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Single Electron Transistor Scheme Based on Multiple Quantum	1			
Dot Islands: Carbon Nanotube and Fullerene				
	3			
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Abstract

Single electron transistor (SET) is a nano dimension device that is offered by technology to 18 solve the problem of aggressive scaling in traditional transistors. Its operation speed depends 19 on carrier mobility of its quantum dot. In this research, fullerene (C₆₀) and carbon nanotube 20 (CNT) are utilized as materials of quantum dots in SET. Two SETs with different multiple 21 quantum dots as C₆₀-CNT-C₆₀ and CNT-C₆₀-CNT are modeled and analyzed. The 22 comparison study shows that total length of quantum dots as fullerene diameter and CNT 23 length have indirect effect on its current. Moreover increasing temperature decreases its 24 current while rising of the gate voltage increases its current. In other words, quantum dot 25 length, temperature and gate voltage are parameters which can control SET operation. 26 Furthermore two SETs are simulated and their stability diagrams are analyzed. The 27 simulation results show that C₆₀-CNT-C₆₀ SET has lower coulomb blockade and also it has 28 more reliability and faster operation than CNT-C₆₀-CNT SET. 29

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Key words: Carbon Nanotube, Fullerene, Quantum Dot, Single Electron Transistor. 30

1-Introduction

According to the Moore's law, the number of transistors in a chip is doubled every 2-3 years 32 but MOSFET scaling results in performance degradations generally called short channel 33 effects (SCEs). Novel transistors are designed to improve limitations imposed by SCEs in 34 traditional bulk MOSFETs. Common examples which are used by the industry includes 35 FinFETs, tunnel FETs, and nanowires FETs [1,2,3]. However, all these technologies still 36 suffer from leakage current and power consumption. On the other hand, we know electrons 37 cross from the transistor channel, so decreasing the number of electrons and transfer one 38 electron from transistor channel at a very short time can improve its performance and 39 increase its operation speed. Furthermore advanced electronic technology needs chips 40 capable of doing more information processing in a shorter time compared with traditional 41 chips and scaling according to Moore's law is no more adequate to achieve nano-dimension 42 devices based on transfer of many carriers at the same time. The device which can improve 43 these limitations in nanoscale is single electron transistor (SET). SET with its particular 44 characteristics such as low energy consumption, nano size dimension and high operating 45 speed can be a candidate to continue aggressive scaling [4]. SET works based on the transfer 46 of single electrons in its channel in a very short time, so its operation speed is much higher 47 than traditional MOSFETs and their derivatives. SET contains source and drain electrodes, 48

gate electrode and an island between them. Its gate electrode can control electron tunneling. 49 SET operates by moving an electron via tunneling between source and drain electrodes [5]. It 50 has higher speed operation and lower energy consumption than Field Effect Transistors 51 (FETs) [6, 7]. FETs work by crossing some electrons in their channels but SET operates by 52 transfer of single electrons between electrodes and island through a tunnel Junction [8,9,10]. 53 Any tunnel junction consists of one capacitance and a resistance in series [11]. When an 54 electron crosses from a tunnel junction to island, the capacitor charges and tunneling of 55 second electron is stopped [12]. This electron is transferred to the other electrode and this 56 phenomenon is called single electron tunneling [13]. 57

Another phenomenon is Coulomb Blockade (CB) that affects on SET operation which has 58 been discussed by C. Gorter in 1951 [14, 15]. It occurs when the resistance of a tunnel 59 junction becomes more than quantum resistance [16]. It prevents electron transfer to or out of 60 SET island, so operation speed of SET depends on carrier mobility in the island [17]. On the 61 other hand, the island has high carrier mobility in quantum size. Therefore quantum dot (QD) 62 can be used in transistor nanostructure [18, 19]. Moreover increasing the number of QDs can 63 reduce some operation limitations of SET such as cryogenic temperature and leakage current 64 [20]. Increasing cryogenic temperature to room temperature is a good improvement in SET 65 operation because CB occurs when the charging energy is less than the thermal energy (The 66 essential energy to tunnel an electron to the QD) [21, 22]. The coulomb blockade interval 67 makes a diamond-shaped region which is called coulomb diamond. It is function of V_g and 68 V_{ds} while the number of electrons on the QD are fixed in any region. The curve for V_g versus 69 V_{ds} is called charge stability diagram [23]. Furthermore, material of QD has direct effect on 70 SET operation. There are different QDs but carbon based materials such as fullerenes and 71 carbon nanotube (CNT) have higher carrier mobilities than other materials [12,24]. Hence, 72 fullerene SET presents lower leakage current and CB region compared with silicon QD-SET 73 [22]. CNT is a one dimensional material while Fullerene is classified under category of zero 74 dimensional materials [25, 16]. Fullerenes have different natural forms as C₃₈ and C₄₂. In 75 addition, some molecules have several symmetric shapes that make direct influence on SET 76 operation [26]. This effect is investigated for three molecules C₃₈, C₄₂ and C₆₀ as shown in 77 Fig.1 and then their charge stability diagrams are reported in Fig.2 (a-f) [27]. The comparison 78 study in Fig.2 indicates that C₃₈ and C₄₂ have different stability diagrams because they exhibit 79 different types of symmetry. This problem decreases reliability of SET, so buckminster 80 fullerene (C_{60}) is selected as SET island. Its molecule not only has one type of symmetry but 81 also is cheaper to produce compared with other fullerene molecules while it is very stable in 82 nano range dimensions [28]. 83

