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1 **Theoretical analysis of a regenerative supercritical carbon dioxide**
2 **Brayton cycle/organic Rankine cycle dual loop for waste heat**
3 **recovery of a diesel/natural gas dual-fuel engine**

4
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14
15 **ABSTRACT:** Supercritical carbon dioxide Brayton cycle is considered one of the most
16 promising systems for waste heat recovery of engines because of its compactness and
17 high energy efficiency. To further improve the fuel utilization ratio and solve the
18 difficulties of waste heat recovery of high temperature exhaust gas, a regenerative
19 supercritical carbon dioxide Brayton cycle/organic Rankine cycle dual loop is proposed
20 for cascade utilization of exhaust heat from a dual-fuel engine. The regenerative
21 supercritical carbon dioxide Brayton cycle of the proposed system is powered by the
22 waste heat contained in the exhaust gas. The working fluid in the organic Rankine cycle
23 is pre-heated by CO₂ exiting the regenerator and then further heated by the residual heat
24 of the exhaust gas. The flow rates of the working fluids in both sub cycles are adjusted
25 to match the waste heat recovery system to respond to the changing conditions of the
26 dual-fuel engine. The results revealed that the maximum net power output of this
27 system is up to 40.88 kW, thus improving the dual-fuel engine power output by 6.78%.

28 Therefore, such a regenerative supercritical carbon dioxide Brayton cycle/organic
29 Rankine cycle dual loop system design enables the thorough recovery of high
30 temperature exhaust heat, leading to higher energy efficiency and lower fuel
31 consumption of the engine.

32 **Key words:** Supercritical carbon dioxide Brayton cycle; Organic Rankine cycle; Dual-
33 fuel engine; Waste heat recovery; Thermodynamic performance

34

35 **Introduction**

36 The increased prominence of the energy crisis and environmental pollution problems,
37 has led to the search for solutions such as finding alternative fuels or improving fuel
38 utilization ratio. For the former, hydrogen, which can be produced from biomass
39 gasification effectively [1], has immense potential for application. For the latter,
40 engines as one of the main consumers of fuel have attained extensive attention. In terms
41 of dual-fuel engines, approximately 30%–45% of fuel energy is converted into useful
42 work, while the remaining energy is released into the atmosphere in the form of heat
43 through exhaust gases, jacket water, and lubrication oil. Generally, there are two ways
44 to improve energy efficiency of a dual-fuel engine: The first is to optimize the internal
45 structure and combustion process of the dual-fuel engine, and the other is to capture
46 and reclaim waste heat. As structure and combustion technologies have been optimized
47 to their best potential, it becomes harder to achieve further improvement using these
48 methods. In contrast, the high temperature of the exhaust gas makes waste heat recovery

49 (WHR) one of the best energy saving technologies for more efficient fuel usage to help
50 improve the environment.

51 Recently, WHR of engine has been studied widely by both experiment and simulation.
52 The organic Rankine cycle (ORC) has immense applicability because of its capability
53 for low temperature heat recovery, compactness, and low erosion. Studies on ORC have
54 focused on various factors that affect its performance, such as selection of organic
55 working fluids, optimization of cycle parameters, and comparison among different
56 layouts. Thurairaja et al. [2] and Scaccabaraozee et al. [3] analyzed the suitable scopes
57 of different organic working fluids to achieve the best match between organic working
58 fluids and working conditions. Additionally, Abadi et al. [4] summarized the advantages
59 and issues of using zeotropic mixtures in ORC and the results showed that in
60 comparison with pure fluids, zeotropic mixtures would increase exergy efficiency by
61 decreasing the irreversibility in the heat exchangers. Braimakis et al. [5] confirmed that
62 adding a regenerator can improve ORC efficiency. Moreover, BMW proposed the dual-
63 loop cycle (called turbosteamer cycle) driven with a 1.8-liter BMW four-cylinder to
64 achieve higher energy efficiency [6]. To find a better match and reduce the temperature
65 difference between the working fluid and the heat source, supercritical and transcritical
66 ORCs were proposed in the WHR area because they did not undergo liquid-gas phase
67 transition in heat exchangers. Li et al. [7] studied the performance of subcritical and
68 transcritical ORCs using R1234ze driven by 100-200 °C hot water. Results showed that
69 transcritical ORC showed higher system efficiency and was suitable for higher
70 temperatures compared with subcritical ORC. Mohammadkhani et al. [8] adopted a

71 transcritical dual loop ORC to recover the waste heat of diesel engines. The results
72 showed that the best performance was achieved using toluene and R143a in the high
73 and low-temperature loops, respectively. At the same time, supercritical ORC has been
74 rapidly developed because of its lower exergy loss and higher energy efficiency. The
75 effect of condensation temperature [9] and organic working fluids [10] on supercritical
76 ORC had been investigated. Moreover, Moloney et al. [11] presented a parametric
77 analysis of a regenerative supercritical ORC. Braimakis et al. [12] compared
78 supercritical and transcritical ORCs with different working fluids. Results showed that
79 supercritical ORC in mixtures exhibited better thermodynamic performance for
80 temperatures above 170 °C. In diesel/natural gas dual-fuel engines, the maximum
81 temperature of the exhaust gas approximately ranges from 720 to 870 K when they are
82 operated under a medium/high operating load [13], while the decomposition
83 temperatures of most working fluids are below 600 K. On account of the decomposition
84 issue of organic working fluids, ORC application is limited in the field of engine WHR.
85 Furthermore, the size and weight of the turbine need to be considered, because of which
86 ORC has not been applied in automobile engine WHR although it has been investigated
87 and tested for a long time. The supercritical carbon dioxide Brayton cycle (SCBC) was
88 proposed by Fether [14] and Angelino [15] because carbon dioxide is environment
89 friendly and noninflammable and has good chemical stability, a low critical point, high
90 specific heat capacity, and high heat transfer efficiency. As the performance of heat
91 exchangers and turbines has improved, the SCBC, which is more suitable for high
92 temperature WHR than supercritical ORC, has gradually become a hotspot of research.

93 Various SCBC layouts were proposed in the past two decades. Crespi et al. [16]
94 organized the numerous cycles in different categories and compared the claimed
95 performance of each cycle. Li et al. [17] presented the advantages and classifications
96 of SCBCs and theoretically and experimentally analyzed their application in various
97 industries. Zhu et al. [18] compared different direct-heated SCBCs integrated with a
98 solar thermal power tower system. Results showed that the intercooling SCBC achieved
99 the highest overall efficiency. Sarkar [19] explored the effects of cycle parameters on
100 supercritical carbon dioxide recompression Brayton cycle (SCRBC) and found that the
101 irreversibility of heat exchangers was much higher than that of the turbomachinery.
102 Kim et al. [20] focused on the influence of pinch point temperature difference on the
103 irreversibility of heat exchangers and cycle efficiency. Park et al. [21] analyzed the
104 application of SCRBC in various small reactors and investigated the effects of channel
105 shape of printed circuit heat exchangers (PCHEs) on pressure drop. They proved that
106 using airfoil fin type PCHE may increase the thermal efficiency by about 1.0% in
107 comparison with zigzag type PCHE. Although the layouts, operating parameters, and
108 components of simple SCBC had been optimized, its energy efficiency is relatively low
109 due to the high temperature of carbon dioxide entering the cooler. Therefore, multi-loop
110 layouts have been adopted to take full advantage of the remaining energy to raise
111 specific power. Manente et al. [22] studied the application of cascaded SCBCs in
112 biomass. The results revealed that a maximum biomass to electricity conversion
113 efficiency of 36% can be achieved by the cascaded configuration, which was 4.7%
114 higher than that of the simple cascaded system using the same boiler design. Wang et

115 al. [23] indicated that the total product unit cost of SCBC/ORC was slightly lower than
116 that of supercritical carbon dioxide Brayton cycle/transcritical carbon dioxide Brayton
117 cycle (SCBC/TCBC). Exergoeconomic analysis and optimization of SCRBC/ORC
118 were made by Akbari [24]. The results indicated that the highest exergy efficiency and
119 the lowest product unit cost for SCRBC/ORC were obtained when Isobutane and
120 RC318 were used as the ORC working fluids, respectively. Singh et al.[25]
121 comprehensively analyzed the energy and exergy of SCBC/ORC combined cycle
122 driving solar parabolic trough collectors and showed that R407c combined cycle
123 obtained the maximum exergy and energy efficiency.

