
There may be differences between this version and the published version. You are advised to consult the publisher’s version if you wish to cite from it.

[http://eprints.gla.ac.uk/189190/](http://eprints.gla.ac.uk/189190/)

Deposited on: 28 June 2019

Enlighten – Research publications by members of the University of Glasgow
[http://eprints.gla.ac.uk](http://eprints.gla.ac.uk)
An investigation into serotonergic and environmental interventions against depression in a simulated delayed reward paradigm

Bernd Porr¹, Alice Miller¹, Alex Trew¹

Abstract
The disruption of the serotonergic (5HT) system has been implicated in causing major depression and the standard view is that a lack of serotonin is to blame for the resulting symptoms. Consequently, pharmacological interventions aim to increase serotonin concentration in its target areas or stimulating excitatory 5HT receptors. A standard approach is to use serotonin reuptake inhibitors (SSRIs) which cause a higher accumulation of serotonin. Another approach is to stimulate excitatory serotonin receptors with psyche delics drugs. This paper compares these two approaches by first setting up a system level limbic system model of the relevant brain areas and then modelling a delayed reward paradigm which is known to be disrupted by a lack of 5HT. Central to our model is how serotonin changes the response characteristics of decision making neurons where low levels of 5HT allow small signals to pass through whereas high levels of 5HT create a barrier for smaller signals but amplifying larger ones. We show with both standard behavioural simulations and model checking that SSRIs perform significantly better against interventions with psychedelics. However, psychedelics might work better in other paradigms where a high level of exploration is beneficial to obtain rewards.

Keywords
Serotonin, Depression, Reinforcement learning, Delayed rewards, Model checking

1 Introduction
Serotonin (5HT) has been implicated in causing major mood disorders such as depression (Chaudhury et al. 2015). Consequently, influencing the serotonergic system with pharmacological interventions has been shown to be effective. In particular, serotonin reuptake inhibitors (SSRIs) have positive effects on a patient’s mood (Barker and Blakely 1995; Cipriani et al. 2012; Stahl 1994). However, this well established therapy has its critics who favour psychedelics instead of SSRIs as a drug for combating depression (Carhart-Harris and Nutt 2017). Psychedelics are mainly known for their ability to alter the perception of sensor stimuli as shown with drugs such as LSD (Winter 2009). In addition SSRIs change the perception of emotionally related stimuli so could be used to indirectly influence a subject’s mood (Harmer 2008). The fact that 5HT can alter cortical processing suggests that the role of the serotonin receptors should be investigated more closely (Mengod et al. 2009). While there are over 7 different 5HT receptors, 5HT1 and 5HT2 have been mainly implicated in mood disorders (Carhart-Harris and Nutt 2017). This means that to understand the action of 5HT we must at least determine how 5HT1 and 5HT2 operate together to influence neuronal processing.

However, mood is not just linked to serotonin but also to dopamine (Schultz 1998; Cofer 1981). This means serotonin cannot be understood in isolation but must be considered in conjunction with the dopaminergic system (Schildkraut 1965; Martin-Solch 2009). In the past dopamine was prominent in models of reward based processing and serotonin was viewed as an inverted dopamine signal. Daw et al. (2002) provided a model of serotonin and dopamine whose signals represented mirror opposites in terms of computations of reward, punishment and long-term average of these signals. Boureau and Dayan (2011) also viewed serotonin as an inverted dopamine signal but in relation to both reward (punishment) and behavioural approach (inhibition/avoidance). However this view has been abandoned (Dayan and Huys 2015) in the light of recent experimental results which show that 5HT tracks the long term anticipation of a reward (Nakamura et al. 2008; Bromberg-Martin et al. 2010; Li et al. 2016). Thus, serotonin codes distinctly different information to dopamine.

What kind of behaviour is improved by the release of serotonin? From recent studies it has become apparent that serotonin is required for situations where an animal needs to wait to obtain a delayed reward (Li et al. 2016; Bari and Robbins 2013) and that 5HT “integrates expected, or changes in, relevant sensory and emotional internal/external information” (Homberg 2012).

