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1	In-plane bending behaviour of S690 high strength steel welded I-section
2	beams
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9	
10	Abstract
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12	The present paper describes an in-depth experimental and numerical investigation into the in-
13	plane flexural behaviour and bending moment resistances of S690 high strength steel welded
14	I-section beams. The experimental investigation was conducted on six different welded I-
15	sections fabricated from the same batch of 5 mm thick S700MC high strength steel hot-rolled
16	plated by means of gas metal arc welding, and involved initial local geometric imperfection
17	measurements and twelve in-plane four-point bending tests, with six performed about the cross-
18	section major principal axes and another six conducted about the cross-section minor principal
19	axes. Following the experimental study, a numerical investigation was performed, where the
20	developed finite element models were firstly validated against the test results and then used to
21	perform parametric studies to generate further structural performance data over a broader range
22	of cross-section sizes. The obtained experimental and numerical results were carefully analysed

and then adopted to evaluate the accuracy of the existing slenderness limits (for classifications 23 of plate elements and cross-sections) and local buckling design rules for S690 high strength 24 steel welded I-sections in bending, as set out in the European, Australian and American 25 standards. The results of the evaluation revealed that the codified slenderness limits are 26 generally safe when used for the classification of the constituent plate elements of the examined 27 S690 high strength steel welded I-section beams, except for that given in the American 28 specification for slender/non-slender outstand elements in compression. All of the three 29 considered design standards were shown to yield accurate cross-section bending moment 30 31 capacity predictions for compact (Class 1 and 2) S690 high strength steel welded I-section beams bent about both the principal axes and non-compact (Class 3) S690 high strength steel 32 welded I-section beams bent about the major principal axes, but resulted in a rather high level 33 34 of conservatism in predicting the cross-section bending moment capacities for non-compact (Class 3) S690 high strength steel welded I-sections in bending about the minor principal axes 35 and slender (Class 4) S690 high strength steel welded I-sections subjected to both major-axis 36 37 bending and minor-axis bending.

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Keywords: Cross-section bending moment resistances; Cross-section classification; Finite
element modelling; Four-point bending tests; High strength steel grade S690; In-plane bending
behaviour, International design standards; Welded I-sections

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45 **1. Introduction**

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High strength construction materials have been increasingly used in bridge and structural 47 engineering. Compared with normal strength mild steels (e.g., grades S235, S275 and S355), 48 high strength steels (with the nominal yield strengths greater than 460 MPa) possess superior 49 mechanical strengths, and enable the achievement of structural components designed with 50 smaller cross-section sizes and lighter self-weights, which lead to structures with (i) more 51 usable interior space between vertical and horizontal components and (ii) lighter overall weight, 52 53 resulting in great savings in the costs of foundations and reduction in seismic loads. However, high material strength is accompanied by low material ductility, and thus high strength steels 54 are not desirable for fabricating beam-to-columns joints, where the rotation capacity (largely 55 56 dependent on the material ductility) is a major design concern. The lack of experimental verification of high strength steel structural members and joints at present limits the actual 57 application of high strength steel in construction engineering. Experimental investigations have 58 59 therefore been prompted to verify the structural behaviour of various types of high strength steel components (e.g., stub columns [1–4], long columns [5–9] and beam-columns [10]) of I-60 shaped sections, quantify their cross-section (or member) capacities, and develop precise 61 design approaches. However, it is worth noting that research into S690 high strength steel 62 welded I-section beams remains relatively scarce, despite three previous studies carried out by 63 McDermott [11], Beg and Hladnik [12] and Wang [13]. 64



section beams and further examine their flexural behaviour and strengths, a thorough testing 67 and finite element simulation study was conducted and presented in this paper. An experimental 68 study was firstly conducted on six S690 high strength steel welded I-sections, and involved 69 initial local geometric imperfection measurements and twelve in-plane four-point bending tests, 70 with six bent about the major principal axes and another six bent about the minor principal axes. 71 This was followed by a numerical modelling investigation, where finite element models were 72 firstly developed and validated against the test results and afterwards used to conduct 73 parametric studies, aiming at generating additional numerical data over a broader range of 74 75 section sizes. Finally, the experimentally and numerically obtained results were used to assess the accuracy of the local buckling design rules for S690 high strength steel welded I-section 76 beams, specified in the European code EN 1993-1-12 [14], Australian standard AS 4100 [15] 77 78 and American specification ANSI/AISC 360-16 [16].

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80 2. Experimental study

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A structural testing programme was performed to examine the in-plane bending behaviour and capacities of S690 high strength steel welded I-section beams. Six different I-section sizes were adopted in the present testing programme: $I-50 \times 50 \times 5$, $I-70 \times 70 \times 5$, $I-80 \times 60 \times 5$, $I-90 \times 70 \times 5$, $I-100 \times 100 \times 5$ and $I-140 \times 70 \times 5$, and all the I-sections were fabricated from the same batch of 5 mm thick S700MC high strength steel hot-rolled plates by gas metal arc welding. Overall, the

⁸² *2.1. General*

testing programme involved twelve in-plane four-point bending tests, with six performed about the major principal axes and another six conducted about the minor principal axes, together with the initial local geometric imperfection measurements of the beam specimens.

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93 2.2. Measurements on material properties and membrane residual stresses

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Prior to in-plane four-point bending tests, material testing was carried out to derive the material 95 stress-strain responses of the examined S690 high strength steel and measurements on 96 97 membrane residual stresses were conducted to determine their distributions and amplitudes in S690 high strength steel welded I-sections. The test rigs and procedures were fully reported in 98 Sun et al. [3], with only a brief summary provided herein. Two longitudinal coupons and two 99 100 transverse coupons were extracted from the same batch of S700MC plates as that used for fabricating the beam specimens, and tested utilising a Schenck 250 kN hydraulic testing 101 machine under displacement control, with the resulting strain rates being in conformity with 102 103 the specific requirements given in EN ISO 6892-1 [17]. Fig. 1 [3] shows the stress-strain curves measured from both the longitudinal and transverse coupons, while the key average measured 104 material properties, including the Young's modulus E, the yield stress f_y , the ultimate stress f_u , 105 the ultimate-to-yield stress ratio f_u/f_v , the strain at the ultimate stress ε_u and the fracture strain 106 ε_{f_2} are reported in Table 1. The membrane residual stress magnitudes and distributions in the 107 examined S690 high strength steel welded I-sections were measured by means of the sectioning 108 method, with the rig and procedures being in compliance with those recommended in Ziemian 109 [18]. On the basis of the experimental results, a new predictive model [3] was proposed 110

specifically for predicting the membrane residual stresses in S690 high strength steel welded
I-sections, with the distribution pattern shown in Fig. 2 and the amplitudes of the peak
membrane residual stresses presented in Table 2.

