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Applying human mobility and water consumption data for short-term water demand forecasting using classical and machine learning models

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ABSTRACT

Water demand forecasting is a crucial task in the efficient management of the water supply system. This paper compares classical and adapted machine learning algorithms used for water usage predictions including ARIMA, support vector regression, random forests and extremely randomized trees. These models were enriched with human mobility data to improve the predictive power of water demand forecasting. Furthermore, a framework for processing mobility data into time-series correlated with water usage data is proposed. This study uses 51 days of water consumption readings and over 7 million geolocated mobility records from urban areas. Results show that using human mobility data improves water demand prediction. The best forecasting algorithm employing a random forest method achieved 90.4% accuracy (measured by the mean absolute percentage error) and is better by 1% than the same algorithm using only water data, while classic ARIMA approach achieved 90.0%. The Blind (copying) prediction achieved 85.1% of accuracy.

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Short-term forecasting; water demand; water consumption; geolocated data; classical forecasting; machine learning

1. Introduction

Water consumption prediction has recently become a very active field of study, as it leads to significant economic and environmental benefits (Brentan et al. 2018). Accurate water demand prediction ensures a reliable water distribution system and provides users with water in adequate volumes and reduced but sufficient pressure. Decreasing water pressure across the network not only improves energy efficiency through lower pumping energy consumption but also reduces the probability of network failures. Water demand predictions also help to identify leakages when observed consumption significantly differs from the forecasted water demand (Herrera et al. 2010). However, pressure reduction requires detailed knowledge of many water consumption factors.

There is a number of parameters affecting water consumptions such as climate, seasonality, economy, urban design and demographics (March and Sauri 2009; Wong, Zhang, and Chen 2010). Brentan et al. (2018) focused on water demand time series generation using a priori knowledge of water demand consumption and weather data such as temperature, precipitation and humidity. A similar set of exogenous variables was used by Al-Zahrani and Abo-Monasar (2015) in their study on daily water demand predictions in Al-Khobar, Saudi Arabia. Effects of including weather information were also investigated by Ghiassi, Zimbra, and Saidane (2008). Babel, Gupta, and Pradhan (2007) developed a model based on a multidimensional approach, using socio-economic characteristics, weather data, public water strategies and policies. Their results indicated that the demographic indicators, water tariff rate, public education level and average annual rainfall are significant variables for predictions of domestic water demand. These factors and their spatial and temporal resolutions have varying significance depending on the prediction time horizon. There are four common types of these horizons used for water forecasting (Rinaudo 2015): shortterm forecasting (hours, days, weeks) is used to optimise a water supplying system; intermediate-term forecasting (1–10 years) is used for demand predictions that account for change in the number of consumers; long-term forecasting (20–30 years) is usually used when major changes in the system need to be planned, e.g. in desalination plants and for large-capacity interbasin transfers.

The most commonly used predictive models for water demand forecasting comprise autoregressive integrated moving average (ARIMA) and autoregressive integrated moving average with exogenous variables (ARIMAX) methods (Braun et al. 2014; Alvisi, Franchini, and Marinelli 2007). Recent studies, however, introduce machine learning (ML) solutions, such as Artificial Neural Networks (ANN), Support Vector Regression (SVR) and regression trees, which now outperform the classical methods (Herrera et al. 2010; Tiwari and Adamowski 2017; Bennett, Stewart, and Beal 2013; Bai et al. 2014; Donkor et al. 2014; Antunes et al. 2018; Xu et al. 2019).

Despite the increasing number of studies on water demand forecasting using exogenous variables and growing awareness of the significance of the human factor, most research omits population behaviour or assumes only the regular patterns (Wong, Zhang, and Chen 2010; Alvisi, Franchini, and Marinelli 2007; Alcocer-Yamanaka, Tzatchkov, and Arreguin-Cortes

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2012). Since human water consumption accounts for a major proportion of water demand (Wong, Zhang, and Chen 2010), ignoring or simplifying this variable may reduce the accuracy of water demand forecasts. To address this research gap, this paper aims to study the influence of exogenous variables related to human mobility on water demand forecasting using classical and machine learning methods.

Human mobility-related data consist of at least a set of coordinates and a timestamp, which may be used to reconstruct human movements and mobility patterns (Barbosa-Filho et al. 2018). These data are harvested from various sources, such as mobile phones, wearable cameras or GPS devices and provide very detailed spatial and temporal information. Human mobility data have been used in city planning (Barbosa-Filho et al. 2018), traffic engineering (Toole et al. 2015) and epidemiology (Bengtsson et al. 2015). To the best of our knowledge, this research is a first attempt of utilising the innovative geolocated data for public utilities demand forecasting.