124 With the maturity of SCBC, some scholars and companies attempted to apply it to
125 engine WHR in recent years. Song et al. [26] adopted a preheating SCBC to recover
126 jacket cooling water and the waste heat of a diesel engine. The findings showed that the
127 improved preheating SCBC based system for WHR increased the engine power output
128 by 6.9%. The performance of regenerative SCBC (RSCBC)/ORC and SCRBC/ORC
129 was discussed and analyzed [27]. Uusitalo et al. [28] investigated the electricity
130 production potential of SCBCs for engine WHR with different operational conditions
131 and working fluids. They concluded that the working fluids and cycle operational
132 parameters not only significantly influenced the thermodynamic cycle design but also
133 highly affected the optimal rotational speed and geometry of the turbomachines.
134 Several studies focused on SCBC for engine WHR, however, a diesel engine was used
135 to explore the effect of a single parameter on cycle performance under a single engine
136 condition. Due to the high temperature exhaust gas of diesel/natural gas dual-fuel

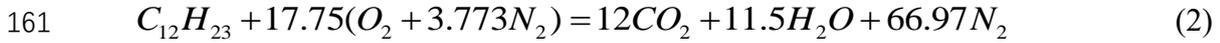
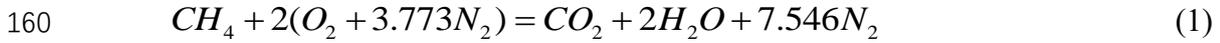
137 engine, no study has focused on its WHR. In this study, a novel RSCBC/ORC dual loop
138 cycle is proposed and discussed for WHR of a diesel/natural gas dual-fuel engine, which
139 has been shown to be a more potential system for its better thermodynamic performance
140 compared with RSCBC and its excellent thermal stability compared with ORC. The
141 design of such a dual loop cycle enables not only the cascade utilization of the waste
142 heat of the dual-fuel engine but also the thorough use of the residual heat of the high
143 temperature cycle (HT cycle). Moreover, the energy and exergy of this dual loop cycle
144 under different working conditions of the dual-fuel engine are assessed to better match
145 the changing conditions of the dual-fuel engine, which can provide reference for its
146 practical application and design of control system. The optimization of multiple
147 parameters and the selection of organic working fluids are also discussed.

148

149 **2. System description**

150 YC6MK375DN is selected as the dual-fuel engine in this study. The speed of the engine
151 was kept constant at 1500 rpm, while its load was varied under different conditions.
152 Four different conditions were considered, and the main parameters are shown in Table
153 1. Under the assumption that the dual-fuel engine burns completely, the exhaust gas is
154 mainly assumed to be composed of N_2 , CO_2 , H_2O , and O_2 . The mass percentage of each
155 of component is calculated using the chemical reaction equation of complete
156 combustion, as shown in Table 2. Next, the specific heat capacity and enthalpy of the
157 exhaust gas can be obtained by REFPROP. In this study, natural gas and diesel are

158 simplified to pure methane (CH₄) and C₁₂H₂₃, respectively. Their complete reaction
 159 equation can be expressed as follows:



162 Table 1 Main parameters of the dual-fuel engine

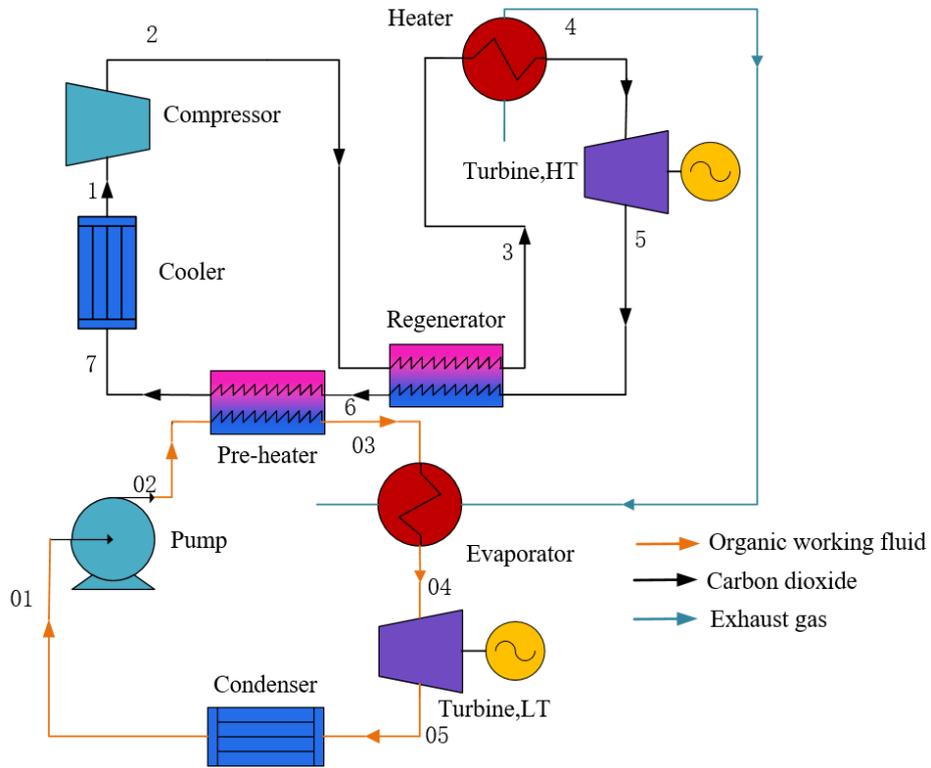
Torque (N·m)	800	1200	1400	1600
Engine power output (kW)	126.8	189	220.8	251.1
Engine efficiency (%)	34.0	38.9	40.7	41.6
Exhaust temperature (°C)	423.2	452.3	463.8	488.3
Exhaust mass flow rate (kg/h)	825	1006	1074	1139

163

164 Table 2 Composition of the exhaust gas

Torque (N·m)	N ₂ (%)	H ₂ O (%)	CO ₂ (%)	O ₂ (%)
800	74.29	6.97	9.08	9.66
1200	74.11	7.47	9.59	8.83
1400	73.98	7.87	10.04	8.11
1600	73.85	8.25	10.48	7.42

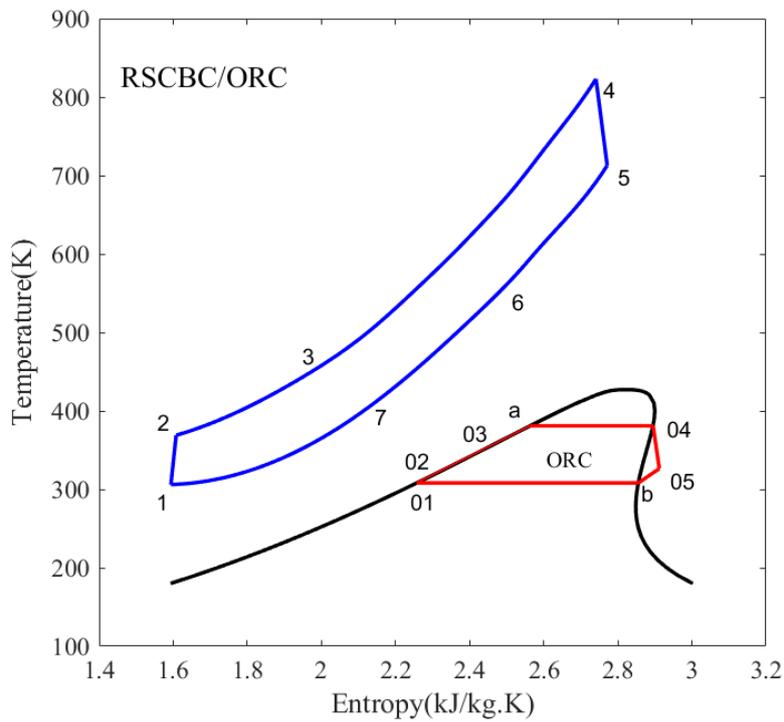
165 A schematic diagram of the WHR system is shown in Fig. 1. The system consists of a
 166 RSCBC and an ORC with a pre-heater. The RSCBC is composed of a compressor,
 167 heater, turbine, regenerator, and cooler. The CO₂ exiting from the compressor is heated
 168 by the regenerator and heater in series. The high temperature S-CO₂ stream expands in
 169 the turbine, and the high temperature expanded stream heats the compressed S-CO₂ and
 170 organic working fluid in series and then returns to the cooler. In ORC, the organic
 171 working fluid at the outlet of the pump is pre-heated by the residual heat of CO₂ exiting
 172 from the regenerator and then is further heated by the exhaust gas in the evaporator.
 173 This design enables thorough utilization of the exhaust gas. The T-S diagram of this
 174 WHR system is shown in Fig. 2.