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115 2.3. Measurements on initial local geometric imperfections

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Initial geometric imperfections are primarily introduced into steel components during the 117 manufacturing process, and may result in premature failure of the steel components with low 118 119 load-carrying capacities and steep post-ultimate load-deformation responses. The focus of the present study is on the in-plane flexural (local buckling) behaviour of S690 high strength steel 120 welded I-section beams, and thus the initial local geometric imperfection of each specimen was 121 122 measured, based on the test rig shown in Fig. 3, where the specimen is clamped on the base table of a milling machine, whilst an LVDT is attached to the head of the milling machine and 123 moved along the centreline of each of the three constituent plates (i.e. one web and two flanges) 124 125 of the specimen to measure the local deviations [19]. It is worth noting that imperfection measurements were all carried out over the central 75% of the specimen lengths, in order to 126 eliminate the effect of flaring of specimen ends upon cutting. For each constituent plate element 127 of the S690 high strength steel welded I-section beam specimen, the maximum initial local 128 geometric imperfection amplitude was taken as the largest deviation from a linear regression 129 surface fitted to the corresponding measured data set [20–23], and presented in Table 3, where 130 $\omega_w, \omega_{f1}, \omega_{f2}$ are the measured maximum local imperfection amplitudes of the web and two 131 flanges, respectively, while the initial local geometric imperfection amplitude of the S690 high 132

strength steel welded I-section beam specimen ω_0 was taken as the maximum of ω_w , ω_{f1} and ω_{f2} .

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136 2.4. Four-point bending tests

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For each S690 high strength steel welded I-section, two four-point bending tests were 138 conducted about both the major and minor principal axes, to study the in-plane flexural 139 behaviour and bending moment resistances. The member lengths and cross-section geometric 140 141 sizes of the beam specimens were carefully measured, and presented in Table 3, where L is the specimen length, h is the outer section depth, b_f is the flange width and t is the wall thickness. 142 The four-point bending test procedures and setup conformed to those recommended in Ziemian 143 144 [18]. Displacement-controlled loading scheme was adopted to drive the actuator of an INSTRON 2000 kN hydraulic testing frame, with a constant speed of 2 mm/min. Fig. 4 shows 145 the setup for the four-point bending tests about the minor principal axes, where two pairs of 146 147 steel rollers are employed to provide the four-point bending configuration, with one pair located at a distance of 50 mm from the end sections of the beam specimen and the other pair placed 148 at third-points of the flexural span (i.e. the span between the two end rollers) of the beam 149 specimen, solid wooden blocks are inserted into the beam specimen at the two loading points 150 as well as the two supports, in order to avoid the occurrence of crippling failure of flanges, and 151 three string potentiometers are placed at the two loading points and mid-span to record the 152 respective vertical deflections. The four-point bending tests about the major principal axes were 153 performed using a similar test rig, as shown in Fig. 5, but with G-clamps vertically mounted 154

onto the spreader beam to act as lateral restraints for preventing any lateral or torsional
deformation of the beam specimens and eliminating the possibility of member lateral-torsional
buckling.

158

All the tested S690 high strength steel welded I-section beam specimens exhibited visible in-159 plane deformation and failed by local buckling; Fig. 6 and Fig. 7 depict the failure modes of 160 typical beam specimens I-100×100×5-MA (in major-axis bending) and I-100×100×5-MI (in 161 minor-axis bending), respectively. The key test results, obtained from the four-point bending 162 163 tests, are presented in Table 4, including the failure moment M_u , the ratios of M_u/M_{pl} and M_u/M_{el} , in which M_{pl} and M_{el} are the cross-section plastic and elastic moment resistances with respect 164 to the considered bending axis, and respectively calculated as the plastic (W_{pl}) and elastic (W_{el}) 165 166 section moduli multiplied by the material yield stress f_y , and the beam rotation capacity R [24– 26]. Figs 8 and 9 depict the normalised moment-curvature curves for the examined S690 high 167 strength steel welded I-section beam specimens in major-axis bending and in minor-axis 168 169 bending, respectively, where the curvature κ is calculated from Eq. (1), in which D_L and D_M are the corresponding vertical deflections at the loading points and at the mid-span, as measured 170 from the string potentiometers, and L_m is the distance between the two loading points. 171

172
$$\kappa = \frac{8(D_M - D_L)}{4(D_M - D_L)^2 + L_m^2}$$
(1)

- 174
- 175
- 176

177	3. Numerical investigation
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179	3.1. General
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181	In conjunction with the structural testing performed in Section 2, a numerical modelling study
182	was performed, utilising the nonlinear finite element (FE) software ABAQUS [27], and
183	reported in the present section. A numerical validation study was initially conducted to validate

the developed FE models against the obtained experimental results, followed by a parametric

study to derive additional numerical results on S690 high strength steel welded-I-section beams

186 over a wider spectrum of cross-section sizes.

187

188 *3.2. Development of finite element (FE) models*

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Having been successfully and widely utilised in previous numerical modelling of high strength 190 191 steel welded I-section members [3,28,29], the four-node shell element S4R [27] was also employed herein for simulating S690 high strength steel welded I-section beams. The element 192 size was selected upon a mesh sensitivity study examining a range of element sizes from 0.5t 193 to 3t; it was generally found that an element size equal to the material thickness t led to accurate 194 incorporation of the membrane residual stresses into the FE models and also resulted in both 195 precise numerical results and adequate computational efficiency, and was thus assigned to each 196 beam FE model. The stress-strain curves, measured from the longitudinal coupons, were firstly 197 converted into the true stress-true plastic strain curves and then inputted into ABAQUS [27]. 198

The membrane residual stress distributions and amplitudes, as derived from the proposed predictive model [3] (see Section 2.2), were incorporated into the beam FE models through the '*INITIAL CONDITIONS' command [27]; Fig. 10 displays a typical membrane residual stress pattern incorporated into the FE models for the beam specimens I-100×100×5-MA and I-100×100×5-MI.

204

For the ease of setting boundary conditions, each of the two sections of the beam FE models at 205 the end supports was coupled to a reference point, positioned at the bottom web-to-flange 206 207 junction for major-axis bending or at the mid-point between the two bottom flange tips for minor-axis bending. In order to replicate the simply-supported boundary condition used in the 208 testing, one reference point was allowed to translate longitudinally and rotate about the axis of 209 210 bending while the other one was only allowed for rotation about the same bending axis. Besides, the cross-section at each loading point was also coupled to a reference point, which was located 211 at the top web-to-flange junction for major-axis bending or at the mid-point between the two 212 213 top flange tips for minor-axis bending, and allowed to have translations along both the longitudinal and vertical directions and rotation about the axis of bending, to mimic the four-214 point bending configuration. With regards to the modelling of beams bent about the major 215 principal axes, additional lateral and torsional restraints were applied to those cross-sections 216 that were restrained by G-clamps in the testing, to eliminate the possibility of lateral-torsional 217 buckling. 218

219

220 Initial local geometric imperfections were incorporated into the S690 high strength steel

welded I-section beam FE models, with the distribution patterns taken as the lowest elastic buckling mode shapes in four-point bending and derived from a prior elastic eigenvalue buckling analysis [30–35]. Four initial local imperfection amplitudes, including the measured imperfection value ω_0 and 1/10, 1/30 and 1/100 of material thickness *t*, were then used to factor the derived imperfection patterns, enabling the sensitivity of the established S690 high strength steel weld I-section beam FE models to imperfection amplitudes to be evaluated.

