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Stray-field imaging of a chiral artificial spin ice during magnetization reversal

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Abstract

Artificial spin ices are a class of metamaterials consisting of magnetostatically-coupled nanomagnets whose interactions give rise to emergent behavior, which has the potential to be harnessed for the creation of functional materials. Consequently, the ability to map the stray field of such systems can be decisive for gaining understanding of their properties. Here, we use a scanning nanometer-scale superconducting quantum interference device (SQUID) to image the magnetic stray field distribution of an artificial spin ice system exhibiting structural chirality as a function of applied magnetic fields at 4.2 K. The images reveal that the magnetostatic interaction gives rise to a measurable bending of the magnetization at the edges of the nanomagnets. Micromagnetic simulations predict that, owing to the structural chirality of the system, this edge bending is asymmetric in the presence of an external field and gives rise to a preferred direction for the reversal of the magnetization, an effect not captured by models assuming a uniform magnetization. Our technique thus provides a promising means for understanding the collective response of artificial spin ices and their interactions.

Keywords

Artificial spin ice, Scanning SQUID microscopy; Nanomagnetism, Magnetization reversal, Chirality

Artificial spin ices consist of geometrically-arranged arrays of lithographically-patterned interacting nanomagnets, whose shape anisotropy defines two possible orientations of the static magnetization in each of the nanomagnets.¹ While these systems were originally designed to mimic the frustration found in rare earth pyrochlore compounds,² it has recently become clear that their geometric arrangement can be tailored to create materials with topology by design, which exhibit novel collective dynamics.³ For example, artificial spin ice can be tailored to support topological charge defects^{2,4,5} whose dynamics can be controlled^{6,7} and exploited for applications such as energy storage.⁸ It has also been demonstrated that

artificial spin ices possess rich excitations in the GHz regime⁹⁻¹² and can be tailored to act as metamaterials for spin waves.^{13,14} Moreover, specific geometries can be used to control magnetic ordering in the ground state¹⁵ as well as during thermal excitation¹⁶ and through external magnetic fields.^{17,18} In particular, it was demonstrated that an artificial spin ice with a chiral geometry can be used to create an active material in which the collective rotation of the average magnetization proceeds in a unique sense during thermal relaxation, thus exhibiting ratchet behavior.¹⁹ These dynamics were attributed to the topology of the magnetostatic field generated at the edges of the lattice, highlighting the importance of understanding the stray field distribution in such systems.

While a number of imaging techniques have been used to measure the static,^{20,21} quasi-static²²⁻²⁴ and dynamic^{10,11} properties of artificial spin ices, none of these have mapped the stray field during magnetization dynamics. Here, we use a nanometer-scale scanning superconducting quantum interference device (SQUID) with sub-micrometer lateral resolution to quantitatively map the out-of-plane magnetic stray field $B_z(x, y)$ of an artificial spin ice system as it is led through magnetic reversal at 4.2 K.^{25,26} This technique allows imaging stray field patterns in the presence of external magnetic fields up to $\mu_0 H_\perp = \pm 1.0$ T for out-of-plane fields and up to $\mu_0 H_\parallel = \pm 0.4$ T for in-plane fields. The investigated artificial spin ice system is a ‘chiral’ ice,¹⁹ which consists of a periodic pattern of four-nanomagnet vertices exhibiting geometric chirality in two dimensions, shown in Figure 1a. In contrast to the experiments in Ref.¹⁹, which have demonstrated dynamic chirality during thermal relaxation at room temperature, our system has substantially thicker, ‘frozen-in’ nanomagnets (see Methods) and the magnetization dynamics are driven by an external field.

Figure 1b is a schematic representation of the scanning nanoSQUID setup. By scanning the sample in the xy plane, the sample’s magnetic stray field distribution $B_z(x, y)$ can be measured. A simulated example of the resulting stray field map of the chiral ice at remanence is shown in Figure 1c and the evolution of the stray field pattern as a function of height is given in Supplementary Figure S1. Imaging the spatial configuration of the

stray field, $B_z(x, y)$, as a function of external in-plane fields, we find that, owing to the thickness of the nanomagnets, the magnetostatic interaction leads to the bending of the magnetization at their edges. This bending becomes most pronounced at low applied fields, close to remanence, and can be experimentally detected using our nanoSQUID when the tip is in close proximity to the sample. Moreover, based on micromagnetic simulations, we find that, in the presence of an external in-plane field, edge bending leads to an asymmetric energy landscape in which the clockwise and counterclockwise net rotations of the magnetization at an individual vertex are energetically inequivalent, leading to different switching fields for the two configurations. This chiral behavior cannot be described by assuming a uniform magnetization of the nanomagnets, demonstrating the importance of considering the large number of degrees of freedom of the magnetization in modeling its behavior. Moreover, the origin of the predicted behavior is different from the previously observed edge-driven dynamic chirality in very thin, thermally-active systems with similar geometry, in which the magnetization of each nanomagnet was uniform.