175

176

Fig. 1 Schematic diagram of RSCBC/ORC dual-loop cycle



177

178

Fig. 2 T-S diagram of the RSCBC/ORC dual-loop cycle

179 **3 Model design and validation**

180 A program developed based on MATLAB and the REFPROP database is adopted to
181 analyze the thermodynamic performance of the system. REFPROP is a reference fluid
182 thermodynamic and transport properties database, which implements reference
183 equations of state for many refrigerants and can be used to calculate all fluid properties
184 [29].

185 *3.1 Thermodynamic model*

186 The following assumptions are applied for modelling:

- 187 (1) The whole system is operated at a steady state condition;
- 188 (2) Changes in the kinetic and potential energies of the fluids are negligible;
- 189 (3) Both heat loss and pressure drops in the pipelines and heat exchangers are negligible;
- 190 (4) The temperature of the exhaust gas is higher than the acid dew point after heat
191 transfer, and the acid dew point is assumed to be 120°C.

192 The following thermodynamic modelling is based on the first and the second law of
193 thermodynamics:

194 HT cycle:

195 1-2 is the compression process in the compressor:

$$196 \quad \eta_{comp} = \frac{h_{2,s} - h_1}{h_2 - h_1} \quad (3)$$

$$197 \quad W_{comp} = m_{CO_2}(h_2 - h_1) \quad (4)$$

198 2-3 and 5-6 are the heat recovery processes in the regenerator:

$$199 \quad h_3 - h_2 = h_5 - h_6 \quad (5)$$

$$200 \quad \varepsilon_{rec} = \frac{T_5 - T_6}{T_5 - T_2} \quad (6)$$

201 3-4 is the endothermic process in the heater:

202
$$Q_{in,HT} = m_{CO_2}(h_4 - h_3) \quad (7)$$

203 4-5 is the expansion process in the turbine:

204
$$W_{tur,HT} = m_{CO_2}(h_4 - h_{5,s})\eta_{tur,HT} \quad (8)$$

205 6-7 is the heat transfer process between the HT cycle and the low temperature (LT)
206 cycle:

207
$$Q_{exc} = m_{CO_2}(h_6 - h_7) \quad (9)$$

208 7-1 is the cooling process in the cooler:

209
$$Q_{cool} = m_{CO_2}(h_7 - h_1) \quad (10)$$

210 LT cycle:

211 01-02 is the compression process in the pump:

212
$$\eta_{pump} = \frac{h_{02,s} - h_{01}}{h_{02} - h_{01}} \quad (11)$$

213
$$W_{pump} = m_f(h_{02} - h_{01}) \quad (12)$$

214 02-03 is the heat transfer process in the pre-heater:

215
$$Q_{in,LT1} = m_f(h_{03} - h_{02}) = m_{CO_2}(h_6 - h_7) \quad (13)$$

216 03-04 is the endothermic process in the evaporator:

217
$$Q_{in,LT2} = m_f(h_{04} - h_{03}) \quad (14)$$

218 04-05 is the expansion process in the turbine:

219
$$W_{tur,LT} = m_f(h_{04} - h_{05,s})\eta_{tur,LT} \quad (15)$$

220 05-01 is the condensation process in the condenser:

221
$$Q_{cond} = m_f(h_{05} - h_{01}) \quad (16)$$

222 The net power output of the dual-loop cycle:

223
$$W_{net} = (W_{tur,HT} - W_{comp}) + (W_{tur,LT} - W_{pump}) \quad (17)$$

224 The total heat absorbed by the dual-loop cycle:

$$225 \quad Q_{in} = Q_{in,HT} + Q_{in,LT2} \quad (18)$$

226 The energy efficiency of the dual-loop cycle:

$$227 \quad \eta_{th} = W_{net}/Q_{in} \quad (19)$$

228 Because kinetic and potential energies are neglected in this system, the incomplete
229 equilibrium state is selected as the reference state. Only physical exergy is considered
230 for exergetic analysis.

$$231 \quad E = E_{ph} = m[(h - h_0) - T_0(s - s_0)] \quad (20)$$

232 The total exergy input of the dual-loop cycle:

$$233 \quad E_{in} = E_{fin} - E_{final} \quad (21)$$

234 Here, E_{fin} is the exergy of the exhaust gas at the beginning, and E_{final} is the exergy
235 of the exhaust gas after two heat exchangers.

236 The exergy efficiency of the dual-loop cycle:

$$237 \quad \eta_{ex} = W_{net}/E_{in} \quad (22)$$

238 The main parameters of the dual-loop cycle and organic working fluids are shown in
239 Table 3 and Table 4, respectively.

240 Table 3 Main parameters of the dual-loop cycle

Parameters	value
Turbine efficiency in HT cycle (%)	93 ^[30]
Compressor efficiency in HT cycle (%)	89 ^[30]
Recuperative ratio (%)	95 ^[30]
Pinch point temperature difference in evaporator and heater (K)	30
Pinch point temperature difference in other heat exchangers (K)	5
Pump efficiency in LT cycle (%)	70 ^[27]
Turbine efficiency in LT cycle (%)	80 ^[27]

241

242 Table 4 Main properties of different working fluids.

Working fluid	Molecular mass	Critical temperature (C)	Critical pressure (MPa)	Safety group	ODP	GWP
CO ₂	44.01	30.98	7.38	A1	0.000	1
R600	58.12	152.0	3.80	A3	0.000	~20
R601	72.15	196.6	3.37	A3	0.000	~20
R601a	72.15	187.2	3.38	A3	0.000	~20
R601b	72.15	160.6	3.20	-	0.000	~20
R1233zd(E)	130.5	165.6	3.57	A1	0.000	4.5
R245ca	134.05	174.4	3.93	-	0.000	726

243 3.2 Model validation

244 Because there is no published literature about such a RSCBC/ORC dual-loop cycle,
245 the established RSCBC and ORC need to be independently verified. Table 5 indicates
246 that the efficiency error for RSCBC is 2.25%, whereas that for ORC ranges from 0.05%
247 to 7.16% mainly because of the different versions of MATLAB and REFPROP, along
248 with the differences in pinch point temperatures and the degree of superheat. These
249 results demonstrate that the simulation results of both RSCBC and ORC agree well,
250 thus providing a basis for using the present combined cycle model for further analysis
251 of the performance of the proposed system.

252 Table 5 Comparison of the present calculated results with the published literature

Cycle	Working fluid	Reference	Energy efficiency in reference	Energy efficiency calculated	Error
RSCBC	CO ₂	Manente ^[22]	36.87%	36.04%	-2.25%
ORC	Benzene	Vaja ^[31]	19.86%	19.85%	-0.05%
	R11		16.58%	16.11%	-2.83%
	R113		8.52%	7.91%	-7.16%

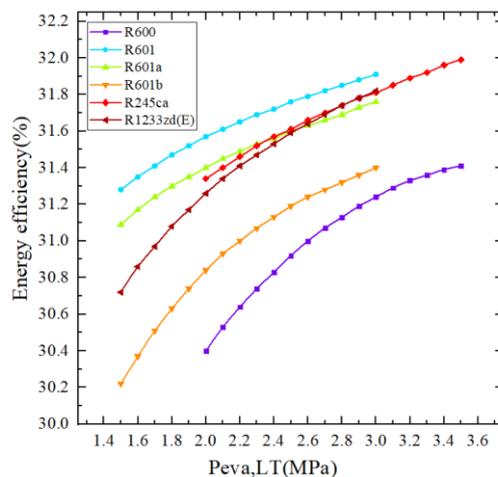
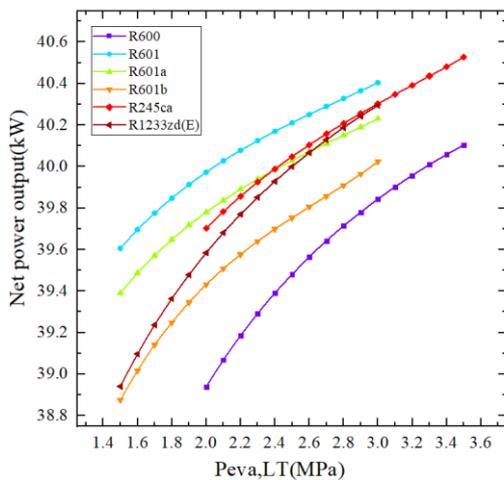
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254 4 Results and discussion

255 Based on the verified combined cycle model, the thermodynamic performance of
 256 the proposed WHR system will be analyzed from three aspects including the selection
 257 of working fluids, the matching of engine conditions, and the optimization of cycle
 258 parameters in the following sections.