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228 *3.3. Validation of finite element models*

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Upon establishment of the S690 high strength steel welded I-section beam FE models, 230 nonlinear static Riks analysis [27] was conducted to determine the numerical ultimate bending 231 232 moments, moment-curvature responses and failure modes. Based on the comparisons of the numerical results against their experimental counterparts, the accuracy of the established beam 233 FE models was evaluated. The FE to experimental ultimate moment ratios for the tested S690 234 235 high strength steel welded I-section beam specimens are reported in Table 5, in which the results generally indicate that all the four adopted initial local geometric imperfection 236 amplitudes yield precise and consistent predictions of the experimental failure moments, with 237 the best agreement obtained when the local imperfection amplitude equal to 1/100 of the 238 material thickness was used in the numerical simulation. Figs 6 and 7 depict the comparisons 239 between the experimental and numerical local buckling failure modes for typical beam 240 specimens I-100×100×5-MA and I-100×100×5-MI subjected to major-axis bending and minor-241 axis bending, respectively, indicating excellent agreement. The experimentally and numerically 242

derived normalised moment-curvature responses for a typical beam specimen I-140×70×5-MA 243 in major-axis bending are compared in Fig. 11, while a similar graphic comparison is shown in 244 Fig. 12 for a typical beam specimen $I-100 \times 100 \times 5$ -MI in minor-axis bending, both revealing 245 that the established beam FE models are capable of replicating the full experimental normalised 246 moment-curvature histories. Moreover, the normalised numerical moment-curvature curves 247 were also derived from the beam FE models without inclusion of membrane residual stresses 248 and shown in Figs 11 and 12; the normalised numerical moment-curvature responses with and 249 without membrane residual stresses were observed to almost coincide, revealing that the effect 250 251 of membrane residual stresses on the in-plane bending behaviour of S690 high strength steel welded I-section beams is negligible, as also highlighted in previous similar numerical studies 252 [33,35]. In sum, the developed beam finite element models have been proven to be capable of 253 254 precisely simulating the four-point bending tests on S690 high strength steel welded I-section beams. 255

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257 *3.4. Parametric studies*

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On the basis of the beam FE models established and validated in Section 3.3, parametric studies were performed to derive additional numerical data beyond those derived from the experiments. In the present parametric studies, the material stress–strain responses measured from the longitudinal coupons were employed, while the incorporated initial local imperfection amplitudes were selected as t/100. The flexural spans of all the numerically modelled I-section beams were equal to 1500 mm, whilst the two loading points were positioned at third-points of

265	the flexural spans. Regarding the cross-section sizes of the modelled I-section beams, the outer
266	depths were fixed at 150 mm, with the flange widths taken as 75 mm, 100 mm and 150 mm,
267	respectively, resulting in a range of cross-section aspect ratios being considered; the thicknesses
268	of the web and flanges of each modelled I-section were set to be equal and varied between 2
269	mm and 15 mm, which led to a broad spectrum of cross-section geometric sizes being examined.
270	In total, 185 and 101 numerical data on S690 high strength steel welded I-section beams under
271	major-axis and minor-axis bending were respectively generated through parametric studies.
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273	4. Assessment of existing international design codes
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275	4.1. General
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277	In the present section, the beam test results, obtained in Section 2, together with the numerical
278	data, acquired in Section 3, were used to evaluate the accuracy of the slenderness limits and
279	design rules for S690 high strength steel welded I-section beams susceptible to in-plane
280	bending failure, as specified in the existing European code EN 1993-1-12 [14], Australian
281	standard AS 4100 [15] and American Specification ANSI/AISC 360-16 [16]. The unfactored
282	design cross-section bending moment resistances ($M_{u,EC3}$, $M_{u,AS}$ and $M_{u,AISC}$) were firstly
283	calculated in accordance with the three considered design codes and afterwards compared
284	against the test (and numerical) ultimate bending moments, with the mean test (or numerical)
285	to predicted ultimate bending moment ratio $(M_u/M_{u,EC3}, M_u/M_{u,AS} \text{ or } M_u/M_{u,AISC})$ for each design
286	code given in Table 6.

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288 *4.2. European code EN 1993-1-12 (EC3)*

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290 *4.2.1. General*

291

The current Eurocode EN 1993-1-12 [14] was developed specifically for high strength steels 292 with grades greater than S460 up to S700, though mirroring most of the design provisions given 293 in EN 1993-1-1 [36] for normal strength mild steels. Regarding the design of S690 high 294 295 strength steel welded I-sections subjected to bending, EN 1993-1-12 [14] adopts the same concept of cross-section classification (i.e. the strength of the cross-section is dependent on the 296 class of the cross-section) as that utilised in EN 1993-1-1 [36]. Four cross-section classes were 297 298 specified in the Eurocodes [14,36]: Class 1 and 2 (plastic) sections in bending can achieve the plastic moment capacities (M_{pl}) , Class 3 (elastic) sections subject to bending are capable of 299 attaining the elastic moment capacities (M_{el}) , and Class 4 (slender) sections fail before the 300 301 material yield stresses f_y are attained, with the design bending moment resistances limited to the effective moment capacities (M_{eff}) . To determine the class of a welded I-section in bending, 302 all of its constituent plate elements (i.e. outstand flanges and internal web) are firstly classified 303 through comparisons of the respective flat width-to-thickness ratios (c_w/t and c_d/t , in which c_w 304 and c_f are respectively the flat widths of the web and flange) against the slenderness limits 305 specified in the Eurocodes [14,36], and the class of the most slender plate element is then 306 defined as the overall class of the examined I-section. The EC3 Class 3 and Class 2 slenderness 307 limits for classifying internal and outstand plate elements under various loading conditions (i.e. 308

compression, bending and compressive stress gradients) are listed in Table 7(a), where ε_{EC3} = $\sqrt{235/f_y}$ is the EC3 material parameter to consider the effect of material strength on the plate element slenderness limits, and k_{σ} is the buckling factor and dependent on the stress distribution and boundary condition of the plate element. In the following sub-section 4.2.2 and sub-section 4.2.3, the accuracy of the EN 1993-1-12 slenderness limits and design bending moment capacities were respectively evaluated.

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- 316 *4.2.2. Cross-section classification limits*
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The Class 3 slenderness limits for outstand plate elements in compression and internal plate 318 elements in bending were assessed based on the experimental and FE data on S690 high 319 320 strength steel welded I-section beams bent about the major principal axes, with the results of the graphic assessments respectively depicted in Fig. 13 and Fig. 14, where the test and 321 numerical ultimate bending moments, normalised by the cross-section elastic moment 322 resistances, are plotted against the $c_{f}/(t\epsilon_{EC3})$ and $c_{w}/(t\epsilon_{EC3})$ ratios of the examined S690 high 323 strength steel welded I-sections, together with the EC3 Class 3 slenderness limits (normalised 324 by ε_{EC3}) for outstand plate elements in compression $c_f/(t\varepsilon_{EC3})=14$ and internal plate elements in 325 bending $c_w/(t\varepsilon_{EC3})=124$. It was generally found that the established Class 3 slenderness limits 326 in EN 1993-1-12 [14] are safe but conservative when used for the classification of internal 327 webs (in bending) and outstand flanges (in compression) of S690 high strength steel welded I-328 sections subjected to major-axis bending. The ultimate bending moment resistances, derived 329 from the structural testing and finite element modelling on S690 high strength steel welded I-330

section beams in minor-axis bending, were then utilised to assess the accuracy of the current EC3 Class 3 slenderness limit for outstand plate elements under triangular compressive stress gradients ($c_{f}/(t\epsilon_{EC3})=21k_{\sigma}^{0.5}$, in which $k_{\sigma}=0.57$) in Fig. 15. The results of the assessments generally revealed that the EC3 Class 3 slenderness limit for outstand plate elements under triangular compressive stress gradients is rather conservative though safe when used for the classification of outstand flanges of S690 high strength steel welded I-section beams in minoraxis bending.

