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Optical Control of Solar Sails using Distributed Reflectivity

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The dynamics of solar sails with a variable surface reflectivity distribution are investigated. When changing the reflectivity across the sail film, which can be achieved using electro-chromic coatings, the solar radiation pressure forces and torques across the sail film can be controlled without changing the attitude of the spacecraft relative to the Sun and without using mechanical systems. The paper presents two approaches. First, a continuous reflectivity distribution is presented to control the sail attitude under the influence of, for example, gravity gradient torques in Earth orbit. The second approach assumes discrete on/off reflectivity regions across the surface. Both concepts of ‘optical reconfiguration’ of solar sails enable a more flexible steering of the spacecraft and minimize actuation effort.

I. Introduction

Using conventional solar sailing technology, the solar radiation pressure (SRP) force vector direction and magnitude depend strongly on the sail attitude relative to the Sun, limiting the applicability of solar sails compared to other low-thrust propulsion systems such as solar-electric propulsion. Furthermore, the SRP force magnitude follows an inverse square law with solar distance, making the sail less efficient at large distances from the Sun. In order to increase the flexibility of modulating the SRP forces and torques, and to decrease the total mass of the spacecraft, we introduce the concept of variable optical properties for large gossamer spacecraft. In particular, the attitude dynamics of a rigid, flat solar sail with a variable surface reflectivity distribution are investigated. When changing the reflectivity coefficient across the sail film, the SRP forces and torques acting on the sail can be controlled without changing the incidence angle relative to the Sun and without using mechanical systems. The reflectivity can in principle be modified using electro-chromic coatings, which consist of an electro-active material that changes its surface reflectivity according to an applied electric potential. By assigning an appropriate reflectivity distribution across the sail area, the center-of-pressure can be shifted optically relative to the center-of-mass (CoM), rather than mechanically, as for example through the use of moving payload masses.

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The paper will demonstrate the potential of using distributed reflectivity for optical control of the sail attitude. First, in section II, the reflectivity distribution $\rho(s)$ is ideally assumed to be continuous across the surface, with arbitrary values of $\rho$ in the interval $[0, 1]$. Through this, the reflectivity can be modulated continuously between diffuse and specular reflection. The concept is applied to counteract gravity gradient torques in a planar Earth orbit. Subsequently, in section III, a more realistic approach is taken, using discrete regions of activated and deactivated (on/off) reflectivity, separated by a variable boundary line. When controlling the shape and position of the boundary line across the surface, a wide range of torque vector directions in the sail-plane can be generated. This approach is demonstrated for two-axis attitude control of the sail in a Sun-centered orbit. It will be shown that through a basic maneuver about two axes, the sail can be brought to a Sun-pointing attitude from a chosen initial displacement. Since the SRP forces acting on the sail vary with the sail’s attitude with respect to the Sun, an analytic method will be derived to compute the required shape and position of the reflective regions in order to maintain a constant torque during the maneuver. This can be achieved through the formulation of an inverse problem to the derived torque equations.

II. Sail Attitude Control using Variable Reflectivity Distribution

In this first section, a continuous reflectivity distribution is used to control the planar attitude of a solar sail in low Earth orbit (LEO). In particular, this steering method is applied to counteract the gravity-gradient torques acting on a large rigid sail film. It will be shown that a constant Sun-pointing attitude can be maintained along the orbit, using the proposed chosen concept. A square solar sail is modeled as a rigid flat Kapton film of density $\delta = 1.572 \text{ kg/m}^3$, thickness $d = 2.5 \times 10^{-6} \text{ m}$ and edge length $L = 50 \text{ m}$, without assembly or payload masses, as shown in figure 1.

A sail-fixed Cartesian coordinate frame $(x, y, z)$ is used to describe the sail attitude along its orbit, where the $z$-axis is constrained to be always perpendicular to the ecliptic plane. This allows only one degree of rotational freedom, while rotation about the sail $x$ and $y$ axes is omitted. The mass moments of inertia of the Kapton film are $I_{xx} = 4093.8 \text{ kg m}^2$ and $I_{yy} = I_{zz} = 2046.9 \text{ kg m}^2$, with a total mass $m = 9.83 \text{ kg}$. To approximate a continuous reflectivity distribution, it is ideally assumed that the entire sail area $A$ is covered with stripes of infinitesimal electro-chromic coating elements that are able to change their reflectivity. The additional mass and thickness of the elements is neglected throughout this preliminary study. When changing the reflectivity of a surface element $dA = L \cdot ds$ on the sail, where $s$ denotes the distance of the element from the axis of rotation $x$, the difference in SRP force creates a torque $T_{\text{SRP},x}$ about the CoM of the sail.