259 4.1 Selection of working fluids in organic Rankine cycle

260 With respect to the Rankine cycle, the properties of the working fluids significantly
 261 influence cycle performance. According to the slope of the saturated vapor line in the
 262 T-S diagram, the organic working fluids can be classified into three categories: dry fluid,
 263 isentropic fluid, and wet fluid [32]. Dry and isentropic fluids are preferred as low or
 264 medium temperature heat sources because they can avoid the occurrence of liquid
 265 hammer in the expansion process without any degree of superheat. Furthermore, the
 266 security, ODP, GWP, and other parameters of working fluids also need to be considered.
 267 Based on the above-mentioned factors, R600, R601, R601a, R1601b, R245ca and
 268 R1233zd(E) are selected for performance comparison to obtain the most suitable
 269 working fluid based on the thermodynamic performance of the dual loop cycle.



270

Fig. 3 (a) Changes in net power output with evaporating pressure in the LT cycle

Fig. 3 (b) Changes in energy efficiency with evaporating pressure in the LT cycle

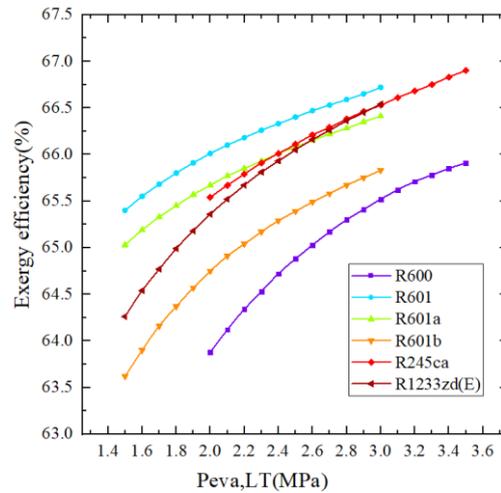


Fig. 3 (c) Changes in exergy efficiency with evaporating pressure in the LT cycle

271

272

273

In this part, the engine speed and torque are fixed to 1500 rpm, 1600 N·m, respectively.

274

The evaporating pressure in the LT cycle varies while the other parameters are fixed.

275

With respect to the HT cycle, $T_{min,HT} = 32$ °C, $P_{min,HT} = 7.45$ MPa, and $T_{max,HT} = 430$ °C.

276

As shown in Fig. 3, the net power output, energy and exergy efficiencies of all the

277

selected working fluids all increase with increase in evaporating pressure $P_{eva,LT}$ in the

278

LT cycle. Among them, R601 and R600 present the maximum and minimum net power

279

output, energy and exergy efficiencies, respectively. When $P_{eva,LT}$ is relatively low,

280

R601 presents the best thermodynamic performance, followed by R601a, R245ca,

281

R1233zd(E), R601b and R600. In the medium $P_{eva,LT}$, R601a, R245ca and R1233zd(E)

282

present the similar thermodynamic performance.

283

4.2 Effect of engine condition

284

In response to the changing conditions, the thermodynamic performance of the

285

proposed dual loop cycle is evaluated under different maximum pressures in the HT

286

cycle and under different evaporating pressures in the LT cycle. In this part, the engine

287

speed is fixed to 1500 rpm and the torques are 800, 1200, 1400, and 1600 N·m. The

288

maximum pressure of the HT cycle ($P_{max,HT}$) and the evaporating pressure of the LT

289 cycle ($P_{eva,LT}$) vary, while the other parameters are fixed. With respect to the HT cycle,
290 $T_{min,HT} = 32\text{ }^{\circ}\text{C}$, $P_{min,HT} = 7.45\text{ MPa}$, and $T_{max,HT} = 380\text{ }^{\circ}\text{C}$. Comprehensively considering
291 the security, environmental protection and thermodynamic performance, R1233zd(E)
292 is chosen as the organic working fluid in the LT cycle.

293 As shown in Fig. 4, once the dual-fuel engine is operated at a steady condition, the net
294 power output of the dual loop cycle increases with $P_{max,HT}$, and its speed of increase
295 gradually decreases. On the one hand, both the enthalpy difference (h_4-h_5) of the
296 expansion process in the HT cycle and that of the compression process in the HT cycle
297 (h_2-h_1) increase as $P_{max,HT}$ increases. Furthermore, the increment in enthalpy difference
298 of the expansion process in the HT cycle is higher than that of the compression process
299 in the HT cycle. On the other hand, the mass flow rate of S-CO₂ (m_{CO_2}) decreases with
300 increasing $P_{max,HT}$, which results in a higher net power output. The dominant position
301 of enthalpy difference ($h_4-h_5-h_2+h_1$) between the expansion and compression processes
302 in the HT cycle is weakened, which leads to a decrease in the growth rate of the net
303 power output. As $P_{max,HT}$ is fixed, the mass flow rate of the organic working fluid (m_f)
304 decreases with the increase of $P_{eva,LT}$. The enthalpy difference ($h_{02}-h_{01}$) of the
305 compression process in the LT cycle varies slightly and that of the expansion process
306 in the LT cycle increases. When $P_{max,HT}$ is below 22MPa, the increment in the enthalpy
307 difference ($h_{04}-h_{05}-h_{02}+h_{01}$) between the expansion and compression processes in the
308 LT cycle is sufficient to offset the decreasing of m_f initially. As a result, the net power
309 output of the dual loop cycle increases. When $P_{max,HT}$ is higher than 22MPa, the
310 enthalpy difference in the LT cycle maintains the leading position first and then it is

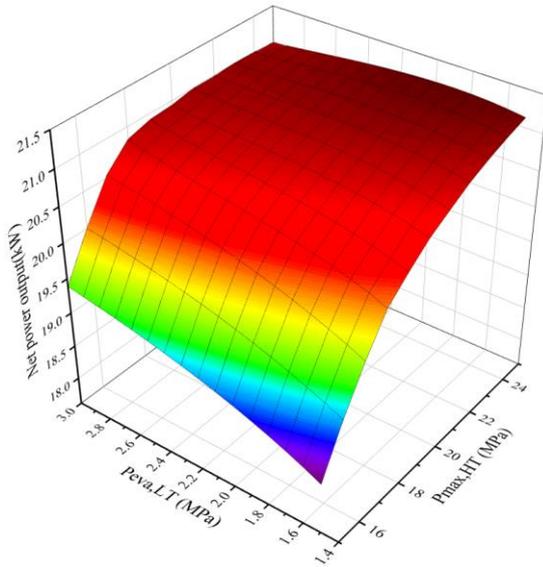
311 replaced by the m_f with the increase of $P_{eva,LT}$, which results in the net power output

312 increases first and then decreases. When $P_{max,HT}$ increases simultaneously, the m_f

313 decreases, thus the peak of the net power output appears at a lower $P_{eva,LT}$.

