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A Metamaterial–Coupled Wireless Power Transfer System Based on Cubic High Dielectric Resonators

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Abstract—In this study, a metamaterial–coupled, highly–efficient, miniaturized, and long range Wireless Power Transfer (WPT) system based on a Cubic High Dielectric Resonator (CHDR) is explored. The proposed WPT system consists of two CHDR metamaterials separated by a distance and excited by two rectangular coils. Initially, this WPT system is analyzed by considering the cube dielectric permittivity, \( \varepsilon_r = 1000 \), and loss tangent, \( \tan \delta = 0.00001 \). From the Ansoft HFSS simulation, it is observed that the system operates in the hybrid resonance mode resonating as a horizontal magnetic dipole providing more than 90% power transfer efficiency at a distance of 0.1\( \lambda \). In addition, parametric studies regarding the transmitter and receiver sizes, loss tangent, receiver misorientation, cube periodicity, etc. are carried out. One of the significant findings of this parametric study reveals that the suggested WPT system is less sensitive to the displacement of the receiver coil, and the WPT efficiency due to misorientation of the receiver can be increased by changing the CHDR cube rotation. Due to inaccessibility of the very high \( \varepsilon_r = 1000 \), eighteen microwave ceramic samples of EXXELIA TEMEX E5080 (Oxide composition: Ba Sm Ti) which has a permittivity, \( \varepsilon_r = 78 \), permeability, \( \mu_r = 1 \), and a loss tangent, \( \tan \delta = 0.0004 \) was made for experimental verification. These cubes are surrounded by Teflon to make the CHDR resonators. From simulations and measurements, it is found that the proposed system outperforms the most recent high-dielectric or copper based WPT systems in terms of efficiency, range, size, and Specific Absorption Rate (SAR).

Index Terms—Cubic high dielectric resonator, hybrid resonance mode, magnetic dipole, metamaterial, rectifier, specific absorption rate, wireless power transfer.

I. INTRODUCTION

Wireless Power Transfer (WPT) makes it possible to supply power through an air gap, without the need for current-carrying wires [1]. WPT can provide power from an Alternating Current (AC) source to compatible batteries or devices without physical connectors or wires. WPT can recharge mobile phones and tablets [2], drones, cars, implantable devices [3], and even transportation equipment [4]–[5]. The concept of transferring power without wires, however, has been around since the late 1890s [6]. Since then, many research groups have been working on this problem, and different methodologies have been introduced to WPT systems. One of the issues being addressed is analyzing and optimizing the near-field inductive or magnetic resonate coupling WPT [7]–[10]. Another one is improving the power control capability and the WPT efficiency [11]–[18]. Miniaturization of the transmitter and receiver coil is also a major concern [3], [19]–[20]. Furthermore, a longer transfer distance and more flexible adaption are required for numerous mobile devices [9], [17], [20]–[21].

One of the non-radiative power transfer techniques is based on resonant coupling between the same-frequency resonators, where the power is transferred through the overlap of their near-fields. In 2007, a group from MIT experimentally transferred 60 W of power over a distance of 2 m with 45% efficiency via strongly coupled magnetic resonances between two metallic coils [7]. However, the resonance coupling based WPT system is very sensitive to the receiver and transmitter sizes, orientations and positions [22]–[23]. The possibility of omnidirectional WPT has also been explored, as opposed to the use of one direction or two directions on the same plane [24]. However, the proposed system in Ref. [24], yields only 60% efficiency at a distance of 0.013\( \lambda \), which leaves much to be desired. Recently, WPT systems based on high permittivity dielectric resonators coupling have been experimentally tested [25]–[26]. As described in Ref. [25], this high permittivity dielectric introduced a higher order Magnetic Quadruple (MQ) mode which offers high WPT efficiency even with a random orientation between the transmitter and the receiver. The same group extended their work in another study [26] by incorporating a colossal permittivity dielectric (\( \varepsilon_r = 1000 \), \( \tan \delta = 0.00025 \)) at 232 MHz. By applying an impedance matching technique, an efficiency of 50% was achieved within the separation between the resonators \( d = 16 \) cm (0.125\( \lambda \)).

