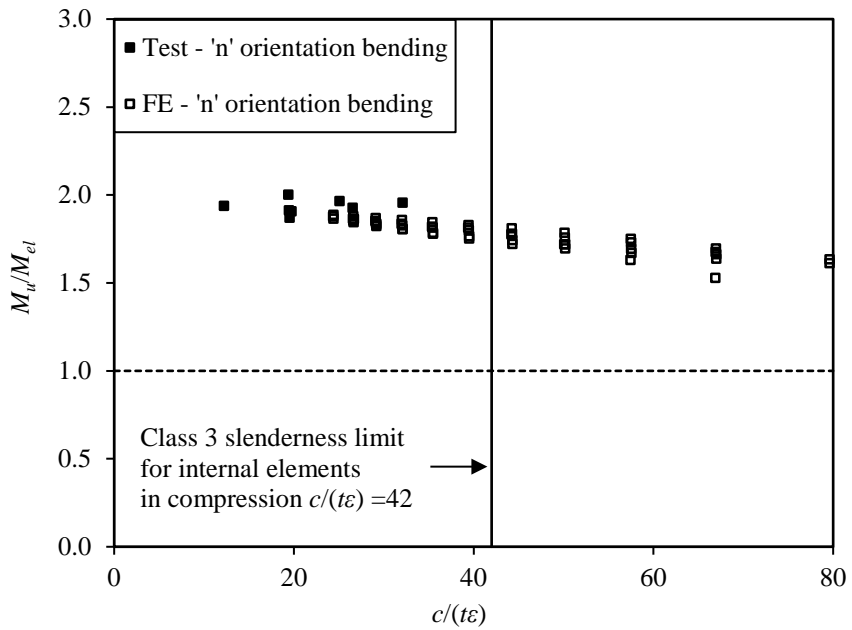
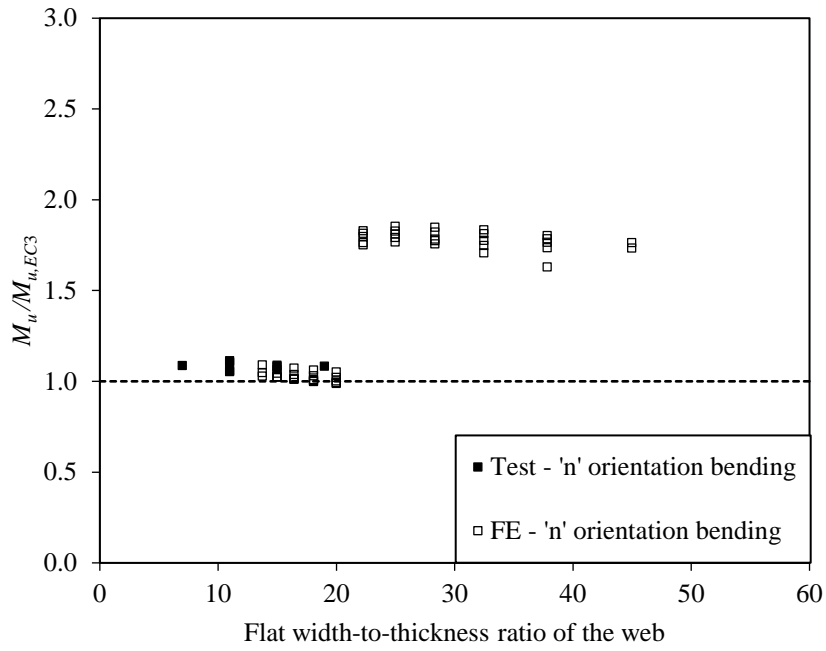
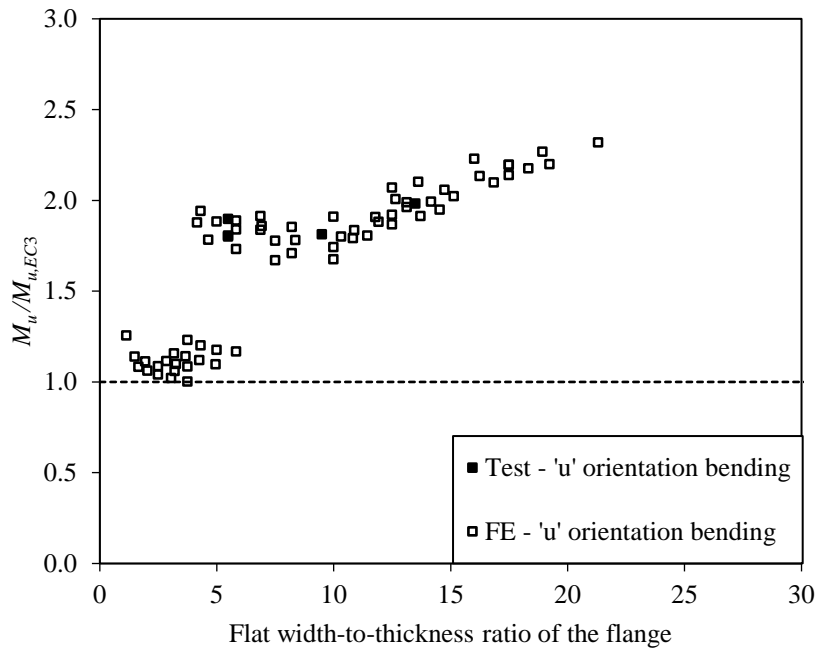


Fig. 15. Assessment of Class 3 slenderness limit for internal elements in compression.