314

315



316

317

Fig.4 (a) 800N·m/1500rpm

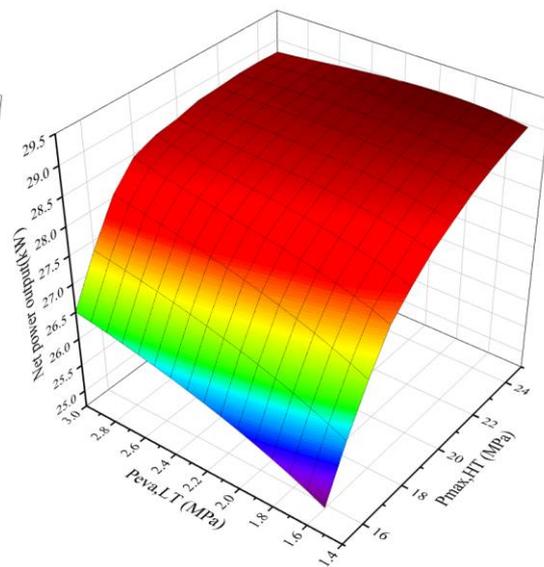
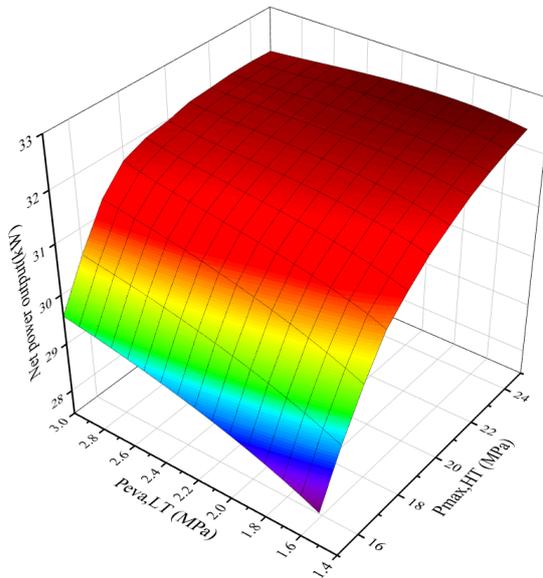


Fig.4 (b) 1200N·m/1500rpm

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Fig. 4 (c) 1400N·m/1500rpm

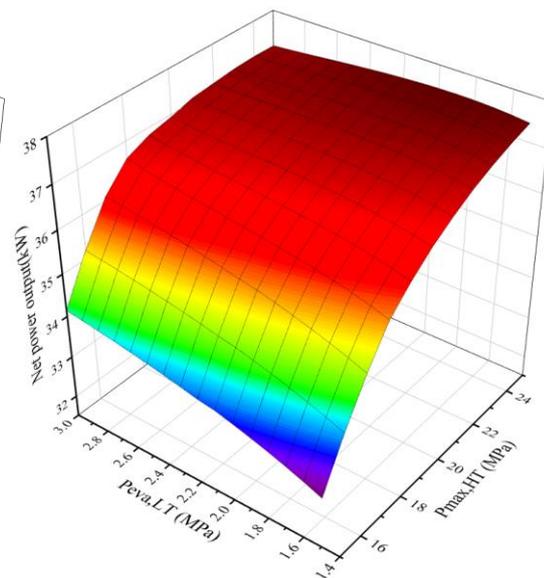


Fig. 4 (d) 1600N·m/1500rpm

321 Fig. 4 Net power output changes with evaporating pressure and maximum pressure under

322

different conditions

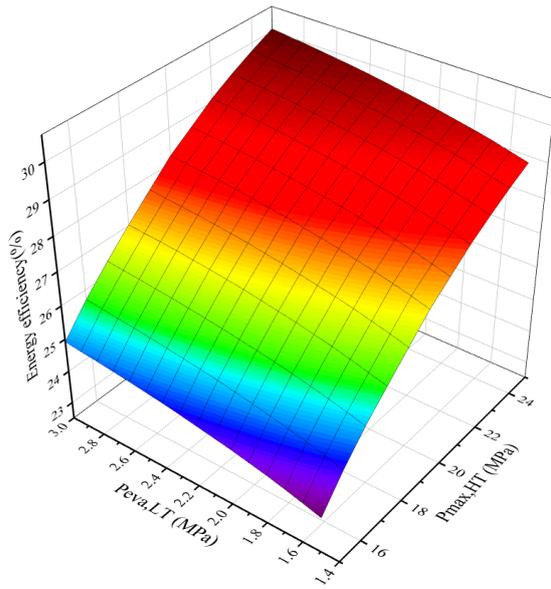
323 For the dual-fuel engine, more heat is available and its quality improves because both
 324 the exhaust temperature and its mass flow rate increase with the increase of torque, as
 325 shown in Table 1. This leads to an increase in m_{CO_2} and m_f based on the heat balance
 326 in the heater and evaporator. Once the parameters of the dual loop cycle are fixed, the
 327 enthalpy difference of each process remains the same and can be determined. Thus, the
 328 net power output elevates as m_{CO_2} and m_f increase. Based on the above-mentioned
 329 reasons, the net power output elevates with an increase of torque when the engine speed
 330 is fixed. Selecting the net power output as the evaluation index, the optimal value of
 331 the double pressures and its maximum net power output under different conditions are
 332 shown in Table 6.

333 Table 6 The maximum net power output and energy efficiency corresponding to the optimal
 334 pressures

Torque	800N·m	1200N·m	1400N·m	1600N·m
$P_{max,HT}$ (MPa)	25	25	25	25
$P_{eva,LT}$ (kPa)	1900	1900	1900	1900
Net power output (kW)	21.2037	29.0446	32.4308	37.4996
Energy efficiency of engine with WHR (%)	39.69	44.88	46.68	47.81

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336



337

Fig. 5 (a) 800 N·m/1500 rpm

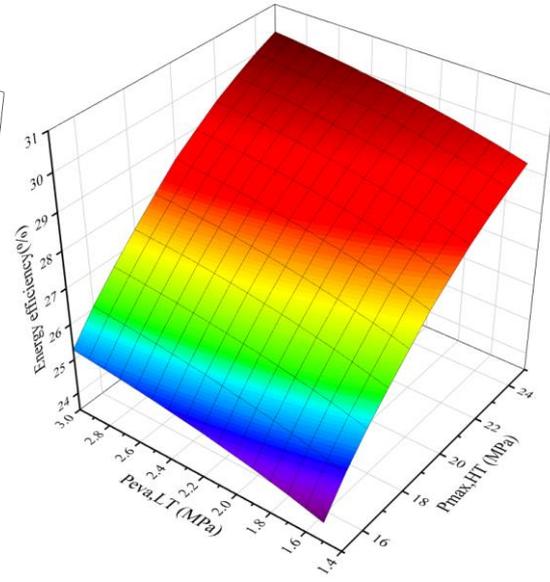
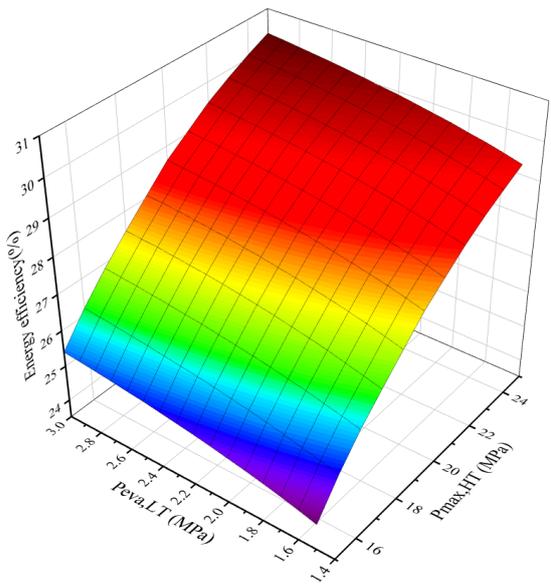


Fig. 5 (b) 1200 N·m/1500 rpm

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Fig. 5 (c) 1400 N·m/1500 rpm

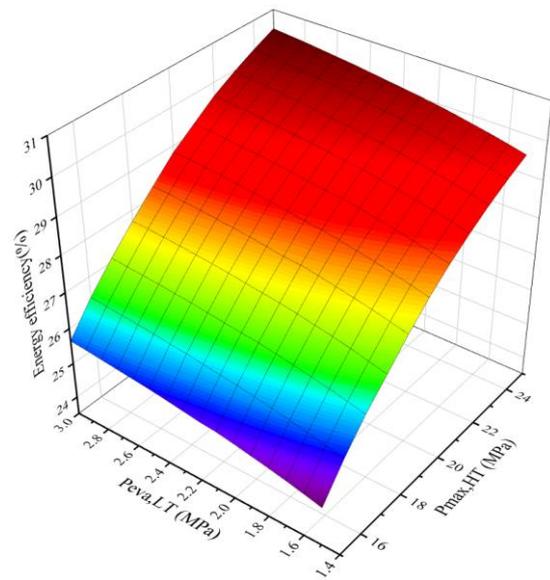


Fig. 5 (d) 1600 N·m/1500 rpm

342

343 Fig. 5 Energy efficiency changes with evaporating pressure and maximum pressure under different
344 conditions

345 Fig.5 shows the effect of evaporating pressure and maximum pressure on energy

346 efficiency. As shown in Fig. 5, when the engine is operated at a steady state condition,

347 the energy efficiency of the dual loop cycle increases as $P_{max,HT}$ increases, which can be