The objective of this research is to propose an integrated approach for short-term water demand forecasting using historical water consumption data in district metering areas (DMA) and human mobility data. This study compares the performance of classical forecasting methods and machine learning approaches for water demand prediction. The proposed approach is evaluated on five different DMAs in the city of Wroclaw and includes data processing and aggregating, training the forecasting models and validation. The merits and limitations of the applied methods are discussed and directions for further improvement of prediction accuracy are identified.

2. Materials and methods

The forecasting framework designed for this research is presented in Figure 1 and it reflects the structure of this section. The data (historical water consumption readings and mobile phone data records) are stored and spatiotemporally integrated into a database. The developed model connects to the database to get the data required for the chosen time of prediction. The data are then automatically processed and fed into the training, testing and evaluation step. At the same time, one of the forecasting methods described in Section 2.3 is tuned in an automated process to achieve the best possible model performance. Finally, the forecasted time-series are produced.

2.1. Study area

The study site is located in Wroclaw, the fourth largest city in Poland with a population of approximately 628,600 inhabitants, covering an area of nearly 293 km². The water is supplied to 99% of citizens from two main water treatment plants. The distribution network is characterized by a great variance in age and material which results in over 10% losses (Fialkiewicz et al. 2018). Annual energy consumption by the water supply system accounts for 19 GWh. Total Wroclaw's annual water consumption in 2018 was 48.7 hm³. Water consumption data used in this project were shared by local water infrastructure manager MPWiK S.A. in a form of ten-minute readings of water consumption in the DMAs.

Mobile phone data were purchased from mobile marketing company Selectivv that scans over 200,000 mobile applications to harvest information about mobile phones location. These data are gathered at the time when the mobile app storing location history was on the list of active applications or was running as a background process. The database consists of 7,133,087 geolocated data records with information for every record about event registration time (timestamp), application name, device location and in some cases also user ID.

The historical water consumption readings and mobile phone data records cover a time range of 51 days, from 21st of January (Sunday) to 12th of March 2018 (Monday) (for the dataset plots see Appendix A). Due to low temperatures within the selected period water consumption corresponds mostly to in-house water usage observed in winter. There are twenty-eight DMAs in Wroclaw that cover 51% of the entire city area. However, a considerable part of the city is still unmetered and therefore, any uncontrolled change in daily water demand hinders the management of water supply system. This study analyses five DMAs - labelled 10, 14_Z, 23, 24_Z, 32 which correspond to 34% of the total city hydraulic sectors area (Figure 2). The selected DMAs differ from each other by the predominant function of the buildings. Sectors 10, 14_Z and 32 are typical residential areas with around 80% of residential housing and less than 4% of industrial buildings. DMA 24_Z stands out with the highest percentage of the buildings with an industrial function which is 23% with only 45% of residential areas. Whereas, sector 23 accounts for a moderate percentage of residential and industrial areas. Consequently, population density also varies, ranging from ~3 000 inhabitants per km² in DMA 10 to less than 1000 inhabitants per km² in DMA 24_Z. The number of geolocated data records in each DMA is higher in residential areas (DMA 32: 30%, DMA 14 Z: 22%, DMA 10: 20% of the data) than in industrial and mixed sectors (DMA 24_Z: 17%, DMA 23: 10%).

The diversity of the predominant function of DMAs is reflected in the water consumption characteristics and week cyclicity. In residential and mixed sectors, increased water consumption can be observed in the mornings and the evenings of each day. While in the industrial sector, consumption is much more irregular and reduces significantly during the weekend (21.01.2018 – Sunday, 28.01.2018 – Saturday).

2.2. Data preprocessing

ensure maximum efficiency in data processing, То a spatiotemporal database was created using the open-source database software PostgreSQL and its extensions: PostGIS for spatial data and TimescaleDB for time-series. All the data have to be transformed and loaded into a database predefined structure. This has to be done manually. Therefore, the model is independent of the structure of provided data. Furthermore, the data are aggregated spatially into DMAs and temporally to one-hour bins. If provided data (either water consumption or mobility data) have lower temporal resolution it can be aggregated to the larger bins. Similarly, if an infrastructure manager provides different spatial segmentation (i.e. DMAs), then the data are aggregated to the provided areas. The datasets used in this study were thoroughly tested for their reliability, representativeness and consistency.



Figure 1. Scheme of water demand forecasting process.