To increase the power transfer efficiency, researchers have also demonstrated that a metamaterial (3D)/metasurface (2D) lens or slab can be used [13]–[14], [17]–[18], [21], [27]–[29]. Metamaterials (MTM) are artificial materials composed of engineered structures that possess peculiar electromagnetic properties not seen in natural materials, such as negative-refractive indexes and evanescent wave amplification [28], [30].
in mind that the magnetic resonant coupling based WPT is essentially coupling of evanescent waves, MTM can be used to enhance the WPT efficiency. On one hand, the efficiency of the WPT system with the MTM is considerably improved for adaptive charging. On the other hand, it can increase the flexibility of the operating range for telemetry systems, such as a farther transfer distance and larger misalignment tolerance for electronic or implantable devices [14]. In most previous studies [14], [17], [18], [21], [28], [29] a copper-based metamaterial/metasurface slab was placed between the transmitter and the receiver to improve the WPT system. However, the polarization dependence of the metamaterial poses a major drawback. Furthermore, copper-based metamaterials introduce ohmic losses at very high frequency and lower the quality factor (Q-factor) of the system as well as the efficiency. In contrast, resonant dielectric structures operating as Dielectric Resonator Antennas (DRAs) via displacement currents can be virtually free from ohmic loss, making them intrinsically highly efficient [25]–[26]. Furthermore, sub-wavelength DRAs with moderate permittivities ($\varepsilon_r > 5$) can efficiently support different modes of resonance [25]. One important and useful mode is pure magnetic resonance, which cannot be obtained with single-layer metallic resonators.

In this study, a metamaterial-coupled, highly-efficient, miniaturized, and long range WPT system based on Cubic High Dielectric Resonator (CHDR) is explored. The CHDR is a metamaterial with cubic high dielectric resonators in a cubic lattice embedded in a low dielectric background. This metamaterial was proposed by Kim et al. [31] in which the authors made use of a combination of Mie resonance and Bragg scattering to achieve the metamaterial properties [32]–[33]. Since, the efficiency of WPT systems has been improved with high permittivity dielectric coupling [26], and it is expected that the WPT efficiency can be further improved by using all-dielectric metamaterial coupling. To the best of our knowledge, there are no previous studies regarding high dielectric metamaterial–coupled WPT system. This paper is composed as follows. Section II analyzes the suggested WPT system by considering the unit cell of the CHDR, and CHDR metamaterial properties, and by characterizing the MTM-coupled WPT system. A comparison among previous studies and this study in terms of efficiency, WPT system size, and loss tangent variations is also included in this section. Parametric studies of the MTM-coupled WPT system are discussed. The influence on WPT efficiency owing to parameters such as the cube lattice periodicity, separation between the transmitter and CHDR, transmitter and receiver sizes, number of arrays, and receiver misalignment are addressed in Section III. Section IV comprises the experimental demonstration of the proposed WPT system. Two CHDR metamaterials were made by using eighteen high-dielectric cubes ($\varepsilon_r = 78$, tan$\delta = 0.0004$) surrounded by Teflon. The Specific Absorption Rate (SAR) is numerically calculated and improvement in WPT efficiency in the presence of a saline phantom for the proposed WPT system is experimentally demonstrated. Finally, the versatility of the proposed WPT system is presented by taking into account the receiver misalignment.

II. ANALYSIS OF THE PROPOSED WPT SYSTEM

A schematic of the proposed WPT system is shown in Fig. 1. The system consists of two rectangular CHDR metamaterial resonators separated at a distance, $d$. For clarification, the WPT system will be divided into the following three sections: a) unit cell consideration, b) CHDR metamaterial characterization, and c) WPT system characterization.