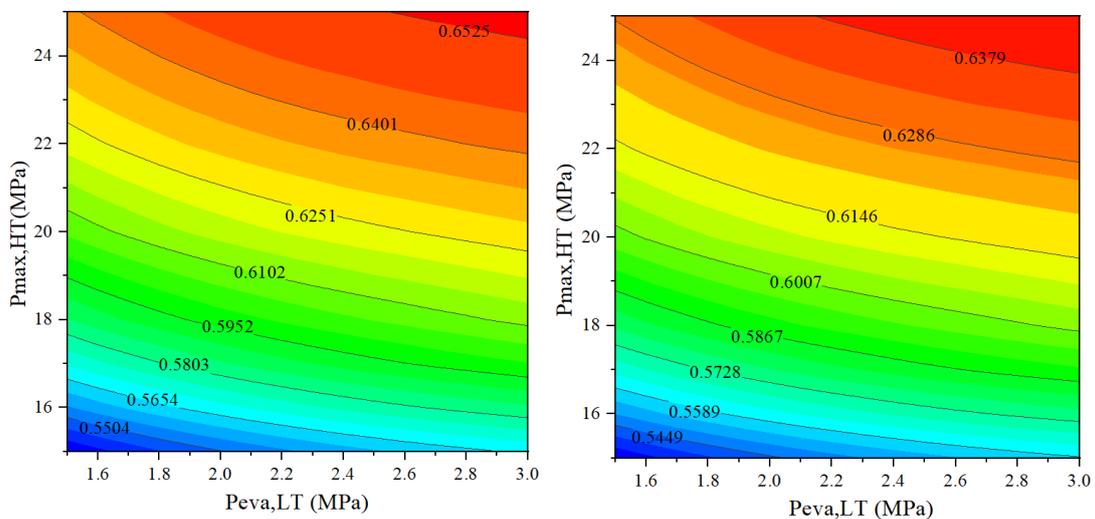
348 explained by the fact that the heat absorbed by the dual-loop cycle keeps approximately
349 constant first and then decreases with increasing $P_{max,HT}$ while the net power output
350 increases. The heat absorbed by the dual loop cycle stays constant with the increase of
351 $P_{eva,LT}$ when $P_{max,HT}$ is below 18MPa, while it decreases when $P_{max,HT}$ is higher than
352 18MPa. Therefore, both the net power output and the heat absorption show that the
353 energy efficiency of the dual loop cycle is elevated as $P_{eva,LT}$ increases. As the engine
354 condition varies, the energy efficiency increases as torque increases, which is mainly
355 caused by the increase of m_{CO_2} and m_f . The maximum energy efficiencies at torques
356 of 800, 1200, 1400, and 1600 N·m are 30.07%, 30.28%, 30.36%, and 30.50%,
357 respectively.

358 As shown in Fig. 6, when the engine is running at a steady state, the exergy efficiency
359 of the proposed WHR system increases with the increase of $P_{max,HT}$. The main reason
360 for this phenomenon is that the net power output increases while the exergy input to the
361 WHR system keeps constant first and then decreases. Fig.6 shows that the exergy
362 efficiency also increases as $P_{eva,LT}$ increases. With the increase of $P_{eva,LT}$, the evaporating
363 temperature of the LT cycle increases, which decreases the temperature difference
364 between the organic working fluid and the heat source, including both S-CO₂ and the
365 low temperature exhaust gas separately. Thus, the irreversibility of the pre-heater and
366 evaporator in the LT cycle reduces, and exergy efficiency can be enhanced. As the
367 engine conditions vary, the exhaust temperature increases with the increase of torque,
368 which augments the temperature difference between S-CO₂ and the high temperature
369 exhaust gas, thus increasing the irreversibility of the heater in the HT cycle and

370 ultimately resulting in the decline of exergy efficiency. The maximum exergy
 371 efficiencies for torques of 800, 1200, 1400, and 1600 N·m are 65.48%, 64.24%, 63.77%,
 372 62.81%, respectively.

373 Fig. 7 depicts the exergy loss of each component for $P_{max,HT} = 25$ MPa and $P_{eva,LT} = 3000$
 374 kPa under different conditions. As torque increases, the percentage of exergy loss of the
 375 heater in the HT cycle increases, while that of the evaporator in the LT cycle shows the
 376 opposite trend. In addition, the percentage of exergy loss of the regenerator and cooler
 377 fluctuates in a small range. The total exergy loss of the dual loop cycle increases as the
 378 torque increases. Under certain conditions, the heat exchangers including the evaporator,
 379 heater, cooler, condenser, regenerator, and pre-heater mainly contribute to the total
 380 exergy loss, which approximately accounts for 72% of the total exergy loss. Therefore,
 381 it is critical to reduce the irreversibility of the heat exchangers for improving exergy
 382 efficiency. Notably, the exergy loss of turbines approximately accounts for 17% to 21%
 383 of the total exergy loss, which can be explained by the relatively large pressure ratio
 384 leading to the increase of irreversibility during the non-isentropic expansion process.

385



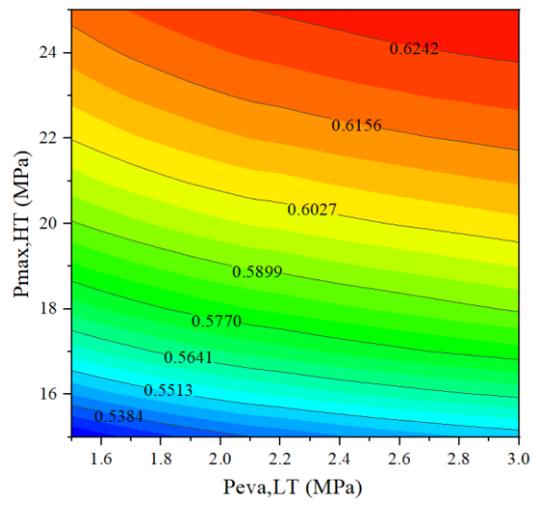
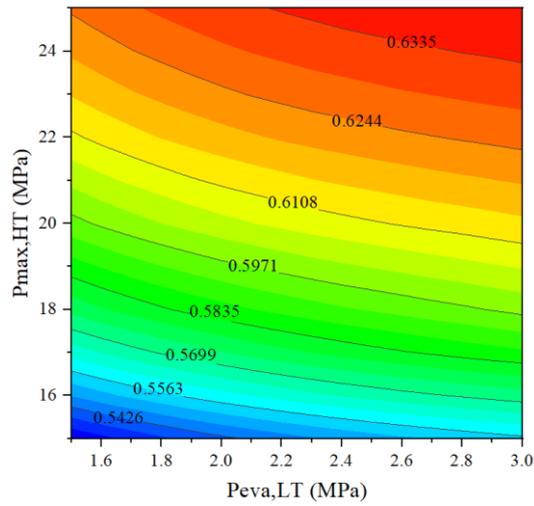
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Fig. 6 (a) 800 N·m/1500 rpm

Fig. 6 (b) 1200 N·m/1500 rpm

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Fig. 6 (c) 1400 N·m/1500 rpm

Fig. 6 (d) 1600 N·m/1500 rpm

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Fig. 6 Exergy efficiency changes with evaporating pressure and maximum pressure under different conditions