To understand the role of 5HT we need to investigate the following:

¹University of Glasgow

Corresponding author:
Bernd Porr, University of Glasgow, Glasgow, G12 8QQ, Scotland
Email: Bernd.Porr@glasgow.ac.uk
• the action of 5HT on the major 5HT receptors, in particular 5HTR1 and 5HTR2

• processing of emotionally relevant stimuli from sensor to action via both cortical and subcortical structures

• how processing/perception of these stimuli is altered/controlled by 5HT

• earmarking behavioural paradigms which require a functional 5HT system

• how the reward system is impacted by altered 5HT signal processing

In other words: we claim that it is only possible to understand the 5HT system by using a holistic approach including all levels starting from 5HT receptors up to behaviour. This means that possible interventions cannot be seen in isolation but need to be viewed in combination.

The standard approach of testing a system model such as ours is to run simulations of the model many times for each proposed set of parameters and perform statistical analysis on the results in each case. This has the advantage that both behaviour and system can be modelled in great detail. However, running multiple simulations is time-consuming and does not guarantee complete coverage (how many simulations should we run?). In this paper we use an additional approach: Model Checking. This is a technique in which a system is expressed using a formal language and converted into a finite state model. This underlying model can then be used to exhaustively check properties (e.g. the probability of an event occurring in the long run) for a range of parameter values. In particular here we will use model checking to investigate the link between the neuronal response characteristic and its impact on delayed reward learning. Both the behavioural simulator and the model are available via an open access repository (Porr et al. 2019).

The paper is structured as follows: first, we present a behavioural experiment which involves a rat waiting for a delayed reward. Then we describe the information flow from sensor inputs to actions via cortical and sub-cortical structures. We then focus on how information processing is altered with the action of serotonin (5HT), how sensor inputs are processed differently depending on the concentration of 5HT and how this is achieved with the two 5HT receptors 5HTR1/5HTR2. Finally the model is completed by adding the dopaminergic reward system. We then run simulations where 5HT is reduced and different interventions such as SSRIs, psychedelics and environmental changes are introduced so that the rat receives more rewards. We will then draw our conclusions as to which of these interventions are successful and under which conditions.

2 Methods

2.1 The behavioural experiment: patience to obtain a reward

Fig. 1 illustrates our experiment, which can loosely be described as “having patience to receive a reward” (Li et al. 2016). A rat needs to learn to approach the green landmark on the left and then wait there until food becomes available and thus visible. The blue landmark on the right is for distraction: it will never show any reward but it generates visual information. We can divide the learning behaviour into five steps:

1. the rat happens to wait in front of the landmark and receives the reward
2. next time the rat has associated the visual information of the landmark with the reward and approaches it
3. at the same it has also associated the area around the landmark as a place to wait
4. the food appears and the rat approaches the food
5. (as in 1) the food results in a reward

These steps emerge naturally just by walking through the behaviour and our task now is to identify neuronal structures which generate this behaviour.

2.2 From sensor to action: the limbic system model

By building our limbic system model we first need to focus on those nuclei which translate a pre-processed sensor signal into an action, thus enabling our simulated rat to approach a landmark which eventually releases food. We will then expand it to the complete model.

2.2.1 Action selection in the mPFC and NAcc

We first describe how a sensor signal causes an action and how this processing is modulated by both serotonin and dopamine. Fig. 2 shows the relevant nuclei: medial prefrontal cortex
(mPFC) and Nucleus Accumbens (NAcc) (Berthoud 2004). The mPFC receives excitatory inputs from primary sensor areas such as visual, smell and tactile. In addition it might also receive input from the hippocampus and other higher level areas which are strongly linked to sensor information and context. These inputs are generally glutamatergic (GLU) and excite the neurons in the mPFC. The prominent neuromodulator here is serotonin (5HT) which is released into the mPFC and other cortical areas from the dorsal Raphe nucleus (DRN) (Linley et al. 2013). A major output target of the mPFC is the NAcc, in particular the NAcc core (Heimer et al. 1991; Brog et al. 1993). The NAcc core is closely related to the more dorsal areas of the striatum and is responsible for action selection. Synapses here are strongly modulated by dopamine. The output of the NAcc core then triggers motor actions via a polysynaptic pathway which targets the motor cortices (Kelley 2004; Humphries and Prescott 2010). In our example there are only two actions: approach the green landmark or approach the blue one. The approach action is initiated when the value in the corresponding core unit reaches a threshold and makes the agent approach the corresponding landmark in a simple Braitenberg-like behaviour-based approach (Braitenberg (1984) inspired by Prescott et al. (2002)). The higher the NAcc core value the higher the speed at which the agent approaches the landmark (with a maximum speed of one). Of course a real animal has more pathways but we focus on two processing streams which are sufficient for our simple experiment. Because the sensor signals progress from the sensor areas through the mPFC and then the NAcc core, we first describe the mPFC and then the NAcc core.