SETs can be used in quantum computing, single electron memory and supersensitive 84 electrometry. In this research, the advantages of two proposed SET structured are explored 85 utilizing fullerene and CNT. Because of SET unique characteristics, it can be an alternative 86 for the next generation of devices in electronic circuits. Moreover we investigate the impact 87 of fullerene diameter, CNT length, temperature and the gate voltage on the SET performance. 88 Finally a comparison study is performed between two proposed structures to reveal which 89 one can be a suitable candidate for replacement of traditional transistors in future technology. 90

2-Theoritical Model

Single electron transistor works based on electron tunneling from source electrode to drain 92 electrode. This electron transfer can be analyzed by the quantum mechanical effects 93 describing that when electron wave crosses from different regions of the device, it has a 94 particular wave function in each region. Therefore SET islands, drain and source are different 95

target regions as shown in Fig. 3 where Schrodinger's equations can be written for them. The
SET model is based on three islands that each island is assumed to behave like a potential
well. Equations which explain wave function at regions of a fullerene island are:
98

$$\Psi_I = A_1 e^{k_1 x} + B_1 e^{-k_1 x} \tag{1}$$

$$\Psi_{II} = A_2 e^{ik_2 x} + B_2 e^{-ik_2 x} \tag{2}$$

$$\Psi_{III} = A_3 e^{ik_3 x} \tag{3}$$

where $k_1 = k_3 = \frac{\sqrt{2m(V_0 - E)}}{\hbar}$ and $k_2 = \frac{\sqrt{2mE}}{\hbar}$. 102

These equations can be solved using appropriate boundary conditions which can be written103from continuity of the wave function and its derivative at x = 0 and L_1 . These parts of the104modeling are fully covered at the appendix A.105

Therefore transmission coefficient of region with a fullerene island is calculated as:

$$T_1 = \frac{1}{1 + K_F sinh^2(k_2 L_1)} \tag{4}$$

106

$$K_F = \frac{(h^2 + ta'm)E - \hbar^2 E_{g_F}}{2\sqrt{ta'\hbar m E(E - E_{g_F})}}$$
(5) 108

where " L_1 " is fullerene diameter, $k_2 = \frac{\sqrt{2mE}}{\hbar}$, "E" is the electron energy, " $m = 9.109 \times$	109
$10^{-31}kg$ " is the electron effective mass in fullerene, " $\hbar = 6.582119514 \times 10^{-16}$ eV.s" is the	110
reduced Planck's constant, " $a' = 3a_{c-c}$ ", $a_{c-c_F} = 1.46A^0$ is the distance between	111
neighbouring carbon atoms in fullerene molecule, " $E_{g_F} = 0.1828$ " is the fullerene bandgap	112
$(C_{60}$ energy gap is defined as the difference between the highest occupied and lowest	113
unoccupied molecular orbitals (HOMO and LUMO)) and " $t=2.5$ eV" is the hopping energy.	114

The Shorodinger equations are written for second part of SET with carbon nanotube island 115 as: 116

$$\Psi_{III} = A_3 e^{k_1 x} + B_3 e^{-k_1 x} \tag{6}$$

$$\Psi_{IV} = A_4 e^{ik_4 x} + B_4 e^{-ik_4 x} \tag{7}$$

$$\Psi_V = A_5 e^{ik_1 x} \tag{8}$$

where
$$k_1 = \frac{\sqrt{2m(V_0 - E)}}{\hbar}$$
 and $k_4 = \frac{\sqrt{2mE}}{\hbar}$. 120