Figure 1. Square solar sail with continuous reflectivity distribution across the surface (left) and sail model using infinitesimal electro-chromic elements (right).
For now, a constant reflectivity is assumed in $x$-direction such that no torque is generated about the sail $y$-axis. The CoM is assumed to move on a circular LEO of 400 km altitude in the ecliptic plane, as shown in figure 2, while air drag and solar eclipses are ignored for illustration. A constant sail cone angle $\alpha=0$ deg between the Sun-sail line $R_S$ and the sail plane normal is assumed.

![Figure 2. Solar sail on Earth-centered circular LEO of 400 km altitude and constant Sun-pointing attitude.](image)

The gravity-gradient torque along the orbit depends on the angle $\gamma$ between the sail plane and the Earth radial direction $R_E$. It can be approximated using the standard relation

$$T_{GG,x} = 3 \frac{\mu_E}{R_{CoM}^3} \sin \gamma \cos \gamma (I_{xx} - I_{yy})$$

(1)

with $\mu_E$ being the gravitational parameter of the Earth and $R_{CoM}$ the radial distance of the sail’s CoM from the Earth’s center. For example, the maximum gravity-gradient torque acting on the sail considered here is of the order $T_{GG,x} = 4 \times 10^{-3}$ Nm about the sail $z$-axis. A variable surface reflectivity distribution $0 \leq \rho(s) \leq 1$ is now assumed to counteract this gravity gradient torque. The SRP force and torque about the sail’s CoM are calculated using a simplified SRP model. It assumes that the sail surface is a perfectly (specular) reflecting mirror, neglecting all other forms of optical interactions between the solar photons and the sail surface such as scattering, absorption and thermal re-emission. The model also does not account for wrinkles, and thus assumes a perfectly flat sail surface. Accordingly, the solar radiation pressure $p_{SRP}$ can be written as

$$p_{SRP} = p_0 [1 + \rho(s)] \left( \frac{R_{S,0}}{R_S} \right)^2 \cos^2 \alpha$$

(2)

at a radial distance $R_S$ from the Sun and $p_0 = 4.563 \times 10^{-6}$ N/m$^2$ being the solar radiation pressure at $R_{S,0} = 1$ AU. In here, $\rho(s) = 1$ represents the ideal mirror that experiences the maximum possible SRP load $p_{max} = 2p_0$, while the minimum reflectivity $\rho(s) = 0$ reduces the effective SRP load to $p_{max}/2 = p_0$, since only the momentum of the incoming photons is applying a force to the surface. As a consequence, the solar radiation pressure induced forces can be modified directly when changing the surface reflectivity. According to figure 1, the incremental SRP force and torque acting about the CoM on a rectangular sail surface element can now be written as

$$dF_{SRP} = p_0 L [1 + \rho(s)] \left( \frac{R_{S,0}}{R_S} \right)^2 \cos^2 \alpha \, ds$$

(3a)

$$dT_{SRP,z} = p_0 L s [1 + \rho(s)] \left( \frac{R_{S,0}}{R_S} \right)^2 \cos^2 \alpha \, ds$$

(3b)
Assuming a linear reflectivity function
\[ \rho(s) = a_0 + a_1 \cdot s \] (4)
the above equations can be integrated over the interval \([-L/2, L/2]\), while constraining the sail surface to be always perpendicular to the Sun-sail line, thus \(\alpha = 0\), and assuming that the solar distance \(R_S = 1\) AU is constant on the Earth-centered orbit. The resulting SRP force and torque are found to be
\[
F_{\text{SRP}} = p_0 L \int_{-L/2}^{L/2} [1 + a_0 + a_1 \cdot s] ds = p_0 L^2 [1 + a_0] \] (5)
\[
T_{\text{SRP},z} = p_0 L \int_{-L/2}^{L/2} [1 + a_0 + a_1 \cdot s] s ds = \frac{1}{12} p_0 L^4 a_1 \] (6)