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339 A similar graphic evaluation was also performed on the established EC3 Class 2 slenderness limit for internal plate elements in bending ($c_w/(t\varepsilon_{EC3})=83$), based on the test and numerical data 340 on S690 high strength steel welded I-section beams under major-axis bending, as given in Fig. 341 342 16. The EC3 Class 2 slenderness limits for outstand plate elements in compression $(c_{f}/(t\varepsilon_{EC3})=10)$ was evaluated, based on the derived experimental and FE data on S690 high 343 strength steel welded I-section beams bent about both the major and minor principal axes, as 344 345 depicted in Fig. 17. The results of the graphic evaluations in Figs 16 and 17 generally revealed that the Class 2 slenderness limits established in EN 1993-1-12 [14] are safe and accurate when 346 used for the classifications of internal webs (in bending) and outstand flanges (in compression) 347 of S690 welded I-section beams. 348

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4.2.3. EC3 Cross-section bending moment resistance predictions

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welded I-section beams were assessed through comparisons against the obtained test and FE 353 ultimate bending moments. The current EN 1993-1-12 [14] prescribes the use of cross-section 354 plastic (M_{pl}) and elastic (M_{el}) moment capacities as the design bending moment capacities for 355 Class 1 (and 2) and Class 3 sections, respectively, and adopts the effective width method to 356 predict the cross-section bending moment resistances for those slender Class 4 sections. The 357 effective width method makes due allowance for loss of effectiveness owing to local buckling 358 by reducing the flat widths of the slender constituent outstand and internal plate elements. The 359 effective (reduced) widths ceff of slender flanges (outstand elements) and webs (internal 360 elements) of I-sections can be respectively calculated from Eq. (2) and Eq. (3) [37], in which 361 $\overline{\lambda}_p$ is the slenderness of the plate element, as defined by Eq. (4), where k_{σ} is the buckling 362 factor, dependent on the type of the plate element and stress distribution throughout plate width, 363 and can be calculated in accordance with Tables 4.1 and 4.2 of EN 1993-1-5 [37]. Upon 364 calculation of the effective widths of all the slender plate elements of the Class 4 welded I-365 section, the EC3 effective section modulus ($W_{eff,EC3}$) and effective bending moment capacity 366 $(M_{eff,EC3} = W_{eff,EC3}f_v)$ can then be derived; it is worth noting that cumbersome iterations may be 367 involved in the calculation of $W_{eff,EC3}$ due to the shift in effective neutral axis along with each 368 round of calculation. 369

370
$$c_{eff} = c_f \left(\frac{1}{\overline{\lambda}_p} - \frac{0.188}{\overline{\lambda}_p^2} \right) \le c_f$$
(2)

$$c_{eff} = c_w \left(\frac{1}{\overline{\lambda}_p} - \frac{0.22}{\overline{\lambda}_p^2} \right) \le c_w$$
(3)

$$\overline{\lambda}_{p} = \frac{c/t}{28.4\varepsilon_{EC3}\sqrt{k_{\sigma}}}$$
(4)

373

The ratios of the test and FE ultimate bending moments to the EC3 cross-section bending 374 moment resistance predictions are plotted against the c_{f}/t ratios of the flanges of the examined 375 I-sections, and depicted in Fig. 18, while Table 6(a) presents the mean experimental (and 376 numerical) to EC3 design cross-section bending capacity ratios $M_u/M_{u,EC3}$, together with the 377 corresponding coefficients of variation (COVs), for different classes of S690 welded I-sections 378 in bending. The results of both the graphic and numerical comparisons revealed that the cross-379 section bending moment resistances are well predicted by the current EN 1993-1-12 [14] for 380 Class 1 (and Class 2) S690 high strength steel welded I-section beams bent about both the 381 382 principal axes and Class 3 S690 high strength steel welded I-section beams in major-axis bending, while EN 1993-1-12 [14] yields overly conservative bending moment capacity 383 predications for Class 3 S690 high strength steel welded I-section beams bent about the minor 384 385 principal axes and Class 4 S690 high strength steel welded I-section beams in both major-axis bending and minor-axis bending. 386

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388 *4.3. Australian Standard AS 4100*

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The current Australian standard AS 4100 [15], which provides design provisions for both normal strength mild steels and high strength steels with grades up to S690, also employs the cross-section classification framework for the design of welded I-section beams failing by local buckling. Through comparisons of the flat width-to-thickness ratios against the slenderness limits for all the constituent plate elements, cross-sections in bending are classified as compact, non-compact and slender sections in AS 4100 [15], corresponding to Class 1 (and 2), Class 3,

and Class 4 sections defined in EN 1993-1-12 [14]. Note that the AS 4100 slenderness limits 396 between non-compact and compact plate elements and between slender and non-compact plate 397 elements are respectively termed as the plasticity and yield slenderness limits (corresponding 398 to the EC3 Class 2 and Class 3 slenderness limits), as presented in Table 7(b), where ε_{AS} = 399 $\sqrt{250/f_y}$ is the AS material parameter. Graphic evaluation of the AS yield slenderness limits 400 for outstand elements in compression ($c_{f}/(t\epsilon_{AS})=14$), internal elements in bending ($c_{w}/(t\epsilon_{AS})=115$) 401 and outstand elements in triangular compressive stress gradients ($c_{t/t}(t_{EAS})=22$) as well as the 402 AS plasticity slenderness limits for internal elements in bending $(c_w/(t\epsilon_{AS})=82)$ and outstand 403 elements in compression ($c_{f}/(t\epsilon_{AS})=8$) was carried out based on the relevant test and FE data, 404 and shown in Figs 19-23, respectively. The results of the graphic evaluations generally 405 indicated that the current AS yield limits are safe but considerably conservative when used for 406 407 the classification of both internal webs and outstand flanges of S690 high strength steel welded I-section beams, while the plasticity slenderness limits yield a good level of accuracy in the 408 plate element classification. 409

410

The current AS 4100 [15] adopts M_{pl} as the design bending moment resistances for compact welded I-section beams, but with an upper limit of $1.5M_{el}$, as given by Eq. (5), and takes into due account partial plasticity in the predictions of cross-section bending moment resistances for non-compact welded I-section beams, with the design formulation shown by Eq. (6), where M_c is taken as the minimum of M_{pl} and $1.5M_{el}$ of the examined non-compact I-section, λ_s is equal to the c/t ratio of the most slender constituent plate element of the non-compact I-section in bending; note that the most slender constituent plate element is defined as the element with

the greatest plate element c/t to yield slenderness limit (see Table 7(b)) ratio, and λ_{sy} and λ_{sp} are 418 the corresponding yield and plasticity limits for the most slender constituent plate element and 419 presented in Table 7(b). Regarding slender welded I-section beams, the effective bending 420 moment resistances, specified in AS 4100 [15], are determined through multiplying the cross-421 section elastic moment capacities M_{el} by the reduction factor ρ , as given by Eq. (7); note that 422 the reduction factor ρ is calculated as (λ_{sv}/λ_s) and $(\lambda_{sv}/\lambda_s)^2$ for welded I-sections with the most 423 slender plate element being subjected to uniform compression (i.e. major-axis bending case) 424 and stress gradients (i.e. minor-axis bending case), respectively. 425

$$M_{u,AS} = M_{pl} \le 1.5 M_{el} \tag{5}$$

426

$$M_{u,AS} = M_{el} + (M_c - M_{el}) \left(\frac{\lambda_{sy} - \lambda_s}{\lambda_{sy} - \lambda_{sp}} \right)$$
(6)