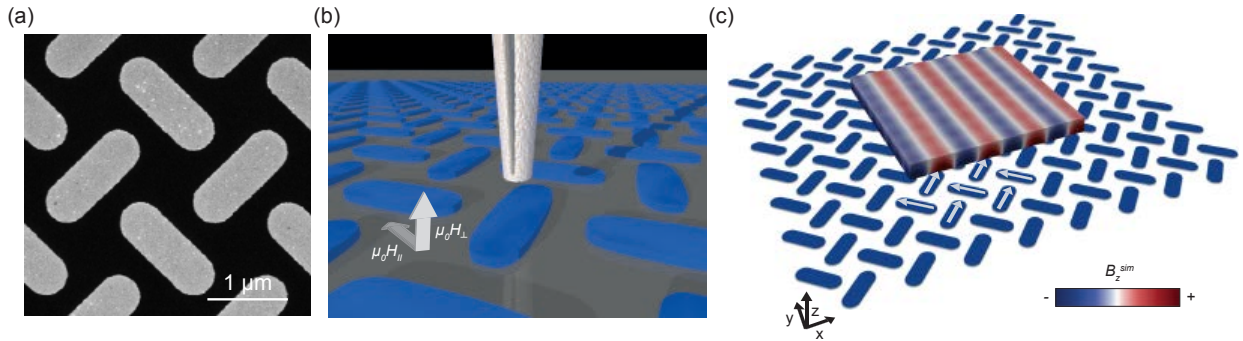


Figure 1: (a) Scanning electron microscopy (SEM) image of a vertex with chiral geometry. (b) Schematic drawing of the scanning nanoSQUID setup. By scanning the sample in xy -plane, the z -component of the sample magnetic stray field $B_z(x, y)$ can be measured. (c) Schematic representation of a chiral ice array at remanence. The white arrows represent the average magnetization within each nanomagnet at a vertex in the remanent state. The color plot shows the simulated stray field $B_z^{sim}(x, y)$ in a region ranging between 190 nm and 540 nm above a portion of the sample.

Results

Starting from saturation, we investigate the stray field pattern of the chiral ice driven by an in-plane field. Figure 2a-h shows a series of measured stray field distributions $B_z(x, y)$ for different applied in-plane field strengths ranging from $\mu_0 H_{\parallel} = 250$ mT to $\mu_0 H_{\parallel} = -250$ mT. The direction of the in-plane field is represented by a blue arrow in Figure 2a and has a small angle with respect to the y-axis. The observed stray field patterns result from the magnetic volume charge distribution within the nanomagnets and appear as diagonal regions of alternating field polarities (red and blue colors in Figure 2). Owing to the evolution of the magnetic state, these diagonal patterns evolve into vertical patterns parallel to the y-axis around zero field.

To interpret the measured stray field patterns, we perform micromagnetic simulations (see Methods). The simulated stray field distributions $B_z^{sim}(x, y)$ obtained for each applied field value $\mu_0 H_{\parallel}$ are shown in Figure 2i-p at the same location within the array. A quantitative match between the measured and simulated magnetic stray field distributions establishes a probe-to-sample distance of 450 nm. The simulated magnetization distribution within the nanomagnets is plotted in the insets. Simulations indicate that while the magnetization within the nanomagnets is uniform at 250 mT, as the field strength is reduced, it starts to exhibit a noticeable bending at the edges (Figure 2k-l), which is highlighted by the large white arrows. For field values between +10 mT and -10 mT, the magnetization aligns along the easy-axis of the magnetic structures, due to shape anisotropy, while the edge bending is maximal, since the magnetization at the edges is more susceptible to the applied field. At $\mu_0 H_{\parallel} = -10$ mT, the magnetization in individual nanomagnets starts to reverse.