These set of equations should also be solved and the boundary conditions can be written at121points x = 0 and L_2 . These parts of model are also fully covered at the appendix A.122

Therefore transition coefficient of region with a CNT island is calculated as

$$T_2 = \frac{1}{1 + K_{CNT} sinh^2(k_4 L_2)}$$
(9) 124

$$K_{CNT} = \frac{(\hbar^2 + ta'm)E - \hbar^2 E_{g_{CNT}}}{2\sqrt{ta'\hbar m E(E - E_{g_{CNT}})}}$$
(10) 125

where " L_2 " is the CNT length, $k_4 = \frac{\sqrt{2mE}}{\hbar}$, $a_{c-c_{CNT}} = 1.42A^0$ is the distance between 126 neighbouring carbon atoms, " $E_{g_{CNT}} = \frac{0.8eV}{d(nm)}$ " is the CNT band gap where d = 2R is the CNT 127 diameter and "t=2.7eV" is the hopping energy of CNT. 128 The first proposed SET comprises three islands as two fullerene molecules and one CNT. 129 Therefore the product of three calculated transmission coefficients as obtained in Eqs. (4) and 130 (9) results in the total transmission coefficient as: 131

$$T_{Total_1} = T_1 \times T_2 \times T_1 \tag{11}$$

$$T_{Total_{1}} = \frac{1}{K_{F}^{4}k_{2}^{4}L_{1}^{4} + 1 + 2K_{F}^{2}k_{2}^{2}L_{1}^{2} + K_{CNT}^{4}K_{F}^{2}k_{2}^{4}L_{1}L_{2} + K_{CNT}^{4}k_{4}^{2}L_{2}^{2} + 2K_{F}^{2}K_{CNT}^{2}k_{2}^{2}k_{4}^{2}L_{1}^{2}L_{2}^{2}}$$
(12) 133

where L_1 is diameter of fullerene and L_2 is CNT length. The parameters were defined 134 previously. 135

SET current with three multiple islands as two fullerene molecules and one CNT can be 136 calculated based on the Landauer formalism as: 137

$$I = \int_{0}^{\eta} T(E). F(E) dE$$
(13) 138

where "T(E)" is the total transmission coefficient of SET (T_{total_1}) and F(E) is Fermi 139 probability function defined as $F(E) = \left[\frac{1}{\exp\left(\frac{E-E_F}{k_BT}\right)+1}\right]$, where "E" is electron energy, " E_F " is 140

Fermi energy, "T" is temperature and " k_B " presents the Boltzmann's constant. 141

Based on proposed model, the current versus voltage characteristic of the SET with three 142 islands as two fullerene molecules and one CNT in the parabolic-band region can be 143 expressed as: 144

$$I = \int_{0}^{\eta} \frac{\overline{K_{F}}^{4} (Ak_{B}T(x+d_{F}))^{2} L_{1}^{4} + 1 + 2K_{F}^{2} (Ak_{B}T(x+d_{F})) L_{1}^{2} + K_{CNT}^{4} K_{F}^{2} (Ak_{B}T(x+d_{F}))^{2} (Ak_{B}T(x+d_{CNT})) L_{1} L_{2}}{\frac{1}{K_{CNT}^{4} (Ak_{B}T(x+d_{CNT})) L_{2}^{2} + 2K_{F}^{2} K_{CNT}^{2} (Ak_{B}T(x+d_{F})) (Ak_{B}T(x+d_{CNT})) L_{1}^{2} L_{2}^{2}} \frac{dE}{e^{x-\eta} + 1}}$$
(14) 145

where "L₁" is diameter of fullerene and "L₂" is length of CNT , $x = \frac{E - E_g}{k_B T}$, $\eta = \frac{E_F - E_g}{k_B T}$, $E_g = 146$

$$\frac{E_{g_F} + E_{g_{CNT}}}{2}, d_F = \frac{E_{g_F}}{k_B T}, d_{CNT} = \frac{E_{g_{CNT}}}{k_B T}, A = \sqrt{\frac{2m}{\hbar^2}} \text{ and other parameters were defined previously.}$$
 147