2.2.2 The action of 5HT1 and 5HT2 receptors in the mPFC As outlined above the mPFC integrates information from numerous primary and secondary sensor areas but the important aspect is that it receives a strong serotonergic innervation. Serotonergic fibers originate in the dorsal Raphe nucleus (DRN) and from there they mainly target prefrontal cortical areas and to a lesser extent primary sensor areas and subcortical areas (Linley et al. 2013). However, we simply focus on the strongest innervations of 5HT and these occur in the prefrontal areas. There are two major receptors in the cortex: 5HT1 and 5HT2 (Palacios et al. 1990; Mengod et al. 2009). While 5HT1 is inhibitory, 5HT2 is excitatory. This may seem contradictory (Andrade 2011). However the interplay between these two receptors results in a non-linear interaction between them (Servan-Schreiber et al. 1990; Andrade 2011). This has been confirmed directly by measuring neuronal responses in the visual cortex (Shimegi et al. 2016; Seillier et al. 2017) and also in the prefrontal cortex (Cano-Colino et al. 2014) with the help of a neurophysiological simulation model which confirms the responses measured in the visual cortex.

5HT1 Based on the work by Cano-Colino et al. (2014) we model the action of the receptor 5HT1 as a parameter in a psychometric function (Servan-Schreiber et al. 1990) which slowly saturates towards one (see a reproduction of the original result for comparison in the appendix A in Fig 13):

\[ mPFC_{G/B}(\text{inputs}_{G/B}, 5HT1) = 1 - e^{-\left(\frac{\text{inputs}_{G/B}}{\text{max}^{5HT1}}\right)^{2}} \tag{1} \]

where \( \text{inputs}_{G/B} \) is the sum of the inputs to the mPFC (see Fig. 2)

\[ \text{inputs}_{G/B} = \text{vis}1_{G/B} + \text{vis}2_{G/B} + \ldots \tag{2} \]

\[ mPFC_{G/B} \] is the output of the mPFC and 5HT1 the activation of the 5HT1 receptor. The subscripts “G/B” indicate that these are two pathways through the mPFC: one to target the green landmark and one to target the blue one. Fig. 3A shows the response of an mPFC neuron at different 5HT1 activations (1, 2, 3). At low 5HT1 activations (5HT1 = 1) low cortical inputs (inputs < 1.5) are amplified whereas when the 5HT1 activation is high (5HT1 > 2) lower cortical input values (inputs < 1.5) are suppressed. This means that when 5HT is small signals are amplified which in turn makes the animal very attentive to small/noisy cues. On the other hand if 5HT is high lower input signals to the cortex are suppressed. Weak cues or any kind of distraction will be suppressed whereas strong stimuli will be more amplified which can we also interpret as the control of the signal to noise ratio (Servan-Schreiber et al. 1990).

5HT2 The action of the receptor 5HT2 can be formulated in a much simpler way: it adds a certain gain to the processing in a cortical neuron which can be seen as a multiplicative term which then scales Eq. 1 and reflects the model by Cathcart-Harris and Nutt (2017) and the findings by Shimegi et al. (2016); Cano-Colino et al. (2014). It can be seen in Fig. 3B that the effect of the gain is seen mainly for strong cortical inputs and these are then disproportionally amplified. This means that strong cortical inputs receive an additional boost and might be executed with a strong vigour Cofer and Appley (1964).