428

$$M_{u,AS} = \rho M_{el} \tag{7}$$

429

The accuracy of the current Australian standard AS 4100 [15] for the design of S690 high 430 strength steel welded I-section beams failing by local buckling was assessed by comparing the 431 obtained experimental and FE ultimate bending moments with the AS predicted cross-section 432 bending moment capacities. As evident in Fig. 24 and Table 6(b), the current AS 4100 [15] 433 yields accurate and consistent cross-section bending moment capacity predictions for compact 434 S690 high strength steel welded I-section beams in both major-axis bending and minor-axis 435 bending and non-compact S690 high strength steel welded I-section beams subjected to major-436 axis bending, but excessively under-estimates the cross-section bending moment resistances 437 for non-compact S690 welded I-section beams bent about the minor principal axes and slender 438 S690 high strength steel welded I-section beams in both major-axis and minor-axis bending. 439

440

441 *4.4. American specification ANSI/AISC 360-16*

442

The existing American specification ANSI/AISC 360-16 [16], with the scope of application 443 covering steels with grades up to S690, also adopts the cross-section classification framework 444 for the design of welded I-section beams prone to local instability. Through comparisons of the 445 flat width-to-thickness ratios against the corresponding slenderness limits for all the constituent 446 plate elements, the existing ANSI/AISC 360-16 [16] classifies cross-sections subjected to 447 bending as slender, non-compact and compact sections, similar to the current AS 4100 [15]; 448 note that the flat element widths of flanges of I-shaped sections are given as half of the full 449 flange widths in ANSI/AISC 360-16 [16], while the flat element widths of webs are defined as 450 451 the clear distances between the flanges. The American specification ANSI/AISC 360-16 [16] terms the slenderness limits for slender/non-compact and non-compact/compact plate elements 452 as non-compact and compact limiting width-to-thickness ratios, as listed in Table 7(c), where 453 $\varepsilon_{AISC} = \sqrt{E/f_y}$ is the AISC material parameter and $k_c = 4\sqrt{t/c_w}$ is a geometric parameter to 454 account for the influence of the size of the internal web on the slenderness limit of the outstand 455 flange. The test and FE numerical results on S690 welded I-section beams were adopted to 456 evaluate the accuracy of the AISC non-compact limiting width-to-thickness ratios for outstand 457 elements in compression ($c_{\#}(t_{\varepsilon_{AISC}}k_c^{0.5})=1.14$), internal elements in bending ($c_{\#}/(t_{\varepsilon_{AISC}})=5.7$) 458 and outstand elements in triangular compressive stress gradients ($c_{f}/(t \epsilon_{AISC})=1.0$) as well as the 459 compact limiting width-to-thickness ratios for internal elements in bending ($c_w/(t\epsilon_{AISC})=3.76$) 460 and outstand elements in compression ($c_f/(t\epsilon_{AISC})=0.38$), with the results of the respective 461

graphic assessments shown in Figs 25–29. It was found that that all the AISC limiting widthto-thickness ratios are safe and generally accurate when used for the classification of plate elements of S690 high strength steel welded I-section beams except for the non-compact limiting width-to-thickness ratios for outstand elements in compression ($c_f/(t\epsilon_{AISC}k_c^{0.5})=1.14$), which results in unsafe plate element classification.

With regards to welded I-section beams bent about the cross-section major principal axes, 468 ANSI/AISC 360-16 [16] prescribes the use of plastic moment resistances (M_{pl}) as the design 469 470 bending moment resistances for both compact I-sections and non-compact I-sections with compact outstand flanges and non-compact internal webs, and takes into account partial 471 plasticity in the predictions of bending moment resistances for non-compact I-sections with 472 473 non-compact outstand flanges and compact or non-compact internal webs, as given by Eq. (8), where λ_{pf} and λ_{rf} are the compact and non-compact limiting width-to-thickness ratios for 474 outstand flanges under compression, respectively, as listed in Table 7(c). The AISC design 475 cross-section effective (reduced) bending moment capacities for slender I-section beams with 476 (i) slender webs and compact flanges, (ii) slender webs and non-compact flanges and (iii) 477 slender flanges are calculated from Eqs (9)-(11), respectively. Regarding welded I-section 478 beams subjected to minor-axis bending, the current ANSI/AISC 360-16 [16] specifies the 479 design cross-section bending moment resistances as the minimum of M_{pl} and $1.6M_{el}$ for 480 compact I-sections, while the design cross-section bending moment resistances of non-compact 481 and slender I-sections are determined according to Eqs (8) and (12), respectively. 482

483
$$M_{u,AISC} = M_{pl} - \left(M_{pl} - 0.7M_{el}\right) \left(\frac{c_f / t - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}}\right)$$
(8)

484
$$M_{u,AISC} = M_{eff,AISC} = M_{el} \left[1 - \frac{c_w / (2c_f)}{1200 + 300(c_w / (2c_f))} (c_w / t - 5.7\varepsilon_{AISC}) \right] \le M_{el}$$
(9)

485
$$M_{u,AISC} = M_{eff,AISC} = M_{el} \left[1 - 0.3 \left(\frac{c_f / t - \lambda_{pf}}{\lambda_{rf} - \lambda_{pf}} \right) \right] \le M_{el}$$
(10)

486
$$M_{u,AISC} = M_{eff,AISC} = M_{el} \frac{0.9k_c}{\left(c_f / t\varepsilon_{AISC}\right)^2} \le M_{el}$$
(11)

487
$$M_{u,AISC} = M_{eff,AISC} = M_{el} \frac{0.69}{\left(c_f / t\varepsilon_{AISC}\right)^2} \le M_{el}$$
(12)

488

Graphic and quantitative evaluations of the AISC design cross-section bending moment 489 capacities were carried out based on the experimental (and FE) ultimate bending moments of 490 the examined S690 high strength steel welded I-section beams, with the results shown in Fig. 491 30 and Table 6(c), respectively. It is evident that the test and FE ultimate bending moments of 492 compact S690 high strength steel welded I-section beams (in bending about both the principal 493 axes) and non-compact S690 high strength steel welded I-section beams bent about the major 494 principal axes are well predicted by the current ANSI/AISC 360-16 [16], while the design 495 cross-section bending moment capacity predictions of non-compact S690 high strength steel 496 welded I-section beams in minor-axis bending and slender S690 high strength steel welded I-497 498 section beams in both minor-axis and major-axis bending, determined from ANSI/AISC 360-16 [16], are excessively conservative and scattered. 499