To correct the water consumption data, erroneous readings were eliminated and the time series were examined for continuity. Outliers were removed using the interquartile range rule. In this method interquartile range (IQR) is the difference between the third (Q₃) and first quartile (Q₁). Every value lower than Q_1 – 1.5 x IQR and higher than Q_3 + 1.5 x IQR was eliminated. As a result, in sectors 10, 14 Z, 23, 24 Z and 32 the percentage of eliminated readings was respectively: 0,1%, 0,8%, 1,1%, 6,7% and 10,3% of the available data. The main reason for the elimination was a meter failure resulting in empty consumption readings, which accounted for over 95% of the rejected records. The remaining 5% were erroneous readings, i.e. those with negative values and outliers. After the initial filtrations, data continuity tests were carried out to identify and describe the length and density of time series gaps. Based on time series continuity charts, 51 days (from 21st of January to 12th of March 2018) were selected for the study, during which the gap in the data on water consumption did not exceed 1 hour.

The mobile phone data did not show any significant outliers, therefore, to prevent information loss, the geolocated data were not pre-processed but loaded into the database in a raw format. After loading and filtration, the data were spatially linked to the corresponding DMAs.

2.3. Forecasting models

Over the last decade, machine learning algorithms were found being superior to other statistical methods as they are highly capable of handling nonlinear and imprecise data (Ghalehkhondabi et al. 2017; Herrera et al. 2010). Furthermore, machine learning algorithms architecture can be easily adjusted to employ multi-source data in a prediction task. This work compares a few popular machine learning regression methods (Support Vector Regression (SVR) and ensemble tree-based methods) with ARIMA and ARIMAX models. As a simulation of lower bound of predictability, a Blind approach is employed.



Figure 2. Map of DMA sectors. Sectors included in this study are marked with turquoise colour.

2.3.1. ARIMA

Auto-regressive integrated moving average model (ARIMA) (Box et al. 2015) is a classical forecasting model which combines auto-regressive (AR) and moving average (MA) components with additional time-series differencing (I). ARIMA is defined as follows:

$$\phi_{p}(B)(t-B)^{a}X_{t} = \theta_{q}(B)a_{t}$$
(1)

where ϕ and θ are coefficients related to the AR and MA components respectively, estimated during a model fitting step. The X_t are the time-series elements at the time t and a are the residuals, B is a backshift expression used to denote previous elements or coefficients (named lags), hence $B^q = X_{t-q}$. ARIMA orders (parameters) p and q determine the number of previous lag observations taken into consideration when estimating model coefficients for AR and MA components and d is a number of differencing transformations, that is an order of lag subtracted from current element X_t .

Performance of a forecasting model can be improved by using additional information related to a predicted series. Such data are referred to as exogenous variables. ARIMA can be extended by adding such variables to the model. If we denote external k inputs as x_{tk} , then ARIMAX(p, d, q) is defined as:

$$\phi_p(B)(t-B)^d X_t = \theta_q(B)a_{Et} + \sum_{i=1}^k \eta \chi_i$$
(2)

where η are the coefficients of external inputs estimated at a model fitting step.

ARIMA and ARIMAX models have been used for decades and valued for their accuracy (Braun et al. 2014; Alvisi, Franchini, and Marinelli 2007). Various extensions of the models were proposed, one of which are SARIMA (seasonal ARIMA) models that account for seasonal effects approximated from the past data, improving their accuracy in long-term forecasting. Despite a large number of studies showing the superiority of machine learning based methods over these models, some studies show that ARIMA and ARIMAX models are still more accurate in long-term predictions than machine learning methods (Ghalehkhondabi et al. 2017).

2.3.2. Support vector machines

Support Vector Machines (SVMs) (Cortes and Vapnik 1995) are supervised machine learning methods. Support Vector Regression is the adoption of SVMs for regression problems. The idea of SVR is to fit a p-1 dimensional hyperplane to a given set of points in p dimensional space by minimising the loss function, which ignores errors yielded by points lying within a margin of tolerance (defined by the ε value). To support nonlinear regression problems, the kernel function is used to transform the data into a higher dimensional feature space where a linear regression can be performed. In comparison to traditional regression procedures, SVR attempts to minimize the prediction error bound to achieve generalized performance, instead of minimizing the observed training error. Over the last decade, a lot of research has been done to improve the SVR in water demand predicting task, finding it resistant to overfitting and having a lower error on previously unseen data, which is important for the noisy water consumption data (Ghalehkhondabi et al. 2017). The limitation of SVR is that the algorithm performance is vulnerable to parameters choice. In order to overcome this problem hybrid SVR with externally determined parameters can be implemented (Bai et al. 2014).

2.3.3. Tree-based ensemble methods

This is a class of supervised learning algorithms based on a tree structure, which can be used for regression problems. In ensemble methods, during the tree fitting process, a large collection of trees is constructed. Then, the result is computed as an average from the results of each tree. With the ability to model nonlinear relationships and resistance to overfitting, tree-based ensemble methods were applied for water demand forecasting producing better results than other machine learning algorithms (Chen et al. 2017; Herrera et al. 2010; Tyralis, Papacharalampous, and Langousis 2019). Furthermore, the tree-based ensemble methods

can effectively handle small sample sizes, which is important in the case of limited data availability. Among the significant limitations of this group of methods is their inability to extrapolate outside the range of a training sample (Tyralis, Papacharalampous, and Langousis 2019).