Combined action of 5HT1 and 5HT2 in the mPFC We can now combine the action of both serotonin receptors which results in the following equation describing how serotonin influences cortical processing:

\[ mPFC_{G/B}(\text{inputs}_{G/B}, 5HT1, 5HT2) = \left(1 - e^{-\left(\frac{\text{inputs}_{G/B}}{\text{max}^{5HT1}}\right)^{2}}\right) \cdot 5HT2 \tag{3} \]

where \( \text{inputs}_{G/B} \) and \( mPFC_{G/B} \) are the total input and output to/from the mPFC respectively. In our example we have two pathways to consider: one for the green landmark and one for the blue.

We need to establish a relationship between the 5HT concentration and the activation of the receptors 5HT1 and 5HT2. In general this means that we have a mapping from the 5HT concentration to the receptor activation which we assume to be linear:

\[ a_{5HT1} = 1 + 5HT \tag{4} \]

\[ a_{5HT2} = 2 + 5HT + HTR2_{OFFSET} \tag{5} \]

where adding the constants 1 and 2 for \( a_{5HT1} \) and \( a_{5HT2} \) respectively guarantees a baseline throughput of
Figure 3. The response functions of mPFC neurons: A) altered by 5HTR1 alone and B) by 5HTR1/R2 combined.

The signals in Eq. 3 so that a signal passes through even when DRN = 0. This means that the minimum value of $a_{5HTR1} = 1$ transforms Eq. 3 into a standard neuronal response curve (Servan-Schreiber et al. 1990) which is then gradually altered with increasing 5HT concentration, thereby suppressing increasingly smaller inputs to the mPFC. The minimum value of $a_{5HTR2,min} = 2$ is the baseline gain of the mPFC and matches the maximum DRN activity which is about 2 in our simulation runs so that this results in transmission gains through the $mPFC_{G/B}$ of between two and four. In other words, the DRN can increase the gain of the mPFC by a factor of two. The constant $HTR2_{OFFSET}$ is usually zero but is set to a positive value if we want to simulate the effect of psychedelics. This will allow us to investigate whether psychedelics are able to reverse the deficit caused by excessive 5HT inhibition.

Overall this means that with high 5HT concentrations inputs to cortical circuits need to have a high salience to coincide with other inputs. For example the visual cue of a food dispenser needs to coincide with the visual input of the food itself at the moment it is delivered. This means that the cortex is both an integrator of information and a gatekeeper. It transmits information to the decision making circuitry in the NAcc core.

2.2.3 Reward based learning in the NAcc core So far we have shaped the signals in terms of attention or signal to noise but have not associated it with any reward. The mPFC projects to the NAcc core which receives a strong dopaminergic (DA) modulation. This has a certain baseline concentration and can either increase or decrease causing a corresponding increase or decrease in synaptic strength of the mPFC input (Beckstead et al. 1979; Humphries and Prescott 2010):

$$\Delta \rho_{G/B} = \mu_{core}(DA - DA_0) \cdot mPFC_{G/B}$$

2.3 Complete circuit model

So far we have dealt only with the novel aspects of our limbic system model which explain how a variable response curve in the cortex and learning in the NAcc core leads to behaviour associated with waiting for a delayed reward. However, we also require the circuitry which generates the signals for both the VTA and the DRN. While the DRN becomes active in anticipation of a reward, the VTA exhibits a classical error signal which only becomes active when the reward is unexpected, and then its amplitude slowly decays. We need to describe how these two signals are computed and the corresponding circuit is shown in Fig. 4.

2.3.1 VTA We start with the activity in the ventral tegmental area (VTA) (Sesack and Grace 2010). A direct pathway from the lateral hypothalamus (LH) to the VTA drives the VTA whenever a primary reward has been encountered. The lateral hypothalamus is well known to respond to primary rewards. However it is also well known that once the reward can be predicted the activity in the VTA will diminish. This is achieved by the pathway: OFC – l-shell – vl-VP – EP – LHb – RMTg and then VTA. Overall this path is inhibitory. The OFC and the NAcc l-shell learn to associate cues with the primary reward (Sackett et al. 2017) which in turn inhibit the VTA. In addition cues or conditioned stimuli cause bursts in the VTA which are conveyed via the m-shell – m-VP – VTA pathway (see appendix A for the mathematical description). This pathway is not modelled as we do not need second order conditioning here.