A. Unit Cell Consideration

1) Theoretical Background: The proposed WPT system along with the unit cell of the CHDR structure are shown in Fig. 1. Theoretically, a rectangular cavity resonator with metal wall has the resonant frequencies given by:

$$f_{mn} = \frac{1}{2\sqrt{\varepsilon\mu}} \left( \frac{m}{s} \right)^2 + \left( \frac{n}{t} \right)^2 + \left( \frac{p}{w} \right)^2.$$  \hspace{1cm} (1)

Where integers $m$, $n$, and $p$ denote the number of half wave variations in the $x$, $y$, and $z$ directions, respectively, and $s$, $t$, and $w$ represent the dimensions of the rectangular cavity, respectively. If a cubic cavity resonator is chosen, then all lengths are equal, which means $s = t = w$. In case of a such cavity resonator, all the lowest order modes such as TM110, TE011, and TE101 have same field patterns or frequency, and referred as the degenerate modes. The resonant frequency of these degenerate modes is:

$$f = \frac{1}{2\sqrt{\varepsilon\mu} w}.$$  \hspace{1cm} (2)

In case of a high dielectric resonator, boundary conditions at the walls can be considered as an open circuits [31], hence, resonant frequencies of the modes can also be approximated by Eqs. (1) and (2). It is found that if a unit cell simultaneously undergoes electric and magnetic resonances might demonstrate a polarization-invariant response due to superimposition of the two resonant modes [34]. The cubic high dielectric resonator has degenerate TE and TM modes due to cubic nature of
the 3D structure according to Eq. (1). Therefore, the CHDR is supposed to be less sensitive to the polarization of the incident wave in the $z$-direction (Fig. 1(a)). As a result, the proposed WPT system shows superior performance due to receiver misalignment, which will be addressed in the later section.

2) HFSS simulation: Initially, the cube size is chosen as $w = 15$ mm, having a permittivity $\varepsilon_r = 1000$, and $\tan \delta = 0.00001$. This high dielectric cube is surrounded by a low dielectric (Teflon) substrate with a periodicity (or, lattice constant), $p = 19$ mm. The resonant frequency $f$ of the lowest order modes for the above-mentioned CHDR resonators can be theoretically approximated based on the formulae given in Eq. (2), which gives us a resonant frequency of $f = 447.1$ MHz. To verify the theoretical approximation, an Ansys HFSS model is established, as shown in Fig. 2(a). Using the finite-element solver of HFSS, the resonant frequency ($f$) calculated under normal incidence. Taking advantage of the symmetry of the problem, the unit cell of the CHDR metamaterial was analyzed by applying two PMC and two PEC boundaries on the sides of the unit cell. The simulated resonant frequency was $f = 476.8$ MHz, which is very close to the calculated resonant frequency of $f = 447.1$ MHz according to the approximation in Eq. (2). The simulated reflection coefficient ($S_{11}$) is plotted and this plot indicates that, if a small loop is placed in the vicinity of the unit cell, $f$ shifts to a higher frequency, as depicted in Fig. 2(b).

B. CHDR Metamaterial Characterization

In general, CHDR metamaterials (MTM) are composed of periodic arrangements of high dielectric elements in a low dielectric background. The periodicity ($p$) of the unit cell controls the macroscopic resonance or the Bragg resonance, and the lattice resonance, whereas the microscopic resonance is due to the individual unit cell characteristics and is known as the Mie resonance. The combination of these two resonances give rise to a negative refractive index [35]. According to Fig. 1, two CHDR structures with height $h = 36$ mm, $p = 19$ mm, and thickness $t = 19$ mm made of a $2 \times 2$ array of high dielectric ceramic cube enclosed in a low dielectric (Teflon) background are considered. The MTM properties of the CHDR structure can be obtained by using a similar unit cell simulation setup (Fig. 2(a)), however, the unit cell should be replaced by the $2 \times 2$ CHDR array. The matrix elements $S_{11}$, $S_{12}$, $S_{21}$, and $S_{22}$ are referred as the scattering parameters or the $S$-parameters. The parameters $S_{11}$, $S_{22}$ have the meaning of reflection coefficients, and $S_{12}$, $S_{21}$ define as the transmission coefficients. The $S$-parameters are related to both the refractive index ($n$) and the impedance ($z$). Therefore, extraction of parameters such as effective permittivity ($\varepsilon_{eff}$), effective permeability ($\mu_{eff}$), and refractive index ($n$) are calculated based on the following equations [31]:

$$z = \pm \sqrt{\frac{(1 + S_{11})^2 - S_{21}^2}{(1 - S_{11})^2 - S_{21}^2}},$$

$$e^{i n d} = \frac{S_{21}}{1 - S_{11}[(z - 1)/(z + 1)]},$$

$$\varepsilon_{eff} = n/z, \quad \text{and} \quad \mu_{eff} = n \cdot z,$$

where, $k_o$ and $d$ denote the wave number and thickness of the metamaterial slab, respectively. The extracted real and imaginary parts of the effective permittivity and permeability are plotted in Fig. 3. A negative real part of either (or both) of these parameters enhances the evanescent wave amplification, whereas, the imaginary part controls the loss associated with the system [14]. Figs. 3(a) and (c) represent the real part, whereas Figs. 3(b) and (d) indicate the imaginary part of the effective permittivity and permeability, respectively. The region covered by the rectangular box is the negative refractive index region. In this portion of the plot, the real parts of both $\varepsilon_{eff}$ and $\mu_{eff}$ become negative, and the imaginary parts are close to zero. Hence, the CHDR structure acts as a metamaterial with a negligible amount of loss.

C. MTM Coupled WPT System Characterization

To realize the WPT system, the CHDR metamaterial is excited by using a simple square loop. The loop has dimensions of $30$ mm $\times$ $30$ mm with a thickness of $3$ mm, as shown in Fig. 1. A feed/port with an impedance of $50$ $\Omega$ was placed in the loop and a separation of $s = 4$ mm was selected between the loop and the CHDR structure. The distance ($d$) between the CHDR was $50$ mm ($\approx 0.1\lambda$, and more than three times higher than the cube size, $w = 15$ mm). Under the simulation setup shown in Fig. 1, resonance occurs around $f = 560$ MHz, which lies in the negative refractive index zone (rectangular box portion) of Fig. 3. The reflection ($S_{11}$) and the transmission ($S_{21}$) coefficients are plotted in Fig. 4(a). A maximum WPT efficiency ($\eta$) of more than 91% was found according to Fig.
Fig. 3. Extracted parameter for the CHDR structure: (a) Real effective permittivity. (b) Imaginary effective permittivity. (c) Real effective permeability. (d) Imaginary effective permeability.

4(a), and $\eta$ can be calculated based on the either of following equations [26]:

$$\eta = \frac{|S_{21}|^2}{1 - |S_{11}|^2}. \quad (6)$$

$$\eta = |S_{21}|^2. \quad (7)$$

In general, the WPT efficiency based on Eq. (6) approximates the maximum achievable WPT efficiency, whereas, Eq. (7) calculates the efficiency in a given situation. For a perfectly matched WPT system, Eqs. (6) and (7) yield an almost identical maximum WPT efficiency, as visualized in Fig. 4(a).

According to the Mie theory under a proper excitation, a high refractive index dielectric exhibits very strong magnetic resonances. Owing to the high dielectric contrast between free space and high dielectric, excitation of the CHDR resonator is expected to lead to strong localization of energy. To understand the above statement, the magnetic (H) and electric (E) field distributions are plotted in Fig. 4(b). As expected, the E and H fields are strongly confined in each cube inside the CHDR. The E field is swirling inside a CHDR cube, whereas, the H field, which lies perpendicular to E, is penetrating inside and out of the CHDR structure. The field distributions correspond to the hybrid resonance mode resonating as a horizontal magnetic dipole (MD) [36]–[37]. The hybrid resonance is one that is usually considered to originate from the very strong interactions between the elements in the unit cell [38]. In the plasmonic nano-structures, the horizontal magnetic–dipole–mode is used to build efficient surface plasmon polariton (SPP) couplers [36], whereas, in this study, this mode has been applied to introduce an efficient WPT system. Fig. 4(c) represents the horizontal magnetic ($|H|$) dipole mode coupling for the proposed WPT system. The efficiency, %

Fig. 4. (a) Characteristics of the proposed WPT system in terms of $\eta$, $|S_{11}|$, and $|S_{21}|$. (b) Magnetic ($|H|$) and electric ($|E|$) field distributions of the MTM-coupled WPT system. (c) Horizontal magnetic ($|H|$) dipole mode coupling for the proposed WPT system.