Simulations show that the reversal is mediated by vortex nucleation and expulsion (on time scales of a few tens of nanoseconds), leading to a reproducible, non-periodic, stray field pattern (shown in Figure 2n). In the experiment, we equally observe a reproducible pattern (Figure 2f and in Supplementary Figure S3d). The differences between the measured and simulated patterns are attributed to the presence of edge roughness and pinning in the

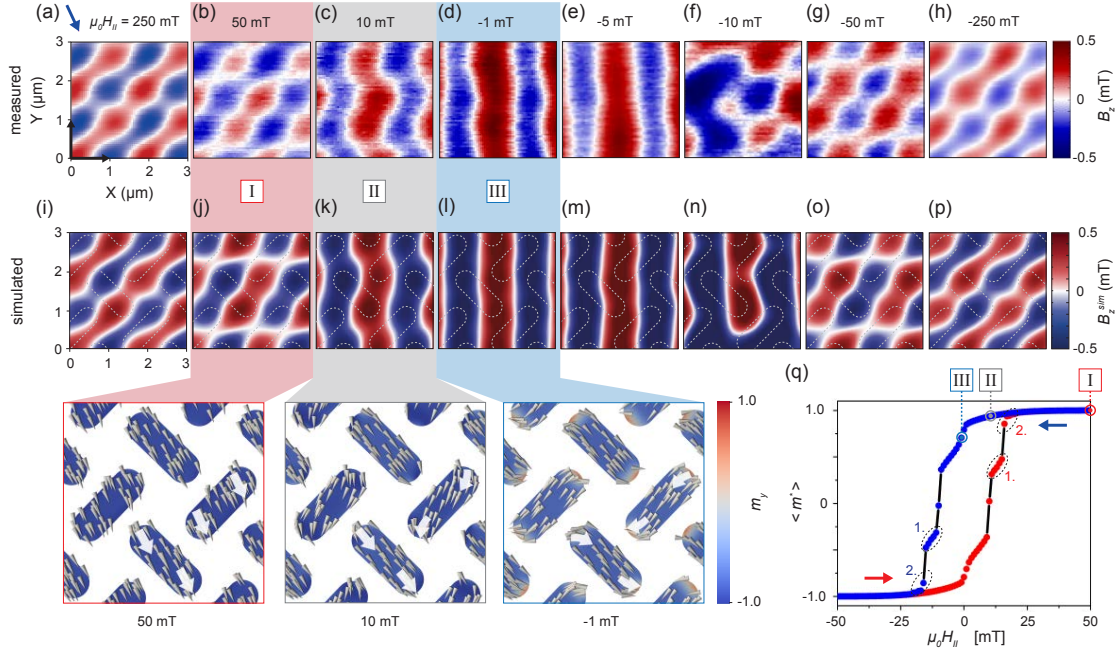


Figure 2: (a-h), Show a series of measured magnetic stray field strength distributions $B_z(x, y)$ for different values of the applied field $\mu_0 H_{||}$, whose direction is indicated in (a). (i-p) shows the corresponding series of simulated magnetic stray field strength distributions $B_z^{sim}(x, y)$, considering the same applied in-plane fields as in the experiment. The probe-to-sample distance is of ca. 450 nm. The direction of $\mathbf{H}_{||}$ is shown by a blue arrow in (a). In (i-p) the dashed outlines indicate the positions of the nanomagnets. In the lower insets, the magnetization at a vertex is plotted using conical arrows. The bending of the magnetization at the edges of the nanomagnets is highlighted by the thick white arrows. (q) Simulated hysteresis loop showing the two-step reversal of the nanomagnet lattice which occurs in the regions labeled ‘1’ and ‘2’. The states labeled I-III correspond to the states shown in (j)-(l). The first reversal is preceded by states in which the magnetization displays increasing edge bending (state III for example), favoring the nucleation of vortices, which mediate the reversal.

sample as well as to the possibility that the reversal might instead proceed through domain wall formation and propagation²⁷. At $\mu_0 H_{||} = -50$ mT (Figure 2g), $B_z(x, y)$ is similar to the pattern measured at +50 mT with an inverted polarity, as expected. The measured stray field distributions in the reverse direction along the hysteresis loop display similar behavior and are shown in Supplementary Figure S3a-g. Figure 2q shows a simulated hysteresis loop, plotted within the range $-50 \text{ mT} < \mu_0 H_{||} < 50 \text{ mT}$. Close to zero field, the edge bending increases until switching occurs around -10 mT. The region labeled ‘1’ corresponds to the reversal of the first sublattice of the system (in which the nanomagnets are mostly parallel

to the applied field), while the region labeled ‘2’ corresponds to the reversal of the second sublattice (in which the nanomagnets are almost perpendicular to the applied field).