2.3.2 DRN The main focus of this paper is serotonin (5HT) which is mainly released from neurons in the dorsal Raphe nucleus (DRN) (Michelsen et al. 2007; Pollak Dorocic et al. 2014). The DRN receives an excitatory input from the lateral hypothalamus (LH) (Aghajanian et al. 1990; Lee et al. 2003) which becomes active when a primary reward is experienced. Again, as with the VTA the signal in the DRN diminishes via the slowly increasing activity in the RMTg – DRN pathway. However, the main difference to the VTA is the intimate reciprocal connection to the prefrontal cortex (Zhou et al. 2015; Roberts 2011), in particular we are interested in the orbitofrontal cortex (OFC). Apart from the input from the LH this is the main excitatory input to the DRN (Zhou et al. 2015). We propose that the sustained activity of the DRN in anticipation of a reward is solely generated by cortical structures and in particular by the OFC. As mentioned above the OFC learns to associate stimuli with the reward. These could be direct sensor inputs or pre-processed ones. In our case we assume that the OFC receives place information from the hippocampus and can then “remember” that a reward has occurred at that place. Of course the OFC has many additional abilities. In particular for reversal learning to provide persistent activity which lasts after a reward has been omitted and can provide long lasting depression of both VTA and DRN neurons via the RMTg. However, this is beyond the scope of this paper in which we just focus on reward acquisition.

This leads us to the following equations to calculate the activity of the DRN. Since the OFC projects into the DRN we need to define its activity first:

\[ OFC = \rho_{PF_G} \cdot PF_G + \rho_{PF_B} \cdot PF_B \]  

where \( PF_G, PF_B \) are hippocampal place fields around the green and blue landmarks respectively and \( \rho_{PF_G}, \rho_{PF_B} \) the weights feeding these place fields into the OFC. The two weights from the hippocampus to the OFC change according to:

\[ \Delta \rho_{PF_G/B} = \mu_{OFC} \cdot DRN \cdot PF_{G/B} \]  

at a learning rate of \( \mu_{OFC} \) and where the activity of the DRN is calculated as:

\[ DRN = \frac{LH + a \cdot OFC}{1 + (b \cdot RMTg + DRN_{SUPP})} + DRN_{OFFSET} \]  

and \( LH \) is the activity of the lateral hypothalamus (LH) which becomes active when encountering a primary reward. The RMTg provides a negative feedback on the OFC via the same subcortical pathway as for the reward prediction error and \( a, b \) are scaling constants. The inhibition of the DRN by GABA-ergic projections from the RMTg and other pathological inhibitory sources (\( DRN_{SUPP} \)) is modelled as shunting inhibition, mediated by GABA-controlled \( Cl^- \) conductance (Mitchell and Silver 2003). The reversal potential of \( Cl^- \) as measured in the DRN is about \( -70 \) mV (Pan and Williams 1989) which is virtually identical to the resting potential of the DRN neurons which is about \( -67 \) mV (Jin et al. 2015). This means that there is little or no hyper-polarisation but results in GABA controlling the incoming excitatory gain in the form of a division operation (Mitchell and Silver 2003).

To test the pathological cases we have introduced two constants: \( DRN_{SUPP} \) is zero under control conditions and set to positive values to simulate excessive tonic inhibition for pathological DRN hypoactivity. Similarly \( DRN_{OFFSET} \) is zero for control but will be set to a positive value to simulate the effect of the serotonin re-uptake inhibitor.

When does the DRN become active? Consider Eq. 10 that shows how the DRN fires via the LH pathway at the moment a reward appears. We propose that 5HT causes learning in the OFC and associates the place field with the reward. Note that it is likely that a small VT A innervation will cause plasticity in the OFC and associates the place field with the reward. This will provide delayed rewards.

Before we run simulations we examine graphical traces of the relevant signals to prepare for the more complex signals in the real simulation run.

2.4 Linking behaviour to the signals

How is the behaviour of the rat in our experiment linked to the neuronal model described above? Before stating the equations we go through the activity with the help of the traces in Fig. 5 which represent a cortical mPFC neuron processing approach behaviour to the left reward site which will provide delayed rewards.