It can be seen that the magnitude of the resulting SRP force is only a function of the absolute coefficient \(a_0\). Furthermore, the SRP torque only depends on the slope \(a_1\) of the linear reflectivity function across the film, thus the difference of SRP force on the left and right hand side of the sail. If the forces are equal on both sides \(a_1 = 0\), the torque on the sail is clearly zero, regardless of the absolute value of the SRP force, as determined by \(a_0\). Equation (6) represents the SRP torque that must be generated in order to counteract the gravity-gradient torque \(T_{\text{GG},z}\) along the orbit, thus \(T_{\text{SRP},z}\) must always be equal to \(T_{\text{GG},z}\). Accordingly, the coefficients \(a_i\) of the linear reflectivity function \(\rho(s)\) can be calculated using the following equations
\[
a_1 = \frac{12T_{\text{GG},z}}{p_0 L^4} \quad \text{and} \quad a_0 = \frac{F_{\text{SRP}}}{p_0 L^2} - 1 \] (7)

Although \(a_1\) is always determined through the local \(T_{\text{GG},z}\) that needs to be compensated, \(a_0\) is in principle only constrained by the maximum possible \(F_{\text{SRP},\text{max}} = 2p_0 L^2\), for which \(a_0 = 1\) and also \(\rho(s) = 1 = \text{const}\) across the surface. However, a reflectivity gradient \(a_1 \neq 0\) is necessary to create a torque, while at the same time \(\rho(s) \leq 1\) must be satisfied across the entire sail. Thus, the upper constraint is \(a_{0,\text{max}} < 1\). The lower constraint is determined through the additional condition \(\rho(L/2) = 0\) or \(\rho(-L/2) = 0\) at the edge of the sail, in order to fix the linear reflectivity curve across the film. Inserting this into the linear reflectivity function, Eq. (4), while keeping \(a_1\) fixed, results in \(a_{0,\text{min}} = \pm a_1 L/2\) as the lower limit, depending on the sign of the torque that needs to be created. Figure 3 shows the resulting reflectivity distribution \(\rho(s)\) along the film as a

![Figure 3. Minimum reflectivity distribution across flat sail film using continuous electro-chromic coating elements.](image)
function of the sail attitude angle $\gamma$ during one revolution along the orbit for the chosen sail configuration. It can be seen that the necessary reflectivity to balance the gravity-gradient torque is relatively small compared to the maximum reflectivity that can be achieved with currently developed electro-chromic devices, e.g. as used on the IKAROS solar sail. According to the reference, a maximum $\rho_{\text{max}} = 0.6$ is currently possible. Accordingly, for the chosen application to counteract gravity gradient torques, the optical steering method has not reached its full potential. The maximum control torque that can be achieved for the current sail, assuming that one half of the sail is set to $\rho = 1$, while $\rho = 0$ for the other half, is $T_{\text{SRP},x} = 0.143 \text{Nm}$, thus 35 times higher than the maximum gravity gradient torque in LEO.

III. Sail Attitude Control using Discrete Reflectivity

In the following, we further demonstrate two-axis attitude control using discrete reflectivity regions on the surface. Instead of varying $\rho$ in the interval $[0, 1]$, the electro-chromic coatings are now restricted between two states, either ‘on’ ($\rho_{\text{max}} = 1$) or ‘off’ ($\rho_{\text{min}} = 0$). This is achieved by introducing a boundary line between the ‘on’ and ‘off’ states, used to separate regions of high and low reflectivity, as shown in figure 4. When distributing controlled regions of high and low reflectivity across the surface, a wide range of torques can be generated in the sail-plane, however, torques perpendicular to the surface are not possible.