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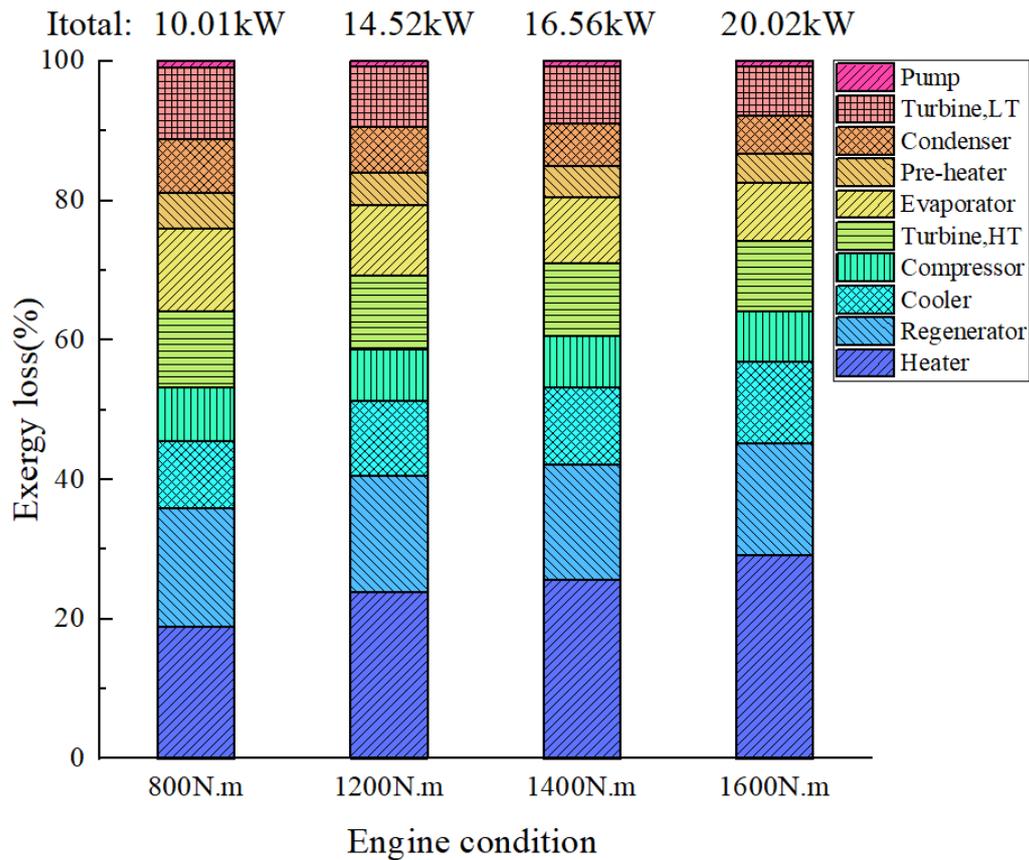


Fig. 7 Exergy loss of each component under different conditions

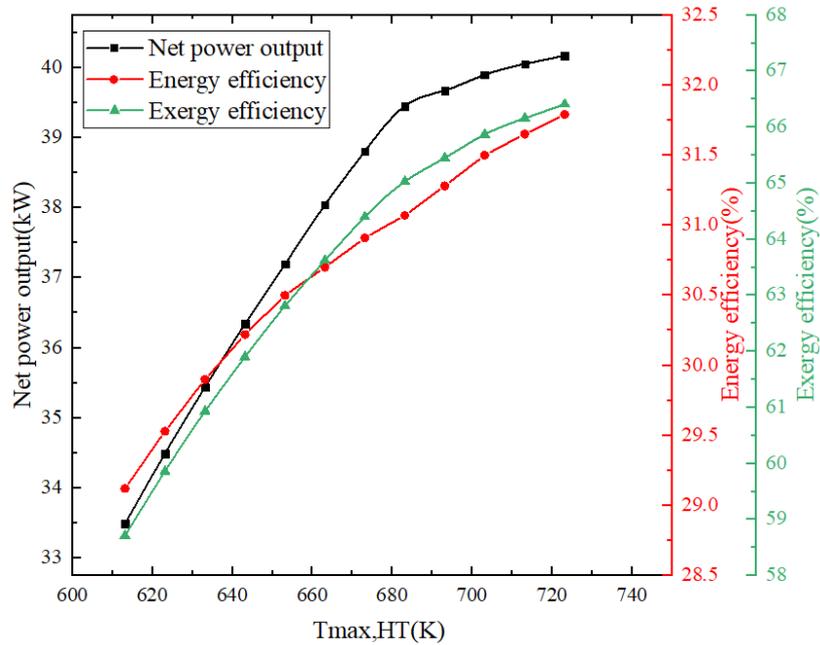
4.3 Effect of operation parameters of the high temperature cycle on the dual loop cycle

The effect of the turbine inlet temperature $T_{max,HT}$ in the HT cycle on thermodynamic performance is investigated on the premise that the engine speed and torque are fixed at 1500 rpm and 1600 N·m, respectively. With respect to the HT cycle, the minimum temperature, the minimum and maximum pressure are set to 32 °C, 7.45 MPa and 25 MPa, respectively. Meanwhile, the evaporating pressure in the LT cycle is set to 3000 kPa. As shown in Fig. 8, the net power output increases as $T_{max,HT}$ increases. With the increase of $T_{max,HT}$, m_{CO_2} declines according to the heat balance in the heater, and the enthalpy difference of the expansion process in the HT cycle increases owing to the divergence of the isobaric line, whereas that of the compression process in the HT cycle

408 remains constant, which results in an increase in the enthalpy difference ($h_4-h_5-h_2+h_1$)
409 between the turbine and compressor in the HT cycle. The enthalpy difference in HT
410 cycle is sufficient to compensate for the decrease of m_{CO_2} , which results in the
411 increase of the net power output of the HT cycle. In terms of the LT cycle, m_f
412 increases as $T_{max,HT}$ increases, and the enthalpy difference ($h_{04}-h_{05}-h_{02}+h_{01}$) between the
413 turbine and pump in the LT cycle remains constant, which results in an increase in the
414 net power output of the LT cycle. The net power output of the HT and LT cycles shows
415 that the net power output of the dual loop cycle increases. Fig. 8 shows that the energy
416 and exergy efficiencies of the dual-loop cycle follow a similar variation trend, which
417 can be explained by the variation of the net power output being higher than that of the
418 heat absorption and input exergy. When $T_{max,HT}$ is 723.15 K, the net power output,
419 energy efficiency, and exergy efficiency present the maximum value, which are 40.1706
420 kW, and 31.76%, 66.41%, respectively.

421 Fig. 9 depicts the changes in specific heat capacity of carbon dioxide with temperature
422 under different pressures. It can be seen from Fig. 9 that the specific heat capacity of
423 carbon dioxide changes greatly near the pseudo-critical point and decreases gradually
424 away from the pseudo-critical point. Besides, its peak decreases gradually with the
425 increase of pressure. As shown in Fig. 10, the net power output, energy and exergy
426 efficiencies of the dual loop cycle are also influenced by the minimum temperature
427 $T_{min,HT}$ and minimum pressure $P_{min,HT}$ in the HT cycle. Fig. 10(a) shows that when
428 $P_{min,HT}$ is below 7.7MPa, the net power output decreases as $T_{min,HT}$ increases, whereas
429 the net power output increases first and then decreases when $P_{min,HT}$ is higher than

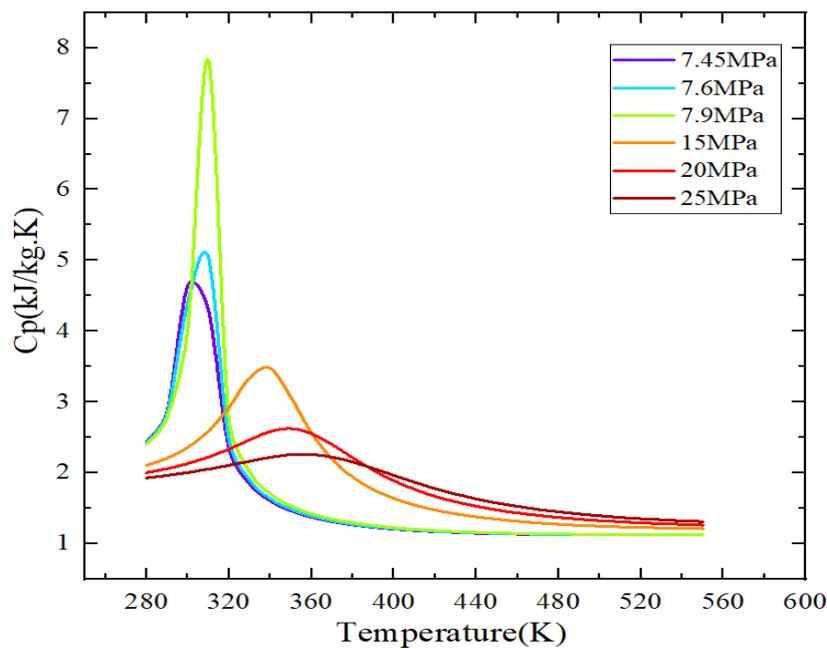
430 7.7MPa. On the one hand, both m_{CO_2} and m_f increase as $T_{min,HT}$ increases, and then
 431 the net power output in the LT cycle increases. On the other hand, the enthalpy
 432 difference of the compressor in the HT cycle increases, while that of the turbine in the
 433 HT cycle remains constant with the increase of $T_{min,HT}$.