The second proposed SET comprises three islands as two CNTs and one fullerene molecule.148The product of three transmission coefficients as calculated in Equations (4) and (9) will be149total transmission coefficient which is now given by:150

$$T_{Total_2} = T_2 \times T_1 \times T_2 \tag{15}$$

$$T_{Total_2} = \frac{1}{K_{CNT}^4 k_4^4 L_2^4 + 1 + 2K_{CNT}^2 k_4^2 L_2^2 + K_F^4 K_{CNT}^2 k_4^4 k_2^2 L_2 L_1 + K_F^4 k_2^2 L_1^2 + 2K_{CNT}^2 K_F^2 k_4^2 k_2^2 L_2^2 L_1^2}$$
(16) 152

where all of the parameters in Eq. (16) were previously defined. Therefore the SET current153with three multiple islands as one fullerene molecule and two CNTs can be calculated based154on the Landauer formalism as:155

$$I = \int_{0}^{\eta} \frac{K_{CNT}^{4} (Ak_{B}T(x+d_{CNT}))^{2} L_{2}^{4} + 1 + 2K_{CNT}^{2} (Ak_{B}T(x+d_{CNT})) L_{2}^{2} + K_{F}^{4} K_{CNT}^{2} (Ak_{B}T(x+d_{CNT}))^{2} (Ak_{B}T(x+d_{F})) L_{1} L_{2}}{\frac{1}{K_{F}^{4} (Ak_{B}T(x+d_{F})) L_{1}^{2} + 2K_{F}^{2} K_{CNT}^{2} (Ak_{B}T(x+d_{CNT})) (Ak_{B}T(x+d_{F})) L_{1}^{2} L_{2}^{2}} \frac{dE}{e^{x-\eta} + 1}}$$
(17) 156

where all parameters were defined previously.

3- Results and discussion

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The proposed models depend on some parameters such as temperature, island length and gate 159 voltage. The impact of CNT length on the current in the first proposed SET is investigated 160 and plotted in Fig. 4. The gate voltage is 1mV, temperature is 300⁰ K and the fullerene 161 diameter is 1nm. The variations in Fig. 4 indicates that CNT length has an indirect effect on 162 the SET current because increasing CNT length increases distance between source and drain 163 therefore leakage current increases in SET .This SET contains two fullerene molecules where 164 the effect of their diameters on the current is shown in Fig. 5. The gate voltage is 1mV, 165 temperature is 300⁰ K and CNT length is 1nm. Fig. 5 shows that decreasing of fullerene 166 diameter decreases leakage current, so it increase SET current. Another effective factor in the 167 proposed model is the temperature. The impact of temperature on the SET I-V characteristics 168 is illustrated in Fig. 6. Here the gate voltage is chosen as 1mv, CNT length and fullerene 169 diameter are both 1nm. It can be seen that the temperature has indirect effect on the proposed 170 model. The increasing temperature increases electron tunneling to QD but electron 171 accumulation occurs in QD, so electron transfer decreases and current decreases in higher 172 temperature. Moreover effect of the gate voltage on SET current is investigated and sketched 173 in Fig. 7. The temperature is 300⁰ K, CNT length and fullerene diameter are both 1nm. The 174 curves in Fig. 7 show that increasing of the applied gate voltage increases SET current. 175

The next proposed SET for our study is comprised of three islands: two CNTs in the channel176sides and one fullerene molecule in the middle as shown in Fig. 8.177

The current versus voltage characteristic of the second proposed SET with one fullerene 178 molecule in the channel and two carbon nanotubes on its sides depends on some factors. The 179 island length affects on SET current. Impact of the CNT length on SET current is investigated 180 as shown in Fig. 9. The gate voltage is 1mV, temperature is 300⁰ K and fullerene diameter is 181 1nm. It confirms that the CNT length has indirect effect on the SET current. The impact of 182 fullerene molecule diameter on the SET current is plotted in Fig. 10. Here, the gate voltage is 183 assumed to be 1mV, temperature is 300⁰ K and CNT length is 1nm. It confirms that 184 increasing fullerene diameter decreases SET current as expected. Both Fig .9 and Fig .10 185 show the bigger QD has the more leakage current, so lower SET current occurs in this case. 186 Moreover the current is affected by changing the temperature as illustrated in Fig. 11. Again, 187 the gate voltage is 1my, CNT length and fullerene diameter are both 1nm. It reveals the fact 188 that increasing of the temperature decreases SET current that shows electron accumulation in 189 QDs and decreasing current. Another important factor is the gate voltage as plotted in Fig. 12. 190 The temperature is 300⁰ K, CNT length is 1nm and fullerene diameter is 1nm. The current 191 versus voltage characteristics of different gate voltages in Fig. 12 show this factor has direct 192 influence on the SET current. 193