system with a metamaterial slab) in that energy is localized in modes intrinsic in dielectric objects rather than engineered resonances in objects such as coils or antennas. As magnetic field coupling occurs between two CHDR metamaterials, therefore, it is not necessary to design a sophisticated coil or antennas. We can use arbitrary non-resonant coils to excite or extract
It is well-known that the WPT efficiency in free space falls off rapidly when the operating distance \( d \) is larger than the largest size of the resonator [21]. Fig. 5(b) depicts the variations of \( \eta \) for different array and resonator sizes. The working WPT distance \( (d) \) was normalized by the associated array or resonator size. Considering only the cube size \( (w = 15 \, \text{mm}) \) and periodicity \( p = 19 \, \text{mm} \), no significant difference in efficiency was observed. Nonetheless, in comparison with the size (diameter \( D = 84 \, \text{mm} \)) of the cylindrical resonator proposed in [26], the improvement in WPT efficiency for the CHDR MTM is noteworthy. Furthermore, when the whole 2 × 2 CHDR array size (length or width = 36 mm) is considered, the proposed CHDR MTM array still performs much better than the cylindrical resonator for the same normalized distance. Numerically, an efficiency of more than 75% can be obtained when the separation between the CHDRs is twice as much as the array size under the matched condition, which, in contrast, indicates a more than 50% improvement in the WPT efficiency to the study in [26].

The WPT system efficiency was obtained at tan\( \delta = 0.00001 \), which is difficult to achieve in reality. Hence, variations of efficiency in terms of the loss tangent are indicated in Figs. 5(c) and (d) for both the MD and MTM–MD modes. For simulation, the distance \( d = 50 \, \text{mm} \), and permittivity \( \varepsilon_r = 1000 \) were selected for each case. As expected from Fig. 5(c), a significant reduction in efficiency as well as in bandwidth occurs when the tangent loss increases. However, the drop of efficiency in the MTM–MD mode is higher than the MD mode according to Fig. 5(d), and the WPT efficiency is less than the 20%, even when tan\( \delta = 0.01 \) for the MTM–MD mode. This is due to fact that the CHDR structure in the MTM–MD mode contains multiple small resonators, and losses in each resonator become significant when tan\( \delta \) increases as compared to losses in a single dielectric resonator in the MD mode. Nonetheless, based on the high dielectric material used in [26], which has a permittivity of 1000 and a loss tangent of 2.5e\(-4\) at 1 MHz, the proposed MTM-coupled WPT system is expected to have a maximum efficiency of more than 80% for the proposed MTM coupled WPT system at a distance of 0.1\( \lambda \).

### III. Parametric Study

According to Fig. 1, there are several parameters that can influence the performance of the proposed WPT system. It is obvious from Eq. (1) that, by increasing the permittivity \( \varepsilon_r \) and/or cube size \( (w) \), the resonance frequency can be reduced. Therefore, in this section, the effect of other parameters such as periodicity \( (p) \), separation \( (s) \), variations in the MTM array and transmitter/receiver size will be addressed. It is important to mention that, the effect of changing different parameters of the CHDR structure on the MTM properties are discussed in [31]. This study mainly focuses on the MTM-coupled WPT system, therefore, how the aforementioned parameters affect the whole WPT system (e.g., \( S_{11} \) and/or \( \eta \)) will be investigated.

#### A. Variation in Periodicity \( (p) \) and Separation \( (s) \)

Figs. 6(a) and (b) represent the variations in WPT efficiency due to changes in periodicity \( (p) \) and separation \( (s) \), and the
corresponding simulation parameters are indicated in each plot. According to Fig. 6(a), when the periodicity ($p$) increases, the resonant frequency of the proposed WPT system shifts to a lower frequency, and the maximum $\eta$ for each case remains almost the same. However, a reduction in WPT efficiency bandwidth (BW) was observed with increments in $p$. This reduction in BW is indicated by drawing a black dashed line along the $x$-axis at 50% WPT efficiency. Similar results were found due to a change in periodicity of the CHDR structure by Kim et al. Furthermore, the separation ($s$) between the transmitter/receiver and the CHDR also influences the resonant frequency and BW. Fig. 6(b) indicates that the resonant frequency of the proposed WPT system can be tuned by adjusting the distance ($s$) [26]. It is observed that, depending on the transmitter/receiver size ($l$), for each distance ($d$), there is an optimum separation ($s$), at which $\eta$ is the maximum. Furthermore, the separation ($s$) is increased with an increasing distance ($d$), and the value of $s$ should not be more than the resonator size ($w$) at short distances ($\leq 0.1\lambda$).