501 **5. Conclusions**

502

A testing and numerical modelling investigation into the in-plane flexural behaviour and 503 bending moment resistances of welded I-section beams made of grade S690 high strength steel 504 has been conducted and described in this paper. The experimental programme was conducted 505 on six different S690 high strength steel welded I-sections, and involved initial geometric 506 imperfection measurements, six four-point bending tests about the major principal axes and six 507 four-point bending tests about the minor principal axes. In parallel with the structural testing, 508 a finite element simulation study was performed, including a validation study to replicate the 509 four-point bending tests on S690 high strength steel welded I-section beams and a parametric 510 sturdy to derive additional finite element data. The obtained test and finite element results were 511 512 adopted to assess the accuracy of the slenderness limits for the classifications of internal webs and outstand flanges of S690 high strength steel welded I-sections in bending as well as the 513 local buckling design provisions for S690 high strength steel welded I-section beams, as 514 specified in 1993-1-12 [14], AS 4100 [15] and ANSI/AISC 360-16 [16]. The assessment results 515 generally indicated that (i) all the established codified slenderness limits are safe for the 516 classifications of plate elements and cross-sections of S690 high strength steel welded I-section 517 beams, with an exception being the AISC non-compact limiting width-to-thickness ratio for 518 outstand elements in compression, and (ii) the codified local buckling design rules in all the 519 three design standards [14-16] were shown to yield precise and consistent cross-section 520 bending moment capacity predictions for compact (Class 1 and 2) S690 welded I-section beams 521 in bending about both the principal axes and non-compact (Class 3) S690 welded I-sections 522

523	bent about the major principal axes, while the predicted cross-section bending resistances,
524	determined from all the three design standards [14-16], were unduly conservative for non-
525	compact (Class 3) S690 welded I-sections in minor-axis bending and slender (Class 4) S690
526	welded I-section beams in both major-axis and minor-axis bending.
527	
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529	
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537 538 539 540	References [1] K.J.R. Rasmussen, G.J. Hancock, Plate slenderness limits for high strength steel sections, J. Constr. Steel Res. 23 (1–3) (1992) 73–96. [2] G. Shi, W. Zhou, Y. Bai, C. Lin, Local buckling of 460 MPa high strength steel welded
537 538 539 540 541	 References [1] K.J.R. Rasmussen, G.J. Hancock, Plate slenderness limits for high strength steel sections, J. Constr. Steel Res. 23 (1–3) (1992) 73–96. [2] G. Shi, W. Zhou, Y. Bai, C. Lin, Local buckling of 460 MPa high strength steel welded section stub columns under axial compression, J. Constr. Steel Res. 100 (2014) 60–70.
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530 537 538 539 540 541 542 543	 References [1] K.J.R. Rasmussen, G.J. Hancock, Plate slenderness limits for high strength steel sections, J. Constr. Steel Res. 23 (1–3) (1992) 73–96. [2] G. Shi, W. Zhou, Y. Bai, C. Lin, Local buckling of 460 MPa high strength steel welded section stub columns under axial compression, J. Constr. Steel Res. 100 (2014) 60–70. [3] Y. Sun, Y. Liang, O. Zhao, Testing, numerical modelling and design of S690 high strength steel welded I-section stub columns, J. Constr. Steel Res. 159 (2019) 521–533.