![Figure 4. Square solar sail with discrete reflectivity region controlled by moving a boundary line between two states, ‘on’ (specular reflection) and ‘off’ (diffuse reflection), and torques created about the in-plane sail axes](image)

The on/off boundary-line is described through a linear function

$$y_{\text{BL}}(x) = ax + b \quad (8)$$

in the $(xy)$-plane of the sail, with an arbitrary slope coefficient $a$ and offset coefficient $b$, describing its vertical offset from the sail $x$-axis. Furthermore, two geometrically mirrored on/off cases can be chosen for the electro-chromic coatings above and below the boundary line. The first case represents an active reflectivity above the boundary-line and inactive below (further named as the ‘upper case’), or vice versa, the second case indicates reflectivity ‘off’ above $y_{\text{BL}}$ and ‘on’ below (named as the ‘lower case’). Switching between the two cases only changes the sign of the torques, not their magnitude. The SRP torques now depend on the two coefficients $a$ and $b$, the local cone angle $\alpha$ (i.e. the current sail attitude), and the considered on/off case. In $x$ and $y$-components, the SRP torques are now written.
when assuming the 'upper case', thus only the electro-chromic coatings above the boundary-line are active. When the RCDs are switched into the 'lower case', the limits of the inner integral in \( y \)-direction need to be inverted to \([-L/2, ax+b]\), cf. figure 4, which is equivalent to changing the signs of the torques. As mentioned above, when using this attitude control concept, no torques about the sail \( z \)-axis, normal to the surface, can be generated.

When integrating equation (9), seven torque cases have to be considered separately, depending on the chosen reflectivity-line coefficients and thus, on the shape of the active region on the sail surface. Each case can be generated.

In order to demonstrate the concept, a sample square sail configuration, with edge length \( L = 100 \) m and total mass \( m = 200 \) kg, is now considered. The sail is ideally assumed to be rigid, with mass moments of inertia \( I_{xx} = I_{yy} = 1.67 \times 10^9 \) kg m\(^2\) and \( I_{zz} = 3.34 \times 10^9 \) kg m\(^2\). The achievable torques as a function
of the reflectivity-line coefficients $a$, $b$ and for increasing cone angle are shown in figure 6, with the electrochromic elements activated in the 'lower case'. As can be seen, this activation case creates a positive $T_x$ over the entire $(a,b)$ domain, while the magnitude decreases for increasing cone angle. The maximum torque is created for $(a, b) = (0, 0)$, when all electro-chromic coatings on the lower half of the sail are active. In $y$-direction, the achievable torques mainly depend on the slope $a$ of the reflectivity-line and only to a very limited extent on the coefficient $b$. In addition, also negative torques can be created, which is not possible in the $x$-direction for the selected 'lower case'. The maximum torques about both sail axes are found to be $T_{\text{max}, x} = T_{\text{max}, y} = \pm 0.57$ Nm, which occurs when all coating elements on one half of the sail are active. For example, applying this torque on the given sample sail results in a full rotation of 360 deg in approx. 1900 s $\approx 32$ min.

All seven torque cases over the selected $(a,b)$-domain are visible in figure 7 through the use of colored regions, showing both torque components for a sail cone angle of $\alpha = 0$ deg and an active 'upper case' reflectivity distribution. The solid lines indicate $T_x$ and the dashed lines indicate $T_y$. From the figure, the feasible torques for each chosen reflectivity line in terms of $a$ and $b$ can be obtained. It is visible that no arbitrary torques about both sail axis can be generated, even when staying below $T_{\text{max}}$ for a chosen sail configuration.
Figure 6. In-plane sail torques over reflectivity-line coefficients a and b and as function of sail cone angle $\alpha$. 

(a) Torque in sail x-direction

(b) Torque in sail y-direction
A. Sail Attitude Maneuvers using Discrete Reflectivity

The described attitude control concept of employing discrete reflectivity regions across the sail surface is now applied to change the attitude of a sail in a Sun-centered orbit from a chosen initial attitude towards Sun-pointing, using combined torques $T_x$ and $T_y$ in the sail plane. The attitude dynamics of the sail are described using Euler’s Equation in quaternion notation.\textsuperscript{5,7} In the present analysis, it is assumed that attitude changes are not affecting the sail’s Sun-centered orbit, thus the orbit and attitude motion are decoupled. Choosing quaternions for attitude representation is beneficial compared to other attitude descriptors such as Euler angles, since quaternions have one redundant parameter (no singularities) and offer a lower computational effort (no trigonometric functions).\textsuperscript{8,9} Accordingly, the governing differential equation system (DES) of the rotational motion of a rigid body can be written as