Random forests (RF) (Breiman 2001) learn a set of trees, where the training algorithm applies bootstrap aggregation (also known as bagging) to each learner which means that each new tree is constructed using randomly selected chunk of the data. In RF, a decision of the best node split, which minimises an internal error criterion, is made using a random subsample from an already selected fragment of a learning set. This leads to the creation of a series of uncorrelated trees, which individually are weak predictors. Then, a new sample is run through each of the trained trees. Because of a random characteristic of data subsample selection some data are not used to construct trees. These samples create an 'out-of-bag' dataset, which is used to evaluate the model and rebuild it with tuned parameters if needed. This procedure yields better results and prevents model overfitting.

Extremely randomized trees, called also Extra-Trees (ET) (Geurts, Ernst, and Wehenkel 2006) are also based on the bagging approach. The difference is that the whole dataset is used to train trees and a random selection of samples is applied at the node-splitting step, where a cutting point is selected at random from selected features. The node-splitting process stops only when the output is constant or the number of elements is lower than the selected value. From the bias-variance point of view, the strongly randomized approach reduces variance better than other algorithms, while using the whole sample for each tree construction minimises its bias.

2.3.4. Blind approach

The Blind approach is used to determine the lower bound of predictability and as a reference for any other algorithm. It is defined as:

$$X_t = X_{t-168h}.$$
 (3)

where X_t is the predicted water demand at time t and X_{t-168h} is the reading from exactly one week earlier.

2.4. Model validation

The results were evaluated using commonly known assessment methods. As a prediction accuracy measures, a mean absolute percentage error measure (MAPE), root mean squared error (RMSE) and Nash-Sutcliffe index of efficiency (EI) were used. If we denote *n* as a number of compared values, y_i as the original value of water consumption from the test or validation set, \hat{y}_i as the water demand prediction and \underline{y} as the mean value of the observations, then the measures are defined as follows (Donkor et al. 2014):

$$MAPE = \frac{100\%}{n} \sum_{i=1}^{n} \frac{|y_i - \hat{y}_i|}{|y_i|},$$
 (4)

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2},$$
(5)

$$EI = 1 - \frac{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}{\sum_{i=1}^{n} (y_i - y)^2},$$
(6)

The MAPE expresses a relative error which is comparable between different time-series. When it equals zero, then the prediction is identical to real water usage. The RMSE is sensitive to outliers and when equals to zero, the model fit data perfectly. It cannot be compared between time-series as it is not normalised. The El expresses the goodness of fit of a model and is more sensitive to systematic errors (Herrera et al. 2010). The El can range from $-\infty$ to 1 inclusively. When El = 1 the model perfectly fits the data.

The mean squared error (MSE) and mean absolute error (MAE) metrics were used as a split evaluation criterion in treebased models. These are defined as:

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - \hat{y}_i)^2,$$
 (7)

$$MSE = \frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i|, \qquad (8)$$

We use the autocorrelation function (ACF) and the partial autocorrelation function (PACF) for an initial determination of ARIMA and ARIMAX orders and validation of results. Autocorrelation is defined as the correlation between an element of a signal with its lag. Therefore, the autocorrelation of *n* lag is a correlation between elements X_t and X_{t-n} . Partial autocorrelation is a correlation between a signal with its own lagged values, where linear dependence for shorter lags are removed.

ARIMA and ARIMAX orders were selected using Akaike's Information Criterion (AIC) which is a commonly used measure for classical forecasting models (Anele et al. 2017). It is defined as:

$$AIC = 2n - 2nII, \tag{9}$$

where *n* is a number of estimated parameters in the model and *nll* is a log-likelihood function for the model. It is the metric of relative model quality on the same set of data. The model with the lowest value of AIC is considered the best.

2.5. Data processing

The pre-processed water use readings and mobile phone data are integrated into a database and must undergo further processing to improve the quality and structure of the data to more accurately predict urban water use. Each prediction is made using the period of 21-days of the data selected from the whole dataset.

2.5.1. Water consumption data processing

The filtered and pre-processed water consumption data are analysed to identify potential trends and week cyclicity effects which help to select the best parameters for forecasting models. To adjust to the temporal resolution of the mobile phone data, ten-minute readings are summed into one-hour periods. Any data gaps are identified and filled with the closest present reading from the same hour and day of a week.