### B. Variation in Transmitter/Receiver Size and Number of Arrays

It is important to minimize the transmitter/receiver size for various applications. As an example, nowadays, WPT in implantable devices is becoming more popular, which requires a smaller transmitter or receiver size. Variation in the transmitter and receiver size (length) as well as their corresponding efficiency is plotted in Fig. 6(c). It is interesting to observe that there is almost no change in the maximum efficiency ($\approx 90\%$) when both the transmitter and receiver length are gradually reduced from 30 mm to 15 mm. In addition, reduction in length of the excitation element also reduces the bandwidth as well as the resonant frequency. However, a notable alteration in resonant properties and reduction in efficiency were found as soon as the length decreases below 15 mm, which happens to be equal to the cube resonator length, $w = 15$ mm. Hence, the resonator size plays an important role in determining the maximum separation distance ($s$) and minimum transmitter/receiver size ($l$) to obtain the maximum WPT output for the proposed system. Another necessary parametric study is the number of MTM arrays, as it is significantly affects the power transfer distance. A comparison between $2 \times 2$ and $3 \times 3$ arrays is revealed in Fig. 6(d). According to this plot, the $3 \times 3$ array shows a significant improvement in $\eta$ beyond the $0.3\lambda$ transfer distance as compared to the $2 \times 2$ array. This finding is identical to the study in [29]. As a consequence, the number of MTM arrays can be adjusted in accordance with the required transfer distance.