$$\dot{\bar{q}} = \frac{1}{2} \bar{q} \otimes \bar{\omega}$$  \hspace{1cm} (13)

representing the first derivative of the attitude quaternion $\bar{q}$ due to the angular velocity $\bar{\omega}$. Furthermore, the second derivative of the quaternion due to an external torque $\mathbf{T}$ about the body axes follows as

$$\ddot{\bar{q}} = \dot{\bar{q}} \otimes \bar{q}^{-1} \otimes \dot{\bar{q}} + \frac{1}{2} \bar{q} \otimes \dot{\bar{\omega}} \quad \text{with} \quad \dot{\bar{\omega}} = \left([I]^{-1} (\mathbf{T} - \bar{\omega} \times [I] \bar{\omega})\right)$$  \hspace{1cm} (14)

with $[I]$ the mass moments of inertia tensor and $\otimes$ representing the quaternion product.\textsuperscript{8} The upper (\textsuperscript{\textcircled{\textdegree}}) denotes a quaternion vector

$$\bar{q} = q_1 + q = \cos \left(\frac{\theta}{2}\right) + \mathbf{a} \cdot \sin \left(\frac{\theta}{2}\right)$$  \hspace{1cm} (15)

with rotation angle $\theta$ and axis of rotation $\mathbf{a}$ with respect to a defined reference frame. Throughout this work, the so called ecliptic reference frame $(x_E, y_E, z_E)$ is used, centered in the sail’s CoM, as can be seen in
value problem of the form sail's Sun-centered orbit, and \( \mathbf{x}_E \) completes the right-handed coordinate system.

The above DES represents a system of second order differential equations and is formulated as an initial value problem of the form

\[
\ddot{q} = f(\dot{q}, \dot{\omega}, t), \quad \ddot{q}(t = t_0) = \ddot{q}_0, \quad \dot{\omega}(t = t_0) = \dot{\omega}_0
\]

The system is solved using a Runge-Kutta Nyström (RKN) integration scheme. A constant torque will be used to rotate the sail from its initial to final attitude (bang-bang control). Halfway during the maneuver, when the sail attitude has rotated over an angle \( \theta/2 \), the sign of the torque is inverted to decelerate the motion until the final attitude is reached. After selecting the required sail torques \( (T_x, T_y)_{\text{req}} \), the corresponding reflectivity-line coefficients as a function of current sail attitude can be found through the formulation of an inverse problem approach.

### B. Inverse Problem Approach for Reflectivity-Line Control

When re-writing the torque equation (11) and (12) for the coefficients \( a \) and \( b \), the reflectivity-line can be expressed as a function of the (required) torques and the current cone angle \( \alpha \). Given here for torque case 1 only, the inverse problem results in

**Case 1**

\[
a \geq 0 \land \frac{L}{2}(a - 1) \leq b \leq \frac{L}{2}(1 - a) \quad \text{or} \quad a \leq 0 \land -\frac{L}{2}(a + 1) \leq b \leq \frac{L}{2}(a + 1)
\]

\[
a = 12 \frac{T_{y,\text{lower}}}{p_0 L^2 \cos^2 \alpha}
\]

\[
b = \pm \frac{L}{2} \sqrt{1 + \frac{8 T_{x,\text{lower}}}{p_0 L^2 \cos^2 \alpha} - \frac{48 T_{y,\text{lower}}^2}{(p_0 L^2)^2 \cos^4 \alpha}}
\]

with the following conditions on the two torque components

\[
-\frac{1}{12} \leq T_{y,\text{lower}} \leq 0
\]

\[
-\frac{1}{8} \left( \cos^2 \alpha - \frac{48}{\cos^2 \alpha} T_{y,\text{lower}}^2 \right) \leq T_{x,\text{lower}} \leq 3 T_{y,\text{lower}} + \frac{48}{\cos^2 \alpha} T_{y,\text{lower}}^2
\]

Consequently, after selecting the required torques that satisfy the maximum achievable limits for a given sail and the previous conditions of equation 18, the shape and position of the reflectivity-line in order to create these torques can now be found for a sail attitude towards the Sun, or cone angle, respectively.