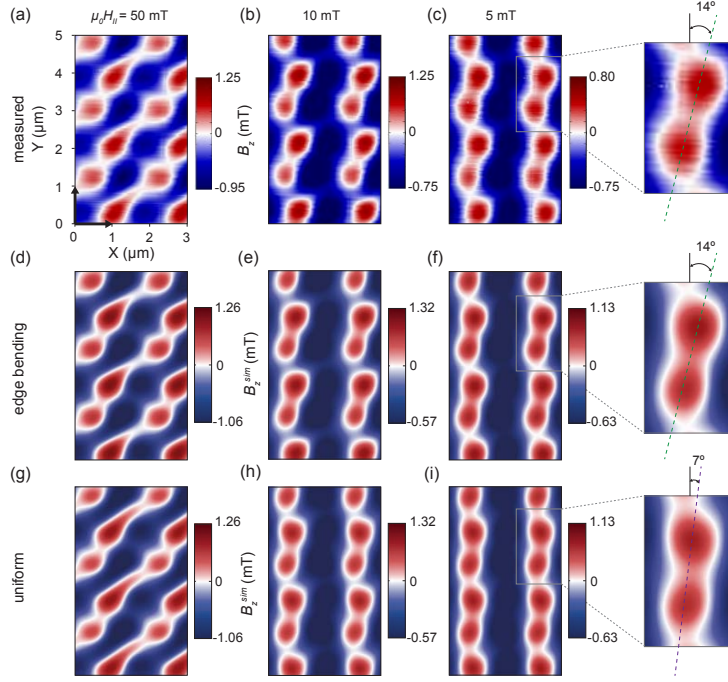


Figure 3: (a-c) Measured magnetic stray field strength maps $B_z(x, y)$ for different values of the applied external field $\mu_0 H_{\parallel}$. The probe-to-sample distance is reduced to 350 nm. (d-f) Simulated maps $B_z^{sim}(x, y)$ resulting from equilibrium configurations (for the same external field values) in which the magnetization displays edge bending. (g-i) Simulated $B_z^{sim}(x, y)$ distributions based on uniformly magnetized nanomagnets. The zoomed-in views of the patterns in (c), (f), and (i) highlight the orientation of the stray field patterns. Simulations in which the magnetization is uniform exhibit a different angle of the stray field pattern.

While the simulations presented in Figure 2 indicate that the magnetization exhibits noticeable edge bending, it is not immediately clear to what extent the bending can be distinguished experimentally in the stray field maps. In the following, we establish that the effects of edge bending are measurable using our nanoSQUID upon reducing the tip-sample distance. In the top row of Figure 3, (a-c) show the measured stray field patterns for three different values of the external field along the same branch of the hysteresis loop as in Figure 2, for a reduced tip-to-sample height of 350 nm. Micromagnetic simulations of the equilibrium configurations (displaying edge bending) are shown in the second row of Figure 3, reproducing the measured stray field patterns. The third row shows the stray field

distribution from simulations in which the magnetization of each nanomagnet is uniform. Differences in the simulated stray field distributions with and without edge bending become clear as the applied field is reduced and mostly drives the bending of the magnetization at the edges of the nanomagnets, leading to stray field patterns that increasingly differ from those of uniformly-magnetized nanomagnets. Zoomed-in views of the stray field patterns at 5 mT in Figures 3c and 3f highlight the similarity between the measured data and the simulations in the presence of edge bending, in contrast to simulations with uniform magnetization, shown in Figure 3i.