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Fig. 8 Influence of turbine inlet temperature $T_{max,HT}$ in the HT cycle



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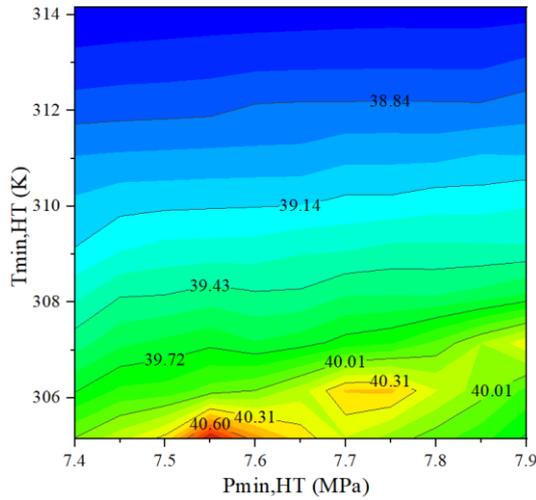
Fig. 9 Changes in specific heat capacity of carbon dioxide

438 Therefore, the net power output in the HT cycle declines with the synthetic effect of
439 mass flow rate and enthalpy difference. The net power output in the HT and LT cycles
440 determines the net power output of the dual loop cycle. Besides, Fig. 10(a) shows that
441 the net power output slightly fluctuates with increasing $P_{min,HT}$, which can be explained
442 by the fact that the variation of specific heat capacity of carbon dioxide, the net power
443 output in HT cycle increases first and then decreases when $T_{min,HT}$ varies from 304.15K
444 to 306.15K, then it increases when $T_{min,HT}$ is higher than 306.15K. And the net power
445 output in LT cycle decreases simultaneously with increasing $P_{min,HT}$. As shown in
446 Fig.10(b), the energy efficiency increases generally with the increasing $T_{min,HT}$ and the
447 decreasing $P_{min,HT}$. Meanwhile, it fluctuates slightly because the heat absorbed varies
448 greatly near the pseudo-critical point. The input exergy has the similar trend with the
449 heat absorbed, which results in the exergy efficiency changes with $T_{min,HT}$ and $P_{min,HT}$,
450 as shown in Fig.9(c). Different layouts with R1233zd(E) as the working fluid in LT
451 cycle are compared in Table 7.

452 Table 7 Comparison with different layouts with R1233zd(E) as the working fluid with the engine
453 running at 1500 rpm and 1600 N·m

Parameters	Engine WHR	without Engine	with Engine	with Engine
		RSCBC	RSCBC/ORC	
Net power output(kW)	251.1	281.47	291.88	
Overall efficiency(%)	41.6	46.63	48.38	
BSFC(g/kW·h)	178.8	159.48	153.80	

454



455

Fig. 10 (a) Changes in net power output with $T_{\min,HT}$ and $P_{\min,HT}$

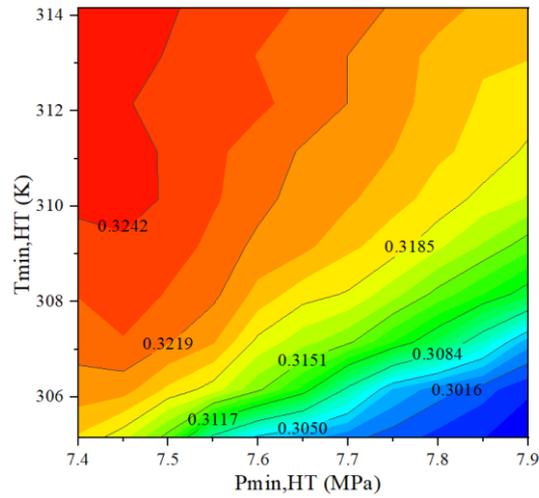
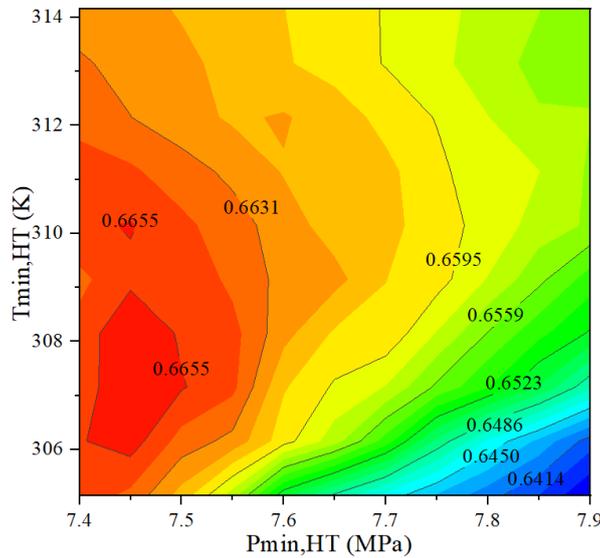


Fig. 10 (b) Changes in energy efficiency with $T_{\min,HT}$ and $P_{\min,HT}$

456



457

458

Fig. 10 (c) Changes in exergy efficiency with $T_{\min,HT}$ and $P_{\min,HT}$

459

460 5. Conclusion

461 In this paper, SCBC and ORC are adopted as the HT cycle and the LT cycle for
 462 WHR of a diesel/natural gas dual-fuel engine, respectively. The combination of these
 463 two cycles leads to thorough WHR of the dual-fuel engine via cascade utilization of
 464 energy according to temperature. Three main aspects including the matching of engine
 465 conditions, the optimization of cycle parameters, and the selection of working fluids

466 are investigated to analyze the thermodynamic performance of the proposed dual-loop
467 cycle. The main conclusions are as follows:

468 (1) The net power output of all the selected organic working fluids increases with the
469 increasing evaporating pressure $P_{eva,LT}$ in the LT cycle. The maximum net power
470 output, energy and exergy efficiencies of the dual loop cycle are obtained by
471 adopting R601.

472 (2) At a fixed speed of 1500 rpm, the net power output of the dual loop cycle increases
473 as torque increases. Furthermore, the net power output of the dual-loop cycle
474 increases with the increase of the $P_{max,HT}$, and it increases with increasing $P_{eva,LT}$
475 when $P_{max,HT}$ is below 22MPa, while it increases first and then decreases when
476 $P_{max,HT}$ is higher than 22MPa. Furthermore, the energy and exergy efficiencies
477 increase with the increase of $P_{eva,LT}$ and $P_{max,HT}$.

478 (3) A comparison of the exergy losses of each component shows that the heat
479 exchangers account for 72% of the total exergy loss. Therefore, reducing the
480 irreversibility of the heat exchangers is essential for improving exergy efficiency.
481 Notably, the exergy loss of turbines is approximately 17% to 21%, which can be
482 explained by the relatively large pressure ratio that leads to the increment of
483 irreversibility during the non-isentropic expansion process.

484 (4) The net power output, energy and exergy efficiencies of the proposed WHR system
485 all increase with the increasing $T_{max,HT}$. And the net power output decreases as
486 $T_{min,HT}$ increases when $P_{min,HT}$ is below 7.7 MPa, whereas it increases first and then
487 decreases when $P_{min,HT}$ is higher than 7.7MPa. Furthermore, the net power output

488 slight fluctuates with increasing $P_{min,HT}$ because of the variation of specific heat
489 capacity of carbon dioxide.

490 (5) The maximum net power output by adopting R1233zd(E) as the working fluid is
491 40.88kW, which shows improvement of the engine power output by 6.78%.

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496 United Kingdom.

497 **Nomenclature**

498 Abbreviations

499	ORC	organic Rankine cycle
500	SBC	supercritical Brayton cycle
501	SCBC	supercritical carbon dioxide Brayton cycle
502	TCBC	transcritical carbon dioxide Brayton cycle
503	RSCBC	regenerative supercritical carbon dioxide Brayton cycle
504	SCRBC	supercritical carbon dioxide recompression Brayton cycle
505	WHR	waste heat recovery
506	HT cycle	high temperature cycle
507	LT cycle	low temperature cycle

508

509 Symbols

510	η	efficiency
511	ε	recuperative ratio
512	s	specific entropy (kJ/kg)
513	h	specific enthalpy (kJ/kg)
514	m	mass flow rate (kg/s)
515	E	exergy (kW)
516	T	temperature (K)
517	Q	heat (kW)
518	W	work (kW)

519

520 Subscripts

521	HT	high temperature
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522	LT	low temperature
523	comp	compression
524	tur	turbine
525	exc	exchanger
526	rec	recuperator
527	cond	condensation
528	cool	cooler
529	th	thermal
530	ph	physical
531	ex	exergy
532	in	inlet
533	max	maximum
534	min	minimum

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