(a) Channel section beams bent in the 'n' orientation



(b) Channel section beams bent in the 'u' orientation

Fig. 16. Comparisons of test and FE failure moments with EN 1993-1-12 flexural strength predictions.

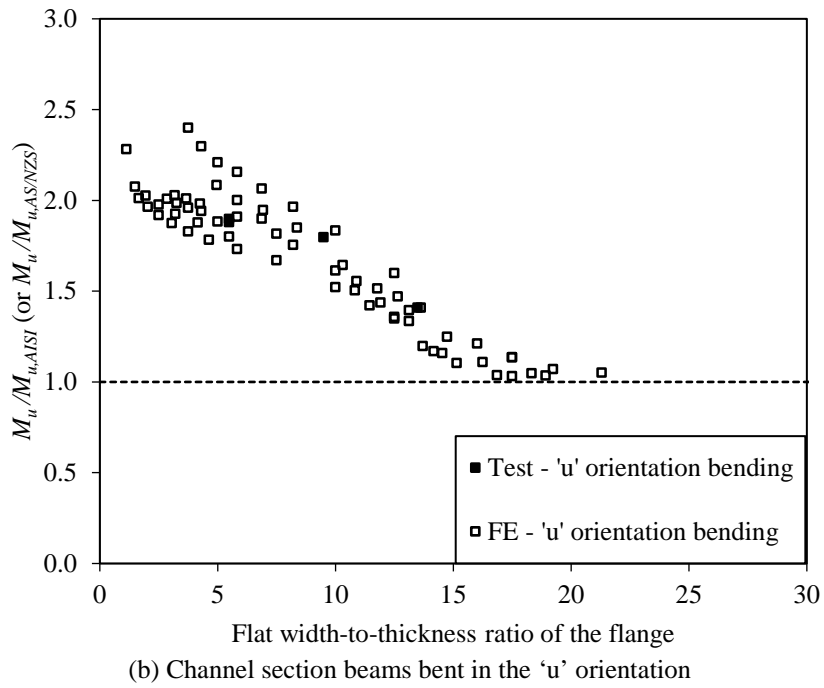
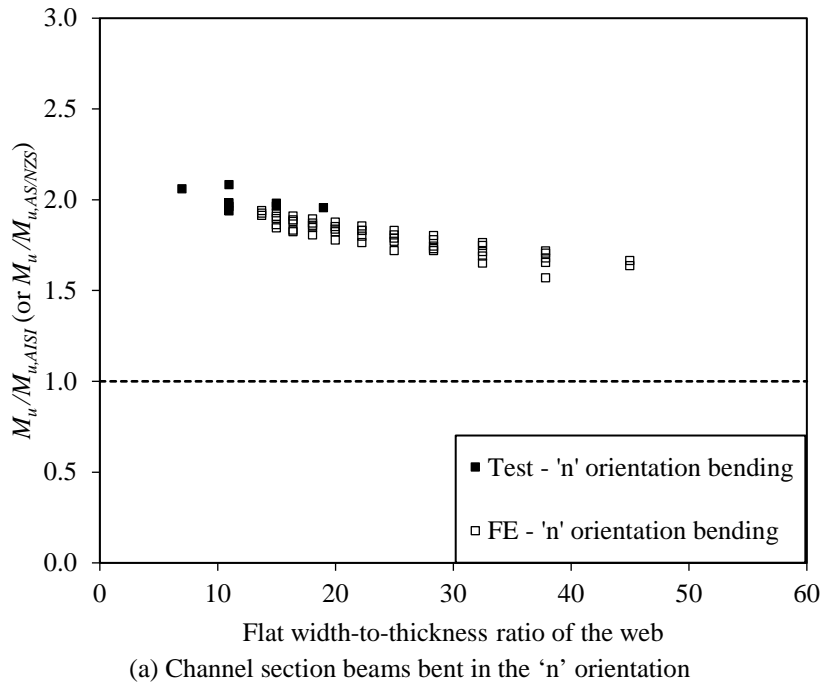


Fig. 17. Comparisons of test and FE failure moments with AISI S100 (and AS/NZS 4600) flexural strength predictions.