2.5.2. Geolocated data processing

In order to use geolocated data as an exogenous predictor, transformation into time-series is required. As the mobile phone data are loaded into the database in a raw format, depending on the application, data may require selective filtration. For example, some mobile applications are programmed to automatically record a person's mobile phone position at midnight and, as this is not a common time for water consumption activity, these records are removed from the database. After filtering out useless records, the data are aggregated into one-hour bins for each DMA in the study area, where the total number of records per DMA is counted. This operation creates a time-series for each of the DMAs.

2.5.3. Data split

The water consumption and the processed geolocated data are merged and split into two datasets: 14 days of learning and testing sets and 7 days of validation data (66.7% and 33.3% respectively). The learning and testing data are taken together and shuffled during the 3-fold cross-validation process for model parameters tuning (Section 2.6), while the validation dataset is used only once at the end of the forecasting process.

N-fold cross-validation divides data n-times into learning and testing sets, which are used to train and evaluate tested models. This approach allows to achieve more reliable results through multiple repetitions of the learning-testing process and to detect overfitting at an early stage. Due to its individual time-series characteristics, the modified cross-validation process is implemented for this work. The previously pre-selected days are split using a moving time window which randomly selects a starting point at least two weeks before the last date in the training and testing dataset. The cross-validation results are calculated as an average from the test scores of each fold.

2.5.4. Raising data correlation

A high correlation between the geolocated data and water consumption time-series indicates their similarity. Therefore, the exogenous variable would potentially improve the forecasting accuracy if that variable is highly correlated with the predicted series. To maximise series correlation, the mobility data need to be processed each time when prediction has to be done. First, due to the temporal sparsity of the data, records from the whole training period are accumulated and averaged with respect to the days of the week. This creates a pattern of a 'typical week' for each of the studied DMAs. After that, the geolocated series is controlled by two parameters named decay and offset. The former informs how long a single record is accounted for, that is, if a mobile phone logs at a specific time, for non-zero decay values it will be still considered to be in an area for the determined period. The offset parameter shifts the geolocated series by a given value, so if the application creates a log just before a person arrives home, that would align mobile phone records with the water demand series (Figure 3(a)). These parameters are selected individually for each DMA during the model training phase through the exhaustive procedure. Parameters are learned only using the training data but are applied further throughout testing and validation phases. For each value of decay parameter, the offset that maximises the correlation of the geolocated series and the water consumption series is determined by the convolution of their Fourier transforms. The inverse Fourier transform is considered to be equal to the calculation of correlation of these series for every possible offset parameter. The combination of these two parameters with the highest series correlation value is selected. This procedure allows raising the correlation level to a range of 40% – 75%. (Figure 3(b)) and increase computational efficiency.

2.6. Model parameters selection

Each tested algorithm has its unique parameters determining its behaviour. Before training, the model automatically searches for the best parameters' combination for a current prediction. This is done by a searching algorithm which uses a predefined set of parameters to fit the model and selects the combination of these parameters giving the lowest error. The best parameters' combination is then used to validate the model. Results from the validation are presented in Section 3.

2.6.1. ARIMA and ARIMAX model tuning

First, predefined set of ARIMA and ARIMAX orders p (from 1 to 5), d (from 0 to 2), and q (from 1 to 5) is determined using ACF and PACF functions. Next, every possible combination of these parameters is tested by an exhaustive grid search algorithm which fits model to the training and testing data. The model with the lowest value of AIC is selected.

In classical approaches, cyclicity has to be determined explicitly for the algorithm. The seasonal pattern is modelled by the spline basis function (De Boor 1978) using current training set and is given as an exogenous variable. This approach captures the cyclicity of the data a priori and does not raise the complexity of the calculations.

2.6.2. Machine learning methods tuning

The tested ML methods' initial parameters (called hyperparameters) have to be set up before running the algorithm and can significantly affect a model's performance. For each of the algorithms, the best performing combination is selected using a random search and a training and testing dataset with 3-fold cross validation applied. It works similarly to the grid search method (2.6.1) but only *n* random combinations are selected. In this case, 100 combinations are tested every time.

Tree-based models are tested for a number of trained trees (from 10 to 1000) and a type of split evaluation criterion (MSE or MAE). The SVR model is tested for various types of kernels (linear, sigmoid, radial basis function, polynomial), various epsilon values (from 10^{-4} to 10) and a penalty parameter C (from 10^{-3} to 20). The epsilon value determines the threshold of an acceptable error where no penalty is given during the training process. The penalty parameter is used to control the trade-off between bias and overfit.

The machine learning methods were adapted for time-series forecasting, which required creating internal and external lag parameters. These lags define how many previous records (hours) from the data are considered at each prediction step. Internal lag determines the number of water demand readings considered and external lag controls the number of geolocated data records fed into the model.