The presence of edge bending in other artificial spin ice systems, such as the kagome⁴ and square ices,² has been predicted to break vertex symmetry, modifying field-driven dynamics²⁸ and leading to the emergence of new magnetic phases as well as to changes in the mode spectrum of the system.²⁹ Here, our simulations show that in the presence of an of an applied in-plane field, edge bending has a direct impact on the energy of different magnetic configurations of the studied chiral ice and thus on the reversal paths of the magnetization. In Figure 4a, we consider a single vertex and compare the energy of the remanent state (labeled *RS*) with that of states in which the net vertex magnetization (represented by a green arrow) is rotated by 45° (labeled *CW45*, for the clockwise rotation and *CCW45* for the counterclockwise rotation) as well as by 90° (labeled *CW90* and *CCW90*) in the presence of a 2 mT field applied along the +y direction. The diagram in Figure 4b shows that the energy difference between the remanent state and states in which the net magnetization has rotated by 90°, is approximately double of that between *RS* and states in which the magnetization has rotated by 45°. Moreover, *CW* and *CCW* states have energies that differ by a few eV in each case. In comparison, given that the experiments are performed at a temperature of 4 K, thermal excitation only amounts to $k_B T = 0.3$ meV. Thus the energy difference between the *CW* and *CCW* rotations is significant enough to give rise to chiral dynamics. We find for example that fully reversing the magnetization of the vertex in the *CCW90* state requires a field of 9 mT, whereas reversing the magnetization of the *CW90* state requires

10 mT. (Reversing the magnetization of the RS state requires 11 mT.) Notably, although the simulations presented in figure 4 are for a single vertex, we find that the results hold when considering *CCW* and *CCW* configurations of the net magnetization of a vertex within a larger array.

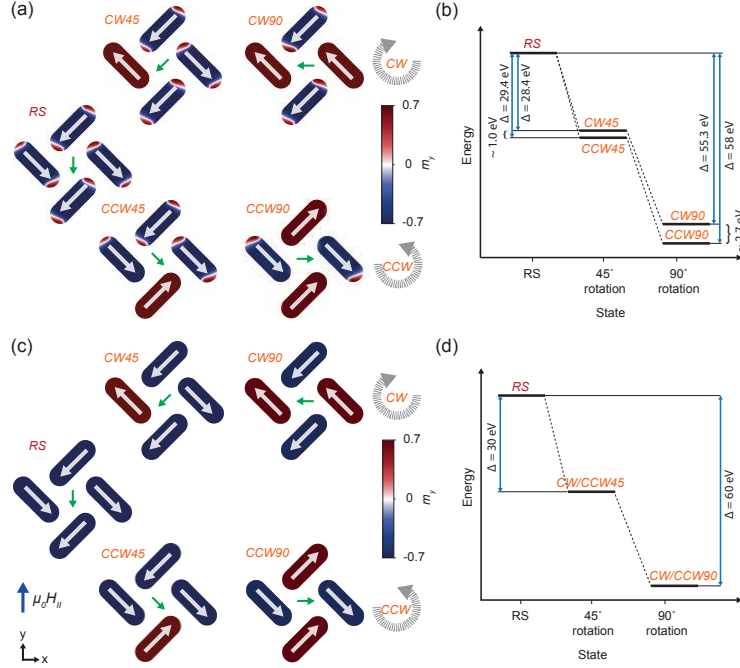


Figure 4: Simulated magnetization configurations and energies of a single vertex in the presence of a field $\mu_0 H_{\parallel} = 2$ mT, applied in the $+y$ direction. In (a), the simulations include bending of the magnetization at the nanomagnet edges. The net vertex magnetization in each state is represented by a green arrow at the center of the vertex. In (b) the energy differences between *RS* and states in which the net vertex magnetization is rotated clockwise (*CW*) or counterclockwise (*CCW*) by 45° and 90° are schematically shown. In (c), the simulations assume a uniform magnetization in each nanomagnet, while (d) gives the energy differences for the same intermediate states.

In contrast, considering nanomagnets with a uniform magnetization, we find that the *CW* and *CCW* energies are degenerate for both the 45° and 90° rotations (Figure 4c,d). These results demonstrate that the edge bending of the magnetization is responsible for the dynamic chirality: the direction of the edge magnetization induced by the external field differs in the *CW* and *CCW* states (see Figure 4a) owing to the broken symmetry of the system. Moreover, from Figures 4b and 4d, the configurations displaying edge bending have

slightly lower energy differences with respect to RS than the configurations with uniform magnetization. This can be understood in terms of the symmetries of the system: indeed, the magnetization of vertices in the uniform CW and CCW states displays inversion symmetry. States displaying this fundamental symmetry generally have higher energies as compared to states in which it is broken,³⁰ such as for the CW and CCW states in the presence of edge bending. The rather modest asymmetry between the simulated energy differences considering uniform states and considering states exhibiting edge bending highlights the fact that even seemingly small perturbations can lead to measurable effects in the presence of symmetry breaking. We note that in the presence of a field whose direction is tilted with respect to the y axis, as in figure 2, the reversal of the nanomagnets, which are most closely parallel to the field is favored leading to a similar, apparently chiral behavior, which is however not intrinsic. For example, assuming a 2 mT field such as in figure 2, we find that the energy difference between the $CW90$ and $CCW90$ states is larger (ca. 50 eV) and, in contrast, favors the CW rotation, thereby overriding the chiral dynamics defined by edge bending.