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Direction	Ε	f_y	f_u		\mathcal{E}_{u}	\mathcal{E}_{f}		f_u/f_y	
	(GPa)	(MPa)	(M	Pa)	(%)	(%	6)		
Longitudinal	216	702.6	750).3	11	24	ŀ	1.07	
Transverse	202	701.8	765	5.6	10	24	ŀ	1.09	
Table 2									
Membrane res	idual stress predi	ictive model p	proposed for	or S690 w	elded I-se	ctions [3].			
Peak tensile re	sidual stress F	Peak compress	sive residu	al stress	a	h	C	d	
$(f_{wt} \text{ or } f_{ft})$	($f_{wc} ext{ or } f_{fc}$			u	υ	t	u	
$0.8 f_y$	F	From equilibri	ium		0.225	$5b_f = 0.1$	$5b_f 0.07$	$5h_w = 0.22$	$25h_w$
Table 2						5			
Table 3 Measured geometric	c properties of th	ne tested hear	n specimer	15		<u>,</u>	~		
Table 3 Measured geometri Specimen ID	c properties of the Axis of bendir	ne tested beam	n specimer	ns.	t	<i>O</i> hr	<i>Wa</i>	00	00
Table 3 Measured geometri Specimen ID	c properties of th Axis of bendir	ne tested beam ng L (mm)	n specimer h (mm)	b_f (mm)	t (mm)	 ω _w (mm)	ω _ſ ι (mm)	ω _{f2} (mm)	ω ₀ (mi
Table 3 Measured geometri Specimen ID I-50×50×5-MA	c properties of th Axis of bendir	ne tested beaming L (mm) 495 7	n specimer h (mm) 49 44	15. bf (mm) 49.42	t (mm) 4 97	ω_w (mm) 0.04	ω ₁ (mm)	ω _{f2} (mm) 0.08	ω ₀ (mi
Table 3Measured geometriSpecimen IDI-50×50×5-MAI-70×70×5-MA	c properties of th Axis of bendir	ne tested beam ng <i>L</i> (mm) 495.7 696.5	n specimer h (mm) 49.44 67.15	ns. <i>b</i> f (mm) 49.42 69.29	<i>t</i> (mm) 4.97 4.93	ω_w (mm) 0.04 0.06	ω _{f1} (mm) 0.13 0.08	ω_{f2} (mm) 0.08 0.08	ω ₀ (mi 0.1
Table 3Measured geometriSpecimen IDI-50×50×5-MAI-70×70×5-MAI-80×60×5-MA	c properties of th Axis of bendir Maior axis	ne tested beam ng <i>L</i> (mm) 495.7 696.5 693.7	n specimer h (mm) 49.44 67.15 79.39	ns. bf (mm) 49.42 69.29 59.01	t (mm) 4.97 4.93 4.96	ω _w (mm) 0.04 0.06 0.03	ω _f 1 (mm) 0.13 0.08 0.14	ω _{f2} (mm) 0.08 0.08 0.11	ω ₀ (mr 0.1) 0.0
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA	c properties of th Axis of bendir Major axis	ne tested beam ng <i>L</i> (mm) 495.7 696.5 693.7 698.1	n specimer h (mm) 49.44 67.15 79.39 90.35	ns. <i>b</i> _f (mm) 49.42 69.29 59.01 69.20	t (mm) 4.97 4.93 4.96 4.93	ω_w (mm) 0.04 0.06 0.03 0.06	ω _{f1} (mm) 0.13 0.08 0.14 0.11	ω _{f2} (mm) 0.08 0.11 0.10	ω ₀ (mr 0.1) 0.00 0.14 0.1
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA	c properties of th Axis of bendir Major axis	ne tested beam ng <i>L</i> (mm) 495.7 696.5 693.7 698.1 998.5	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02	ns. bf (mm) 49.42 69.29 59.01 69.20 99.09	<i>t</i> (mm) 4.97 4.93 4.96 4.93 4.91	ω _w (mm) 0.04 0.06 0.03 0.06 0.05	ω _{/1} (mm) 0.13 0.08 0.14 0.11 0.15	ω _{f2} (mm) 0.08 0.08 0.11 0.10 0.13	ω ₀ (mr 0.1) 0.0) 0.1 0.1
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA I-140×70×5-MA	c properties of th Axis of bendir Major axis	ne tested beam ng <i>L</i> (mm) 495.7 696.5 693.7 698.1 998.5 1397.3	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02 139.33	ns. <i>b</i> _f (mm) 49.42 69.29 59.01 69.20 99.09 69.23	t (mm) 4.97 4.93 4.96 4.93 4.91 4.94	ω _w (mm) 0.04 0.06 0.03 0.06 0.05 0.04	<i>ω</i> _{f1} (mm) 0.13 0.08 0.14 0.11 0.15 0.09	ω _{f2} (mm) 0.08 0.11 0.10 0.13 0.08	ω_0 (mi 0.1) 0.0 0.1 0.1 0.1 0.1
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA I-140×70×5-MA I-50×50×5-MI	c properties of th Axis of bendir Major axis	ne tested beam ng L (mm) 495.7 696.5 693.7 698.1 998.5 1397.3 497.5	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02 139.33 49.41	ns. <i>b</i> _f (mm) 49.42 69.29 59.01 69.20 99.09 69.23 49.59	t (mm) 4.97 4.93 4.96 4.93 4.91 4.94 4.99	ω_w (mm) 0.04 0.06 0.03 0.06 0.05 0.04 0.04	<i>ω</i> _{<i>f</i>1} (mm) 0.13 0.08 0.14 0.11 0.15 0.09 0.09	ω _{f2} (mm) 0.08 0.08 0.11 0.10 0.13 0.08 0.10	ω ₀ (mi 0.1 0.1 0.1 0.1 0.1 0.1
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA I-140×70×5-MA I-50×50×5-MI I-50×50×5-MI	c properties of th Axis of bendir Major axis	ne tested beam ng <i>L</i> (mm) 495.7 696.5 693.7 698.1 998.5 1397.3 497.5 874.0	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02 139.33 49.41 68.62	ns. bf (mm) 49.42 69.29 59.01 69.20 99.09 69.23 49.59 69.28	t (mm) 4.97 4.93 4.96 4.93 4.91 4.94 4.99 4.97	ω_w (mm) 0.04 0.06 0.03 0.06 0.05 0.04 0.04 0.04 0.07	<i>ω</i> _Л (mm) 0.13 0.08 0.14 0.11 0.15 0.09 0.09 0.12	ω _{f2} (mm) 0.08 0.11 0.10 0.13 0.08 0.10 0.07	ω_0 (mi 0.1, 0.0 0.1, 0.1, 0.1, 0.1, 0.1, 0.1,
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA I-140×70×5-MA I-50×50×5-MI I-50×50×5-MI I-50×50×5-MI I-50×50×5-MI I-80×60×5-MI	c properties of th Axis of bendir Major axis Minor axis	ne tested beam ng L (mm) 495.7 696.5 693.7 698.1 998.5 1397.3 497.5 874.0 696.0	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02 139.33 49.41 68.62 79.63	ns. <i>b</i> _f (mm) 49.42 69.29 59.01 69.20 99.09 69.23 49.59 69.28 59.16	t (mm) 4.97 4.93 4.96 4.93 4.91 4.94 4.94 4.99 4.97 4.90	ω_w (mm) 0.04 0.06 0.03 0.06 0.05 0.04 0.04 0.07 0.06	<i>ω</i> _{f1} (mm) 0.13 0.08 0.14 0.11 0.15 0.09 0.09 0.12 0.13	<i>ω_f</i> 2 (mm) 0.08 0.08 0.11 0.10 0.13 0.08 0.10 0.07 0.13	<i>ω</i> ₀ (mi 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA I-100×50×5-MI I-50×50×5-MI I-70×70×5-MI I-50×50×5-MI I-90×70×5-MI I-90×70×5-MI I-90×70×5-MI I-90×70×5-MI	Axis of bendir Major axis	ne tested beam ng L (mm) 495.7 696.5 693.7 698.1 998.5 1397.3 497.5 874.0 696.0 756.0	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02 139.33 49.41 68.62 79.63 90.35	ns. <i>b</i> _f (mm) 49.42 69.29 59.01 69.20 99.09 69.23 49.59 69.28 59.16 69.12	t (mm) 4.97 4.93 4.96 4.93 4.91 4.94 4.99 4.97 4.90 4.93	<i>ω</i> _w (mm) 0.04 0.06 0.03 0.06 0.05 0.04 0.04 0.04 0.07 0.06 0.06	<i>ω</i> _Л (mm) 0.13 0.08 0.14 0.11 0.15 0.09 0.09 0.12 0.13 0.09	<i>ω</i> _{f2} (mm) 0.08 0.11 0.10 0.13 0.08 0.10 0.07 0.13 0.13	<i>ω</i> ₀ (mr 0.1: 0.1: 0.1: 0.1: 0.1: 0.1: 0.1: 0.1:
Table 3 Measured geometri Specimen ID I-50×50×5-MA I-70×70×5-MA I-80×60×5-MA I-90×70×5-MA I-100×100×5-MA I-140×70×5-MI I-50×50×5-MI I-50×50×5-MI I-90×70×5-MI I-90×70×5-MI I-80×60×5-MI I-90×70×5-MI I-90×70×5-MI I-90×70×5-MI I-100×100×5-MI	c properties of th Axis of bendir Major axis Minor axis	ne tested beam ng L (mm) 495.7 696.5 693.7 698.1 998.5 1397.3 497.5 874.0 696.0 756.0 996.5	n specimer h (mm) 49.44 67.15 79.39 90.35 99.02 139.33 49.41 68.62 79.63 90.35 99.31	bs. b_f (mm) 49.42 69.29 59.01 69.20 99.09 69.23 49.59 69.28 59.16 69.12 99.48	t (mm) 4.97 4.93 4.96 4.93 4.91 4.94 4.94 4.99 4.97 4.90 4.93 4.98	<i>ω_w</i> (mm) 0.04 0.06 0.03 0.06 0.05 0.04 0.04 0.07 0.06 0.06 0.06 0.05	<i>ω</i> _{f1} (mm) 0.13 0.08 0.14 0.11 0.15 0.09 0.12 0.13 0.09 0.15	<i>ω_f</i> 2 (mm) 0.08 0.08 0.11 0.10 0.13 0.08 0.10 0.07 0.13 0.13 0.13	<i>ω</i> ₀ (mi 0.1 0.0 0.1 0.1 0.1 0.1 0.1 0.1 0.1

Table 4

	1				
Specimen ID	Bending axis	M_u (kNm)	M_u/M_{pl}	M_u/M_{el}	R
I-50×50×5-MA		10.0	1.10	1.30	>1.61
I-70×70×5-MA		19.4	1.09	1.25	>4.04
I-80×60×5-MA	Maionauia	21.0	1.07	1.24	>2.41
I-90×70×5-MA	Major axis	27.7	1.07	1.22	2.68
I-100×100×5-MA		39.8	1.02	1.15	1.48
I-140×70×5-MA		49.5	1.06	1.24	2.78
I-50×50×5-MI		5.0	1.11	1.73	>4.15
I-70×70×5-MI		9.3	1.08	1.66	>6.13
I-80×60×5-MI	Minonovia	6.8	1.08	1.69	>6.16
I-90×70×5-MI	Willior axis	9.2	1.07	1.67	>5.35
I-100×100×5-MI		17.2	0.98	1.49	_*
I-140×70×5-MI		10.0	1.10	1.80	>8.76

Test results for beam specimens.

* The ultimate moment M_u of the specimen I-100×100×5-MI is lower than the cross-section plastic moment capacity M_{pl} .

Table 5

Comparison of experimental results with FE results considering four levels of imperfections.