Figure 3. Correlation of geolocated data and water usage time-series in DMA 24_Z: (a) series comparison after applying offset and decay parameters. (b) correlation depending on the decay parameter for each DMA. Depicted correlations are calculated for the best offset parameter.

Experimental calculations showed that MAPE drops for 24 and again for 168 lags, which is the length of a day and a week (in hours), respectively. The value of 168 lags is used for every prediction. After setting the number of internal lags, the same test is run for a number of external lags. However, for that parameter, the prediction accuracy does not vary significantly, since the external data are provided in real-time. Hence, 5 lags for geolocated data were used as it guarantees robustness for missing data in most cases and is low enough not to raise the complexity of calculations.

3. Results and discussion

Due to the heuristic nature of machine learning algorithms, it is important to ensure the multiple validation of the models on various time ranges. Experimental results were calculated in a validation process which was repeated 30 times, each time selecting 21 consecutive days of data from the whole study period of 51 days with a 24-hours step. Finally, errors were averaged from all the validation cases. For each method, different variants of fed data were calculated. The results for 7-days and 24-hours forecasts are presented in Tables 1 and 2 (for the separate results for each DMA see Appendix B). *W* indicates that historical water consumption data were used. The geolocated data are abbreviated as *G*. If a decay parameter was applied it is denoted as *D* and if time-series where shifted by an offset parameter it is denoted as O. Hence, when geolocated data were processed by decay and offset parameter it is abbreviated as G(D,O) and when data were not processed it is denoted as G. The geolocated data modified using only the offset parameter is denoted as G(O).

3.1. Weekly forecasts

Table 1 shows that the Blind prediction method, for a weekly forecast, has an accuracy (measured as 1 – MAPE) of almost 85%, which means that most of the long-term trends in the water demand are rather cyclic-based than week-based. Therefore, all the methods that contain cyclic-signal will be correct. Comparing all the other methods to the Blind approach reveals that the gained improvements are on the level of 20% for EI, 40% RMSE and up to 35% for MAPE.

Following this major notion that the cyclic variation plays a central role in water demand signal it is also clear to observe that classical autoregressive prediction methods such as ARIMA and ARIMAX provide second best predictions and are insensitive, i.e. they do not take any advantage of exogenous variable – geolocated data. It looks as the impact of such data contains too scattered, non-seasonal signal that is difficult to model using polynomials (Equation (2)).

The sole use of geolocation data (G in Table 1) provides less predictive accuracy than any other tested data source (Blind

Table 1. Calculated average MAPE, RMSE and EI for 7-days ahead forecast for all the DMAs with respect to the methods and variants.

Measure	Method	W	W + G	W + G(D,O)	W + G(O)	G
MAPE [%]	ET	10,044	10,071	10,056	10,075	19,891
	RF	9,611	9,558	9,601	9,601	17,769
	SVR	14,232	14,065	14,146	14,187	39,166
	ARIMA/ARIMAX	9,969	9,969	9,969	9,969	-
	Blind	14,934	-	-	-	-
RMSE [m ³ /h]	ET	3,476	3,474	3,480	3,479	5,271
	RF	3,369	3,355	3,368	3,366	5,098
	SVR	4,509	4,447	4,380	4,433	8,637
	ARIMA/ARIMAX	3,523	3,523	3,523	3,523	-
	Blind	5,798	-	-	-	-
EI [-]	ET	0,886	0,885	0,885	0,885	0,753
	RF	0,888	0,889	0,888	0,888	0,764
	SVR	0,809	0,813	0,813	0,813	0,361
	ARIMA/ARIMAX	0,863	0,863	0,863	0,863	-
	Blind	0,688	-	-	-	-

Table 2. Calculated average MAPE, RMSE and EI MAPE for 24-hours ahead forecast for all the DMAs with respect to the methods and variants.

Measure	Method	W	W + G	W + G(D,O)	W + G(O)	G
MAPE [%]	ET	10,963	11,036	11,060	11,040	31,679
	RF	9,612	9,529	9,637	9,623	27,327
	SVR	14,674	14,985	15,232	15,184	43,950
	ARIMA/ARIMAX	16,327	16,327	16,327	16,327	-
	Blind	16,126	-	-	-	-
RMSE [m ³ /h]	ET	3,371	3,381	3,391	3,388	7,523
	RF	3,040	3,030	3,057	3,046	7,144
	SVR	4,374	4,395	4,365	4,425	9,461
	ARIMA/ARIMAX	5,251	5,251	5,251	5,251	-
	Blind	5,176	-	-	-	-
EI [-]	ET	0,881	0,880	0,880	0,879	0,460
	RF	0,898	0,898	0,896	0,897	0,493
	SVR	0,811	0,801	0,788	0,794	0,185
	ARIMA/ARIMAX	0,669	0,669	0,669	0,669	-
	Blind	0,685	-	-	-	-

approach in terms of MAPE). It is, however, providing an advantage when looking into the RMSE and El parameters. These results show that the seasonal variation in the geolocation data were not pertaine, but a short term scatter would be well represented.