The difference in energies and, consequently, in switching fields of different configurations in the presence of edge bending is expected to lead to favored magnetization reversal paths in larger systems. In a recent experimental study, Li *et al.*¹⁷ have indeed observed that magnetization reversal in the chiral ice geometry is mediated by the formation of mesoscopic domains, separated by boundary regions defined by a limited number of vertex states with topologies resembling those of ferromagnetic domain walls. While these topologies were found to be dependent on the angle of the applied reversal field, we expect these to additionally be influenced by the predicted intrinsic chirality of the system, in particular when the field angle is close to zero. Moreover, the chiral boundaries of arrays with a similar geometry have been shown to play a role in the magnetization reversal process³¹ and may compete with the intrinsic chirality studied here which occurs in the bulk of the array.

Conclusion

We have performed scanning SQUID-on-tip measurements of a spin ice system and measured the evolution of its stray field as a function of external field. Our experiments, supported by micromagnetic simulations, demonstrate that the individual nanomagnets are not in a uniform state, but that their magnetization instead exhibits a strong bending at the edges of the nanostructures. Moreover, while the presence of edge bending has been studied in other artificial spin ice systems and was predicted to give rise to new magnetic phases as well as to changes in the mode spectrum of the system,²⁹ we predict that edge bending in the chiral ice geometry gives rise to an asymmetric energy landscape at individual vertices in the presence of an applied field. This favors the reversal of configurations in which the magnetization has rotated counterclockwise (with respect to the remanent state), giving rise to chiral dynamics. These results demonstrate how the presence of a large number of degrees of freedom of the magnetization can give rise to complex emergent behavior. Such behavior can be exploited to create artificial spin systems in which magnetic states could be tailored to design functional materials^{32,33} such as superferromagnets^{15,17} with tunable ground states and controllable reversal paths or reconfigurable²⁷ magnonic crystals^{13,34} with topologically-protected states¹⁴, which may enable new schemes for computing based on artificial spin ices.³⁵⁻³⁷

Methods

Sample Preparation: Large $230\text{-}\mu\text{m} \times 230\text{-}\mu\text{m}$ arrays consisting of Permalloy ($\text{Ni}_{83}\text{Fe}_{17}$) nanomagnet ensembles with chiral geometry as shown in Figure 1a were fabricated on a non-magnetic Si (100) substrate using electron beam lithography combined with thermal evaporation at room temperature and a base pressure of 10^{-6} mbar followed by lift-off. The nanomagnets had a length and width of $1.55\ \mu\text{m}$ and $560\ \text{nm}$, respectively, and a lattice constant of $1.5\ \mu\text{m}$ (center-to-center distance of neighbouring nanomagnets). To prevent

oxidation, a 2 nm thick aluminum capping layer was evaporated on top of the Permalloy. Atomic force microscopy (AFM) was used to measure the thicknesses of the arrays, which was measured to be 10 nm on average across the entire array, without taking the capping layer into account. Each nanomagnet had a homogeneous surface and the general shape displayed a high quality. Both are important factors to avoid a multi-domain state, which is not desirable. The size of the nanomagnets was chosen such that essential features (such as the separation between neighboring magnets as well as the spatial extent of the edge bending of the magnetization) were large enough to match the experimental resolution of the tip, while the thickness was chosen to insure that the nanomagnets were in a single-domain state. The single-domain nature of the magnetic state was determined using X-ray Photoemission Electron Microscopy (XPEEM).³⁸