Specimen ID	Finite element M_u / Test M_u				
	ω_0	<i>t</i> /100	<i>t</i> /30	<i>t</i> /10	
I-50×50×5-MA	0.98	0.98	0.98	0.97	
I-70×70×5-MA	0.95	0.95	0.94	0.94	
I-80×60×5-MA	0.97	0.98	0.97	0.95	
I-90×70×5-MA	1.01	1.02	1.01	1.00	
I-100×100×5-MA	0.97	0.98	0.97	0.95	
I-140×70×5-MA	1.00	1.00	0.99	0.98	
I-50×50×5-MI	1.02	1.03	1.01	0.97	
I-70×70×5-MI	0.96	0.98	0.95	0.89	
I-80×60×5-MI	0.93	0.94	0.93	0.90	
I-90×70×5-MI	0.91	0.91	0.89	0.86	
I-100×100×5-MI	0.96	0.98	0.95	0.92	
I-140×70×5-MI	0.96	0.97	0.94	0.90	
Mean	0.97	0.98	0.96	0.94	
COV	0.03	0.03	0.03	0.05	

Table 6

Comparisons of experimental and FE ultimate moments against predicted bending moment resistances.

Axis of bending	Class of cross-section	on Number of Number of		$M_u/M_{u,EC3}$	
		experimental data	numerical data	Mean	COV
	Class 1 or Class 2 I-section	5	34	1.07	0.02
Majoravia	Class 3 I-section	0	59	1.15	0.04
wajoi axis	Class 4 I-section	1	92	1.28	0.08
_	Sub-total	6	185	1.18	0.09
	Class 1 and 2 I-section	5	25	1.09	0.02
Minorovia	Class 3 I-section	1	26	1.57	0.05
WIIIOF axis	Class 4 I-section	0	56	1.52	0.06
	Sub-total	6	101	1.44	0.19
	Total	12	286	1.26	0.18

(a) EN 1993-1-12 [14]

(b) AS 4100 [15]

Axis of bending	Class of cross-section	Number of	Number of	M_u/N_u	$I_{u,AS}$
		experimental data	numerical data	Mean	COV
	Compact I-section	2	21	1.08	0.01
Maionavia	Non-compact I-section	4	80	1.10	0.03
wajor axis	Slender I-section	0	84	1.58	0.29
	Sub-total	6	185	1.31	0.31
	Compact I-section	2	8	1.17	0.03
Minor oxis	Non-compact I-section	4	51	1.33	0.06
WIIIOF axis	Slender I-section	0	42	3.22	1.46
	Sub-total	6	101	2.05	1.38
	Total	12	286	1.57	0.92

(c) ANSI/AISC 360-16 [16]

Axis of bending	Class of cross-section	Number of	Number of	M_u/I	$M_{u,AISC}$
_		experimental data	numerical data	Mean	COV
	Compact I-section	2	36	1.06	0.02
Majoravia	Non-compact I-section	4	131	1.11	0.07
Major axis	Slender I-section	0	18	1.35	0.15
	Sub-total	6	185	1.12	0.10
	Compact I-section	2	28	1.09	0.03
Minorovia	Non-compact I-section	4	40	1.30	0.16
WIIIOF axis	Slender I-section	0	33	3.13	1.08
	Sub-total	6	101	1.81	1.11
	Total	12	286	1.36	0.74

Table 7

Established slenderness limits in the current design standards.

(a) EN 1993-1-12 [14]			
Plate element type	Loading condition	Class 3 limit	Class 2 limit
Outstand flange	Compression	14 <i>EEC</i> 3	$10\varepsilon_{EC3}$
Internal web	Bending	$124\varepsilon_{EC3}$	$83\varepsilon_{EC3}$
Outstand flange	Compressive stress gradient	$21 \varepsilon_{EC3} k_{\sigma}^{0.5}$	_

(b) AS 4100 [15]

Plate element type	Loading condition	Yield slenderness limit	Plasticity slenderness limit
Outstand flange	Compression	$14\varepsilon_{AS}$	$8\varepsilon_{AS}$
Internal web	Bending	115 <i>EAS</i>	$82\varepsilon_{AS}$
Outstand flange	Compressive stress gradient	$22\varepsilon_{AS}$	_

(c) ANSI/AISC 360-16 [16]

Plate element type	Loading condition	Non-compact limiting	Compact limiting width-to-
_		width-to-thickness ratio	thickness ratio
Outstand flange	Compression	$1.14 \varepsilon_{AISC} k_c^{0.5}$	$0.38 \varepsilon_{AISC}$
Internal web	Bending	$5.7\varepsilon_{AISC}$	$3.76\varepsilon_{AISC}$
Outstand flange	Compressive stress gradient	$1.0\varepsilon_{AISC}$	-



Fig. 1. Measured stress-strain curves from longitudinal and transverse coupons [3].



Fig. 2. General membrane residual stress pattern for welded I-sections [3].



Fig. 3. Test rig for initial local geometric imperfection measurements.



Fig. 4. Minor-axis four-point bending test setup.



Fig. 5. Major-axis four-point bending test setup.





Fig. 6. Test and FE failure modes for beam specimen I-100 \times 100 \times 5-MA in major-axis bending.



Fig. 7. Test and FE failure modes for beam specimen I-100×100×5-MI in minor-axis bending.



Fig. 8. Normalised moment-curvature curves for beam specimens bent about the major principal axes.



Fig. 9. Normalised moment-curvature curves for beam specimens bent about the minor principal axes.



Fig. 10. Typical residual stress pattern (in MPa) in modelled S690 welded I-section beams I-100×100×5-MA and I-100×100×5-MI (Positive values indicate tensile residual stresses while negative values indicate compressive residual stresses).



Fig. 11. Normalised test and FE moment-curvature curves for beam specimen I-140×70×5-MA.



Fig. 12. Normalised test and FE moment–curvature curves for beam specimen I-100×100×5-MI.



Fig. 13. EC3 Class 3 slenderness limit for outstand elements in compression.



Fig. 14. EC3 Class 3 slenderness limit for internal elements in bending.



Fig. 15. EC3 Class 3 slenderness limit for outstand elements under triangular compressive stress gradients.



Fig. 16. EC3 Class 2 slenderness limit for internal elements in bending.



Fig. 17. EC3 Class 2 slenderness limit for outstand elements in compression.



Fig. 18. Comparison of experimental and numerical ultimate moments with EC3 bending resistance predictions.



Fig. 19. AS yield slenderness limit for outstand elements in compression.



Fig. 20. AS yield slenderness limit for internal elements in bending.



Fig. 21. AS yield slenderness limit for outstand elements under triangular compressive stress gradients.



Fig. 22. AS plasticity slenderness limit for internal elements in bending.



Fig. 23. AS plasticity slenderness limit for outstand elements in compression.



Fig. 24. Comparison of experimental and numerical ultimate moments with AS bending resistance predictions.



Fig. 25. AISC non-compact limiting width-to-thickness ratio for outstand elements in compression.



Fig. 26. AISC non-compact limiting width-to-thickness ratio for internal elements in bending.



Fig. 27. AISC non-compact limiting width-to-thickness ratio for outstand elements under triangular compressive stress gradients.



Fig. 28. AISC compact limiting width-to-thickness ratio for internal elements in bending.



Fig. 29. AISC compact limiting width-to-thickness ratio for outstand elements in compression.



Fig. 30. Comparison of experimental and numerical ultimate moments with AISC bending resistance predictions.