If one would like to compare machine learning methods (ET, RF, SVR) applied with or without geolocation data, it is clear that these data slightly change forecasts and the most success-ful uptake of such data improves forecasts by 1.4%. Moreover, increase in correlation between G and W time series as shown in the section 2.5.2. is not always improving forecasting skills of the algorithms (see Table 1 e.g. RF RMSE W + G vs W + G(D,O)).

3.2. 24-hours forecasts

Results in Table 2 show that for a 24-hours prediction the Blind method provides better estimates of the water demand than the one based on geolocation data only (G), but interestingly it also outperforms in all cases of ARIMA/ARIMAX approach. The other results shown in Table 2 are consistent with these presented in Table 1. Random forest approach works best based on all three statistics and adding geolocation data is improving solution only by a single percentage. It might suggest that for a shorter forecast horizon the cyclical term is less determining than for longer forecasts, hence the machine learning approaches (ET, RF, SVR) work better than standard predictive models and the Blind method.

3.3. Classical and machine learning water demand prediction methods

Results in Tables 1 and 2 indicate that the RF proved to be the best performing method for all the DMAs which is consistent with the results presented by Antunes et al. (2018). Yet, their analyses use a set of additional input features such as temperature and rain occurrences, which may cause different and incomparable results. Errors yielded by ARIMA/ARIMAX and ET algorithms are very similar to each other and 0.5% higher on average than the RF results. In accordance with Antunes et al. (2018) and Xu et al. (2019), the SVR algorithm performs worse than other models. Its performance results are similar to the Blind method. Also, Ghalehkhondabi et al. (2017) in the review paper point out that the machine learning (named soft computing methods) are outperforming classical multilinear regression, multiple non-linear regression and ARIMA methods. Literature review (Braun et al. 2014; Chen et al. 2017; Antunes et al. 2018) offers usually a comparison of shorter forecasts: daily water demand/use (one value per day) or sub-daily prediction (24 values per day). In these studies SVR (Braun et al. 2014) is outperforming SARIMA by 1% (1-sigma) and 4% (2-sigma) (measured as a percentile relative error). Antunes et al. (2018) present a comparison of models where ARIMA is outperformed by RF and ANN by 50% in terms of MAPE and 5% of RMSE. In another study (Adamowski et al. 2012) RMSE of ARIMA is two times higher than the best performing ANN method. It has to be mentioned that the weekly forecast is not usually validated

against the reference data (House-Peters and Chang 2011) but such studies are suggested (Ghalehkhondabi et al. 2017).

3.4. Autocorrelation function analysis

Additionally, the analysis of an ACF function on residuals was performed. In general, lower autocorrelation means that cyclic patterns and time-dependent relations have been captured and reproduced accurately. This usually leads to higher accuracy of predictions. The degree of residuals' autocorrelation is expressed as an averaged share of statistically significant correlation values. It is presented in Table 3 for 7-days and 24hours forecasts.

Table 3 shows that the average share of significant correlation values for both forecasting horizons is the lowest for the ARIMA/ARIMAX method which indicates that this method captures time-dependent relations best, despite the fact it is not the best performing one. This can be caused by the explicit modelling of the cyclic pattern in this method. The tree-based ensemble approaches have a slightly higher share of significant correlations in ACF function than ARIMA/ARIMAX approach, with RF approach being the best ML method, which is consistent with the presented prediction errors (Tables 1 and 2). On the other hand, SVR performed the worst of all methods, including Blind approach, demonstrating the inability of this approach to effectively model cyclic patterns in the data. In a shorter forecasting horizon all the ML methods are performing worse than for 7-days ahead prediction, while classical approach has the same amount of statistically significant correlation values in the ACF function.

Importantly, when geolocation data were applied along with W time series in the ML methods, the average share of significant correlation values drops slightly (up to 3%) with the W + G(D, O) combination providing the largest decrease. Presumably, the geolocation data helps model dynamic fluctuations of cyclic patterns generated through an alternation of the human factor in water consumption. The ARIMA/ARIMAX methods were not affected by the geolocation data, therefore it does not influence the ACF function of residuals.

Table 3. Averaged share of significant correlation values in the autocorrelation function for 7-days and 24-hours ahead forecasts for all the DMAs with respect to the methods and variants.