### C. Receiver Misalignment

An efficient WPT system should be able to transfer power even if a misalignment exists between the transmitter and/or the receiver end. Depending on the misalignment susceptibility, the overall proficiency of a WPT system can be approximated. Here, the misalignment from the receiver end is considered. In general, two types of misplacement can occur, one is due to misorientation ($\theta$) and the other is due to displacement ($M$), as visualized in Figs. 7a) and (b), respectively. According to Fig. 7(a), the maximum WPT efficiency of the proposed system remains at more than 50% at $\theta = 60^\circ$, and decreases quickly to 3% for complete misorientation at $\theta = 90^\circ$. However, a significant improvement in $\eta$ was found when the MTM cubes are rotated along with $\theta$. At first, only the receiver end cubes are rotated at an angle, $\theta_r = 15^\circ$, which gives a noteworthy enhancement in efficiency when $\theta$ is more than $80^\circ$. In addition, a rotation in the MTM cubes for both the transmitter and receiver ends ($\theta_{t/r}$) results in a remarkable boost in efficiency at $\theta = 90^\circ$. Based on the simulated results, the maximum WPT efficiency can be more than $35\%$ at $\theta = 90^\circ$ for $\theta_{t/r} = 15^\circ$. As a consequence, the cube orientation ($\theta_{t/r}$) can be adjusted to obtain a reasonable amount of power transfer efficiency supposing a completely misoriented receiver end. Fig. 7(b) shows the change in $\eta$ due to displacement $M$. It is interesting to see that, at a distance $d = 50$ mm, when the receiver end is entirely out of sight from the transmitter end (i.e., at $M = 36$ mm), this WPT system still maintains more than 50% efficiency, which implies a great susceptibility of the proposed WPT system to misalignments.
The periodicity $p$ and excited by two similar rectangular loops of dimensions $3 \times 3$ accordingly to achieve the proper using a 2 the evanescent wave decays more rapidly. Hence, instead of frequencies (lower GHz range). Fig. 8(a) shows a photograph of the experimental setup along with metamaterial slabs. It should be noted that at high frequency, loss increases and the evanescent wave decays more rapidly. Hence, instead of using a $2 \times 2$ array, a $3 \times 3$ array is used, and the size of the transmitter ($T_x$) and receiver ($R_x$) loop also increased accordingly to achieve the proper $S_{11}$. For measurements, two identical $3 \times 3$ CHDR metamaterials having dimensions of $53 \times 53 \times 19$ mm are separated by a distance $d$ and excited by two similar rectangular loops of dimensions $50 \times 50$ mm. The thickness of the loop was 0.5 mm. The periodicity $p$ and the separation $s$ were selected as 19 mm and 15 mm, respectively. In addition, to make a fair comparison between the recently introduced MD based WPT systems and the proposed WPT system, the MD WPT system [26] was created by combining all the available cubes to act as a dielectric slab, as shown in Fig. 8(b). From simulation, the resonant frequencies for the MD and MTM-MD modes were found as 1 GHz and 1.67 GHz, respectively. The simulated and measured reflection ($S_{11}$) and transmission coefficients ($S_{21}$) for the MD-MD WPT system are plotted in Fig. 8(c). The measured resonance frequency was found at 1.7 GHz, and the maximum $S_{21}$ measured as -2.43 dB as compared to the simulated $S_{21}$ of -1.3 dB at $d = 20$ mm (0.1$\lambda$). The deviation between the simulated and measured results mainly occurs due to the presence of a visible air gap between cubes and Teflon. This air gap influences the performance of the MTM slab and coupling. The mismatch between the $T_x$ and $R_x$ loop also affected the measured results. Considering all these experimental limitations, the measured results remain almost identical to the simulated results. For $\varepsilon_r = 78$, permeability, $\mu_r = 1$, and a loss tangent $\tan \delta = 0.0004$. As a result, the resonant frequency was scaled up to higher frequencies (lower GHz range). Fig. 8(a) shows a photograph of the experimental setup along with metamaterial slabs. It should be noted that at high frequency, loss increases and the evanescent wave decays more rapidly. Hence, instead of using a $2 \times 2$ array, a $3 \times 3$ array is used, and the size of the transmitter ($T_x$) and receiver ($R_x$) loop also increased accordingly to achieve the proper $S_{11}$. For measurements, two identical $3 \times 3$ CHDR metamaterials having dimensions of $53 \times 53 \times 19$ mm are separated by a distance $d$ and excited by two similar rectangular loops of dimensions $50 \times 50$ mm. The thickness of the loop was 0.5 mm. 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mm. The distance, $d$, is chosen as 130 mm, and more than 5% efficiency was achieved for the MTM-MD case at a distance of 0.65$\lambda$ even when the $R_x$ end is completely out of sight from the $T_x$ end. However, the received $\eta$ reduced to 1.4% without the MTM coupling. By doubling the input power compared to Fig. 9, the received power without MTM not enough to turn on the LED, as indicated in Fig. 10(a). In contrast, by simply placing the MTMs for the same input power, the LED shines brightly, as revealed in Fig. 10(b). This illustration provides insight into the power transfer capability of the proposed WPT system for misalignments.

In the MTM-MD based WPT system the large separation ($s$) also signifies that magnetic field coupling occurs between the two MTM resonators, therefore, $T_x$ and $R_x$ can be moved independently. This phenomenon is displayed in Fig. 11, where $R_x$ is placed at the worst position, with complete displacement to the $T_x$ axis and rotated by 90°. For $d = 100$ mm (0.5$\lambda$), traditional WPT gives a negligible transfer efficiency of 0.14% as opposed to the 1.15% for the proposed WPT system. These results are also reflected by Figs. 11(a) and (b) for the power input of 1 W. This separation ‘$s$’ feature enables future studies where, there will be no need to place the devices ($R_x$ end) on a charging pad for wireless charging. Instead, we will be able to establish truly wireless charging as long as the devices remain in the MTM–coupled region.