### C. Sample Sail Attitude Maneuver

The inverse problem solution is now applied to perform a basic sail maneuver. Initially, the sail is chosen to be tilted over a cone angle \( \alpha_{\text{init}} = 40 \) deg and clock angle \( \delta_{\text{init}} = 52 \) deg, as shown in figure 8. This translates into a rotation angle \( \theta_x = 38 \) deg and \( \theta_y = 12 \) deg about the sail \( x \) and \( y \)-axis. After the maneuver, the sail shall be Sun-pointing, thus \( \alpha_{\text{final}} = 0 \). From the quaternion approach, it follows that the axis of rotation is \( \mathbf{a} = (-0.3, -0.1, 0) \). This axis can be obtained from the initial attitude quaternion that is calculated from the initial displacement angles \( \theta_x \) and \( \theta_y \). Therefore, a constant torque pair of \( T_x = -0.3 \) Nm and \( T_y = -0.1 \) Nm is selected so that the total torque vector matches the initial displacement of the sail with respect to the ecliptic reference frame. Since the torque \( T_x \) is negative, the 'upper case' distribution needs to be used, according to figure 7. For the selected initial cone angle, the achievable torques over the \( (a, b) \)-domain of the reflectivity-line are visible in figure 9, for an active 'upper case' reflectivity distribution. The solid lines again indicate \( T_x \) and the dashed lines indicate \( T_y \). Red points identify the two feasible \( (a, b) \)-sets for the
selected torques, as calculated from the inverse problem in section III B. They both require the same slope of the reflectivity-line, however, a positive or negative offset in \( y \)-direction can be chosen. Furthermore, from Equation (17) of the inverse problem, the reflectivity-line coefficients are now fully determined as a function of the local cone angle during the maneuver, as shown in figure 10. When adapting the reflective region across the surface during the maneuver according to the derived control law for the reflectivity-line, the in-plane torques acting on the sail can be kept constant, although the light incidence angle (cone angle) and thus the SRP forces are varying during the rotation. The sail attitude is now computed through the DES of rotational motion, equation (14), using the integration method described in equation (16). The resulting time history of the cone angle and angular rates \( \omega_x \) and \( \omega_y \) of the sail about the in-plane body axes are shown in figure 11, together with the applied bang-bang torque profile. The total maneuver time to rotate the sail into Sun-pointing attitude is \( 1216 \text{s} \approx 20 \text{ min} \).
In-plane sail torques $T_x$ (solid lines) and $T_y$ (dashed lines) as function of reflectivity-line coefficients $a$ and $b$ and sail cone angle $\alpha = 40$ deg. Red dots indicate feasible sets $(a, b) = (0.45, \pm 0.59)$ for the required maneuver torques.

A variable reflectivity distribution across the surface of a solar sail film has been proposed to investigate flexible steering for solar sails without the use of mechanical systems. The surface reflectivity can be manipulated when distributing electro-chromic elements across the sail film that change their reflectivity according to an applied electric potential. First, a continuous linear reflectivity function was employed to control the attitude of the sail in low Earth orbit under the influence of gravity-gradient torques. It was shown that a constant Sun-pointing attitude can be maintained along the orbit, while only a very low value of the reflectivity is needed. This is beneficial, since currently developed electro-chromic coatings are not yet capable of adapting their optical properties arbitrarily between diffuse and fully specular reflection. Furthermore, a discrete concept using controlled regions of active reflectivity across the surface has been
employed to enable two-axis attitude control of a solar sail. When controlling the boundary-line between two regions of specular and diffuse reflection, a wide range of in-plane torque-vector directions can be generated, depending on the shape and position of the boundary-line on the surface. Since the torque magnitude depends on the light incidence angle between the sail and the Sun, an analytic control law has been derived that maintains a constant torque even when the sail is rotating during maneuver phases. The control law moves the boundary-line across the surface, depending on the current sail attitude with respect to the Sun. The concept has been demonstrated by maneuvering the sail from its initial attitude towards Sun-pointing. The proposed concepts introduce a more flexible and potentially lightweight attitude control method to large gossamer spacecraft and hereby represent major opportunities for future highly-integrated 'smart' spacecraft with on-board autonomy.
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