Measurements: SQUID-on-tips were pulled to achieve the required SQUID-on-tip (SOT) diameter and fabricated using a three-step evaporation of Pb on the apex of a quartz capillary according to the technique described by Vasyukov *et al.*²⁵. The Pb evaporation was performed in a custom-made evaporator with a rotateable sample holder cooled by liquid ⁴He with a base pressure of 2×10^{-8} mbar. For protection of the SOTs against electrostatic discharge an Au shunt was deposited close to the tip apex prior to the Pb evaporation. SOTs were characterized in a test setup prior to their use in the scanning probe microscope. The SOTs used here had effective diameters between 100 and 150 nm, as determined by measurements of the critical current as a function of a uniform magnetic field applied perpendicular to the SQUID loop. The sub- μm resolution is limited by the spacing and – ultimately – the SOT diameter. Measurements of the critical current show pronounced oscillations as a function of H_{\perp} up to $\mu_0 H_{\perp} = \pm 1.0$ T and $\mu_0 H_{\parallel} = \pm 0.4$ T (see Supplementary Figure S1). We measured the magnetization evolution within the center of the arrays (i.e. far from the edges) in response to an applied field. The angle of the field, indicated in Figure 2a, was due to the experimental setup. Additionally, for each in-plane field strength, a small out-of-plane magnetic field is applied, which ensures that the working point of the SOT is in

the most sensitive region. This field is taken into account in the micromagnetic simulations and does not affect the magnetization within the nanomagnets due to their strong in-plane shape anisotropy (see [Supporting Information](#)).

Micromagnetic simulations: Micromagnetic simulations³⁹ were performed by solving the Landau-Lifshitz-Gilbert (LLG) equation in three-dimensions. The magnetostatic interaction, including the coupling between separate nanomagnets, is calculated using a hybrid finite-element/boundary element method. The simulations were carried out on a system of 144 nanomagnets, each with lateral dimensions of 833 nm \times 290 nm and 10 nm thick. The simulated size corresponds to approximately 50% of the lateral size of the measured nanomagnets, keeping the thickness as in the experiments, in order to reproduce the bending of the magnetization at the nanomagnet edges. The structure was discretized using a tetrahedral mesh with an average cell size corresponding to an equivalent cube with 5.7 nm side length. The simulated and measured stray field patterns were found to match for in-plane fields applied at an angle of 25° with respect to the y-axis. In Figure 4, the different states (*RS*, *CW*, *CCW*) were defined as initial configurations with uniform magnetization in each nanomagnet. The magnetization was dynamically relaxed into the lowest energy state. The nanomagnets in the single vertex simulations have the same dimensions as in the array simulations. For the hysteresis loop (Figure 2q), the field was varied in increments of 0.5 mT between 250 mT and -250 mT and the equilibrium states were obtained through energy minimization based on the conjugate gradient method. In Figure 2i-p, the magnetization was dynamically relaxed into the lowest energy state for the different field values, hence also capturing the dynamics during magnetization reversal. For the hysteresis loop (Figure 2q), the field was varied in increments of 0.5 mT between 250 mT and -250 mT and the equilibrium states were obtained through energy minimization based on the conjugate gradient method. The simulations were performed with the following material parameters for Permalloy: saturation polarization $\mu_0 M_s = 1$ T, exchange constant $A_{\text{ex}} = 1.3 \cdot 10^{-11}$ J/m and zero magnetocrystalline anisotropy $K = 0$, assuming a temperature of $T = 0$.

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Supporting Information Available

The Supporting Information is available free of charge on the ACS Publications website at DOI: XXXX, XXX, XXX-XXX.

- SuppInfo.pdf: Quantum interference pattern of the SQUID. Simulated stray field patterns as a function of height with respect from the sample. In-plane field hysteresis loop.

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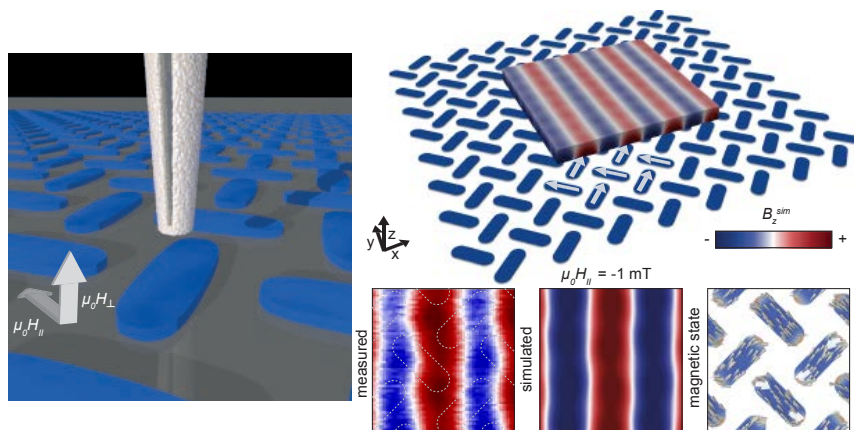


Figure 5: For table of contents (TOC) only.