The Specific Absorption Rate (SAR) still remains a concern with the WPT system [40]–[41]. If any human tissue/implantable device lies in the middle of $T_x$ and the $R_x$,

![Fig. 11. Demonstration of WPT efficiency considering the worst case scenario of ‘$s$’: (a) Traditional WPT. (b) MTM-MD WPT systems.](image)

![Fig. 12. Normalized 1-g local SAR calculation in human skin tissue for: (a) MTM–MD based WPT system. (b) Traditional inductive coupling based WPT system. Measurements in a simple cup containing fresh water for (c) Traditional WPT system. (d) Proposed MTM–MD system.](image)
The parameter, ‘s’ can be adjusted for tuning the WPT system and to optimize the WPT efficiency, as discussed in Section III. A of the main manuscript. It is also mentioned that for optimizing efficiency, ‘s’ can be increased with an increasing distance \( d \). This situation has many advantages. In one case, the proposed method can reduce the SAR as well as increase the efficiency compared to the most commonly used inductive/resonant coupling. A HFSS simulation illustration of the SAR is shown in Fig. 12. For the simulation setup, a cylindrical skin phantom \((\varepsilon_r = 39.2, \sigma = 1.11\) at 1.7 GHz\) of radius 3 cm and height 5.3 cm is placed in between the transmitter and receiver side, and the distance, \( d \) was chosen as 72 mm. Two similar rectangular loops of dimension 50 mm \( \times \) 50 mm were considered as \( T_x \) and \( R_x \). For Simplicity, simulated 1–g SAR was normalized to 1 W/kg. As visualized in Fig. 12(b), in traditional inductive coupling if the exciting element (i.e., \( T_x \)) lies very close to human tissue, it introduces a local hot spot inside the tissue, as opposed to the MTM-coupled WPT system in Fig. 12(a). In addition, it is important to note that the simulated received efficiency is almost four times higher in the case of the proposed WPT system as compared to the traditional WPT system, even when the \( T_x \) and the \( R_x \) are more than 20 cm apart from each other. Measurement validation is carried out by placing a simple cup of fresh water as a phantom in the middle of \( T_x \) and \( R_x \) separated by 70 mm, as indicated in Fig. 12(c). From Figs. 12(c) and (d), it can be confirmed that, for the same power input of 0.7 W, the MTM-MD based WPT system offers higher efficiency as compared to the traditional WPT system, as indicated by the LED. Due to low SAR and high efficiency in the MTM–MD WPT system, the input power can also be increased to reach the SAR safety limit when more power is required by a system.

V. CONCLUSION

In this paper, a WPT system referred to as ‘MTM–MD’, based on two CHDR metamaterials which are excited by two similar non–resonant oops, is explored. The CHDR metamaterial is composed of an array of cubic high dielectrics arranged in a low dielectric background. From HFSS simulation, it is observed that this WPT system introduces a horizontal magnetic dipole between the CHDR metamaterials and achieves more than 80% efficiency at short distances and 50% efficiency at a distance of 0.2\( \lambda \). The proposed WPT system requires a smaller foot-print for higher efficiency compared to previous studies and the transmitter and receiver sizes should not be lower than the CHDR’s cube size for a reasonable WPT efficiency. It is also found that a larger CHDR array helps to improve the range of the WPT system. For measurements, the CHDR metamaterials were designed by considering microwave ceramic samples of EXXELIA TEMEX E5080 for high dielectric cubes and Teflon was selected as a low dielectric background. Experimental comparison between the most recent high–dielectric–coupled WPT system and the proposed system was also carried out to demonstrate the long range power transfer capability. The versatility of the system was also discussed by considering the receiver misalignment. We found that the suggested WPT system can withstand receiver displacement from the transmitter axis as well as the orientation of the cubes inside the CHDR metamaterial can be adjusted for misorientation while maintaining an efficient WPT system. Furthermore, the MTM-MD WPT system performed superiorly in the presence of a tissue like material in terms of the SAR and efficiency as compared to the traditional WPT system. Due to the heterogeneous nature of the human tissues, it is expected that the proposed dielectric–based method will only expose or stimulate the desired part without affecting the surrounding media. Hence, the proposed concept can be explored to power up a tiny medical device or to give tissue-specific heating for hyperthermia without affecting the surrounding tissues and so on.

REFERENCES

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