Method	W	W + G	W + G(D,O)	W + G(O)	G		
7-days forecast							
ET	2,92	2,90	2,87	2,93	3,87		
RF	2,82	2,78	2,74	2,79	3,43		
SVR	3,34	3,36	3,31	3,29	6,19		
ARIMA/ARIMAX	2,45	2,45	2,45	2,45	-		
Blind	3,19	-	-	-	-		
24-hours forecast							
ET	2,97	2,91	2,93	2,96	3,91		
RF	2,86	2,82	2,80	2,79	3,47		
SVR	3,38	3,39	3,38	3,30	6,22		
ARIMA/ARIMAX	2,45	2,45	2,45	2,45	-		
Blind	3,21	-	-	-	-		

3.5. Geolocated data application

The forecasts based only on the geolocation data are not capturing time-dependent relations, leading to worse performance. However, if it was possible to model cyclic patterns a priori it may significantly improve the effectiveness of this method.

Results presented in Tables 1–3 show that adding geolocated data as exogenous variable slightly improves the accuracy of ML methods and has the largest impact for the longer forecast horizon. Moreover, adding geolocation data reduces the number of significant correlation values in the ACF function of residuals. For the best performing method, the average MAPE improves by over 0.9%.

The implication of improved 24-hours predictions on water supplying system has the potential to reduce energy costs. It was shown that using accurate water demand forecasting in energy optimization of the water pumping system can reduce energy consumption for about 39.4% (Bouach and Benmamar 2019).

In comparison to other studies that used exogenous variables for water demand prediction, the accuracy gains are similar. Many water demand prediction models incorporate weather variables as an exogenous data as it has a large impact on prediction accuracy. Antunes et al. (2018) used temperature and rain information to predict water demand, achieving 0.25% MAPE improvement in the best case but at the same time they noted an increase of RMSE. Ghiassi, Zimbra, and Saidane (2008) improved MAPE of hourly forecasting model by 0.35% through adding weather information to the prediction. Al-Zahrani and Abo-Monasar (2015) did not provide a direct evaluation of the impact of adding weather information to prediction but they found MAPE to be varying by 0.71% depending on the types of variables used.

The geolocated data from mobile applications used in this study proved to be a useful addition for improved accuracy. Hence, to improve the model performance further, other more accurate human mobility data such as Call Detail Records and/or GPS data would have to be used. Future research will focus on more sophisticated utilisation of geolocated data and possible accuracy improvements. For instance, it is possible to classify geolocated data into trips and stops and to infer a purpose of a particular trip (Siła-Nowicka et al. 2016) and then link it to an individual water usage profile, which may result in a better performance of forecasting models. Incorporating other datasets such as weather conditions or land use data could further improve model accuracy (Stańczyk et al. 2018; Ghiassi, Zimbra, and Saidane 2008; Al-Zahrani and Abo-Monasar 2015).

4. Conclusions

The most important factor for a reliable and efficient water distribution system is providing an adequate volume of water at a reasonable pressure to its users. Therefore, short-term water demand forecasting is a crucial task in efficient water supply system planning and management.

This research studied the relationships between human mobility-related data and information about approximate forecasted water demand. The experiment was conducted on data from the city of Wroclaw in Poland during winter, a time of in-house water usage. The selected DMAs have mixed characteristics: the DMA 10, 14_Z and 32 are predominantly residential, DMA 24_Z is an industrial area and DMA 23 is a mixed residential-industrial area. The proposed approach is the first application of human mobility data in water demand prediction models. It also evaluates the ability of predicting water demands using only human mobility data, which may be a promising opportunity for water infrastructure managers who cannot afford to install meters on their network. With that, they still may be able to predict hourly urban water demand.

In this paper, the performance of classical and machine learning algorithms was compared. The selected methods were ARIMA, SVR, RF, ET and the Blind approach. The paper proposes a forecasting framework and describes the full workflow, starting with data cleaning and filtering, through geolocated and water demand data processing, to model training, tuning and evaluation. All of the tests were carried out with 3-fold cross-validation, using a different training and testing sample each time and validating the trained model once on the validation set.

The best performing algorithm was RF, reaching 90.4% prediction accuracy at an average for one-week ahead forecast. ET, which are also a tree-based algorithm, and classical regression methods had a slightly higher prediction error (4% on average). SVR performed worse than other methods and only slightly better than the blind approach. It was found that the autocorrelation of residuals was best minimised by the tree-based methods when exogenous data were used. Importantly, it was found that when human mobility data were incorporated into the model, statistical errors were lower and residuals were less correlated. It was also shown that the moderate (over 50%) correlation of the geolocated time-series and water demand data could be achieved through the introduction of decay and offset parameters, used for the human mobility data modification, which opens up the potential to use it as a water use predictor in the future. The future smart water supply management system could include a short-term prediction based on people mobility to locally adjust the pressure in the area where the large relocation of users is predicted or detected.

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