The impact of island material on the SET operation can be illustrated using its charge 194 stability diagram. Two proposed SETs with different islands $C_{60} - CNT - C_{60}$ and $CNT - C_{60}$ 195 $C_{60} - CNT$ are designed with Atomistic Toolkit software [27], so their charge stability 196 diagrams are simulated and plotted in Fig. 13. The important parameters which are extracted 197 from stability diagrams of two structures as shown in Fig. 13 are summarized in table1. It 198 clearly shows the range of gate and drain voltage for each diamond and the associated area. 199 The sum of coulomb diamond areas for C_{60} -CNT- C_{60} SET is 1.329 while this summation for 200 CNT-C $_{60}$ - CNT SET equals 7.538. 201

Table1: Important parameters extracted from Fig. 13.					
Diamond	V _{ds_{min},V_{ds_{max}}}	ΔV _{ds}	Vg _{min} ,Vg _{max}	<mark>∆Vg</mark>	Area
$\frac{C_{60}\text{-}CNT\text{-}C_{60}}{\text{Diamond 1}}$	-0.297,0.319	<mark>0.616</mark>	<mark>-1.164,-0.869</mark>	<mark>2.033</mark>	<mark>0.626</mark>
C ₆₀ -CNT-C ₆₀	-0.312,0.319	<mark>0.631</mark>	<mark>-0.862,-0.529</mark>	<mark>1.391</mark>	<mark>0.438</mark>

Diamond 2					
C ₆₀ -CNT-C ₆₀	-0.529,-0.204	<mark>0.733</mark>	-0.521,-0.204	<mark>0.725</mark>	<mark>0.265</mark>
Diamond 3					
CNT-C ₆₀ - CNT	<mark>-0.372,0.364</mark>	<mark>0.736</mark>	-3.159,-2.781	<mark>5.940</mark>	<mark>2.185</mark>
Diamond 1					
CNT-C ₆₀ - CNT	-0.595,0.572	<mark>1.167</mark>	<mark>-2.773,-2.192</mark>	<mark>4.965</mark>	<mark>2.897</mark>
Diamond 2					
CNT-C ₆₀ - CNT	-0.669,0.651	<mark>1.320</mark>	<mark>-2.182,-1.540</mark>	<mark>3.722</mark>	<mark>2.456</mark>
Diamond 3					

The comparison study of coulomb diamond patterns in Fig. 13 indicates that not only SET 206 with two fullerene molecules and one CNT has smaller coulomb diamonds but also has lower 207 coulomb blockade range and zero conductance region than other proposed SET. It reveals the 208 fact that the most important factor in SET operation is the island length and since SET with 209 $C_{60} - CNT - C_{60}$ islands has smaller islands, it presents lower coulomb blockade range and 210 faster and better operation compared with $CNT - C_{60} - CNT$ SET. 211

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4-Conclusion

Single electron transistor (SET) based on quantum dot can improve problems of integrated 215 circuit scaling. Quantum dots such as fullerene and carbon nanotube can be utilized to 216 increase operation speed of SET. In this research, two SETs with fullerene (C₆₀) and CNT 217 islands as $C_{60} - CNT - C_{60}$ SET and $CNT - C_{60} - CNT$ SET were analyzed and also some 218 effective factors on SET operation were investigated. The comparison study indicates that 219 decreasing fullerene diameter, CNT length and temperature increase SET current but applied 220 gate voltage has a direct effect on the current. Moreover proposed SETs were simulated and 221 simulation results were compared together. Comparison study showed that $C_{60} - CNT - C_{60}$ 222 SET has lower coulomb blockade range and also higher operation speed than $CNT - C_{60}$ – 223 CNT SET. It confirms effective role of island length and its material in SET operation and 224

SET reliability. Therefore selecting suitable material for the island and the associated length225can control the current value. Furthermore current can be tuned by temperature and applied226gate voltage.227

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Appendix A

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The Schrodinger equations are solved for the first part:

$\frac{\hbar^2}{2m} \frac{d^2 \psi_I(x)}{dx^2} + (E - V) \psi_I(x) = 0$	$x \leq 0$	Region I	(A1)	237

$$\frac{\hbar^2}{2m} \frac{d^2 \psi_{II}(x)}{dx^2} + E \psi_{II}(x) = 0 \qquad 0 < x < L_1 \text{Region II}$$
(A2) 238

$$\frac{\hbar^2}{2m} \frac{d^2 \psi_{III}(x)}{dx^2} + (E - V)\psi_{III}(x) = 0 \qquad x \ge L_1 \qquad \text{Region III}$$
(A3) 239

The boundary conditions can be written from continuity of the wave function and its 240 derivative at x = 0 and L_1 as: 241

$$A_1 + B_1 = A_2 + B_2 \tag{A4} 242$$

$$k_1 A_1 - k_1 B_1 = i k_2 A_2 - i k_2 B_2 \tag{A5}$$

$$A_2 e^{ik_2 L_1} + B_2 e^{-ik_2 L_1} = A_3 e^{k_1 L_1}$$
(A6) 244

$$ik_2 A_2 e^{ik_2 L_1} - ik_2 B_2 e^{-ik_2 L_1} = k_1 A_3 e^{k_1 L_1}$$
(A7) 245

The Schrodinger equations are solved for second part as:

$$\frac{\hbar^2}{2m} \frac{d^2 \psi_{III}(x)}{dx^2} + (E - V)\psi_{III}(x) = 0 \qquad x \le 0 \qquad \text{Region III}$$
(A8) 247

$$\frac{\hbar^2}{2m} \frac{d^2 \psi_{IV}(x)}{dx^2} + E \psi_{IV}(x) = 0 \qquad 0 < x < L_2 \text{Region IV}$$
(A9) 248

$$\frac{\hbar^2}{2m} \frac{d^2 \psi_V(x)}{dx^2} + (E - V)\psi_V(x) = 0 \qquad x \ge L_2 \qquad \text{Region V}$$
(A10) 249

These boundary conditions can be written at x = 0 and L_2 as:

$A_3 + B_3 = A_4 + B_4$	(A11)	251
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$$k_1 A_3 - k_1 B_3 = i k_2 A_4 - i k_2 B_4 \tag{A12}$$

$$A_4 e^{ik_4 L_2} + B_4 e^{-ik_4 L_2} = A_5 e^{k_4 L_2}$$
(A13) 253

$$ik_4 A_4 e^{ik_4 L_2} - ik_4 B_4 e^{-ik_4 L_2} = k_1 A_5 e^{k_4 L_2}$$
(A14) 254

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C42-cs

C60



Fig.1. C_{38} and C_{42} molecules with different types of symmetry and C_{60} molecule [23].



Fig. 2.Stability diagrams of C_{38} and C_{42} with different types of symmetry and C_{60} .



Fig. 3.Top: SET with three islands (two fullerene molecules in the sides and one carbon nanotube in the middle: $C_{60} - CNT - C_{60}$), Bottom: SET energy versus position in the channel region.



Fig. 4. I-V characteristics of the proposed SET ($C_{60} - CNT - C_{60}$ islands) for different CNT380lengths.381



Fig. 5. I-V characteristics of the proposed SET ($C_{60} - CNT - C_{60}$ islands) for different398fullerene diameters.399



Fig. 6. I-V characteristics of the proposed SET ($C_{60} - CNT - C_{60}$ islands) at different406temperatures.407



Fig. 7. I-V characteristics of the proposed SET ($C_{60} - CNT - C_{60}$ islands) for different gate 412 voltages. 413



Fig.8. Top: SET with three islands (two CNTs in the sides and one fullerene molecule in the419middle: $CNT - C_{60} - CNT$), Bottom: SET energy versus position in the channel region.420





Fig. 9. I-V characteristics of the proposed SET ($CNT - C_{60} - CNT$ islands) for different438CNT lengths.439





Fig. 10. I-V characteristics of the proposed SET ($CNT - C_{60} - CNT$ islands) for different452fullerene diameters.453









Fig. 11. I-V characteristics of the proposed SET ($CNT - C_{60} - CNT$ islands) at different464tempratures.465



Fig. 12. I-V characteristics of the proposed SET ($CNT - C_{60} - CNT$ islands) for different478gate voltages.479



Fig. 13. The charge stability diagrams of two proposed SETs with three islands :(a) islands as484 $C_{60} - CNT - C_{60}$, (b) islands as $CNT - C_{60} - CNT$.485