1. When the rat encounters the primary reward at the green landmark the LH fires which in turn makes the NAcc core learn to associate the visual information of the landmark \( \nu_{vis,1,G} \) with the reward. This will guarantee that the rat will approach the green landmark.
from this distance. At the same time the primary reward is transmitted from the LH to the OFC which associates the place field (circle around the landmark) with the reward.

2. The rat sees the landmark from a distance so input \( \text{vis}_{1,G} \) is zero. The food is not yet shown so \( \text{vis}_{2,G} \) is zero. The activity of 5HT is zero which allows the activity \( \text{vis}_{1,G} \) to progress easily via the mPFC and NAcc core to the motor circuits, thus causing the rat to approach the landmark.

3. The rat enters the place field. The hippocampus now provides place field information to the OFC which in turn drives the DRN. This means that the 5HT is released in the mPFC where it changes the signal to noise ratio of the incoming signals. Recall that at this point \( \text{vis}_{1,G} \) is greater than zero (indicating “go to landmark”) whereas \( \text{vis}_{2,G} \) is zero. This will effectively make the output of the mPFC smaller which can be seen in the cartoon.

4. After a delay the food appears and \( \text{vis}_{2,G} > 0 \) which, in conjunction with \( \text{vis}_{1,G} > 0 \), results in a strong input to the mPFC which can progress to the NAcc core and cause the animal to approach the food.

In summary we have described a model of a decision-making network that spans cortical and subcortical areas. The cortex shapes the signals so that with low 5HT concentrations small stimuli cause an action whereas with high 5HT concentrations only strong or combined stimuli can progress to the NAcc core to trigger actions. The subcortical areas are therefore responsible for reinforcement learning.

2.5 Scenarios to investigate drug action

Central to this paper are models against depression. It is widely accepted that a hypofunction of the DRN causes less 5HT to be released. There are several proposed solutions to this problem and we will investigate them in this paper. Our aim is to determine which of the proposed solutions will indeed prove to be beneficial, and which will be shown to be counterproductive. To achieve this, after a successful run of a healthy animal we will reduce the release of 5HT by enabling excessive inhibition of the DRN. We will observe the behavioural effects and measure the impact of different interventions.

The scenarios for the statistical analysis have an additional parameter which complements the pathological interventions above: the time the agent must wait for a reward. The default number of time steps is 150. By reducing this period to 100 steps in some cases we can model two interventions:

1. Pharmacological intervention: SSRIs or 5HT receptor agonists such as LSD or magic mushrooms.

2. Environmental intervention: the time the agent needs to wait till it receives its reward.

As we have a scenario where waiting is crucial to obtaining a reward a reduced waiting time is the obvious intervention here. This can then be compared to the pharmacological intervention in terms of its effect.

We combine our (two pharmacological and one environmental) interventions to allow us to consider the following scenarios. In all cases the reward is delayed the default number of time steps unless a reduced reward delay is indicated:

1. Control: the simulated rat successfully waits in front of the landmark. When the reward appears it approaches it and eats it.

2. Reward early: the parameters are the same as in 1 but the food appears earlier (reduced reward delay).

3. DRN suppress: the DRN activity is suppressed by a excessive GABA-ergic influence \((\text{DRN}_{\text{SUPP}} > 0 \text{ in Eq. 10})\).

4. DRN suppress & reward early: the parameters are the same as in 3 but with a reduced reward delay.

5. DRN suppress & SSRI: DRN suppression as in 3 but now the action of the SSRI’s cause a constant baseline shift of the 5HT receptor activations because of slow 5HT reuptake \((\text{DRN}_{\text{SUPP}} > 0, \text{DRN}_{\text{OFFSET}} > 0 \text{ in Eq. 10})\).

6. DRN suppress & SSRI & reward early: the parameters are the same as in 5 but with a reduced reward delay.

7. DRN suppress & 5HTR2 agonist: the DRN activity is suppressed as in 3 \((\text{DRN}_{\text{SUPP}} > 0 \text{ in Eq. 10})\) but additionally the 5HTR2 receptor is tonically stimulated \((\text{HTR2}_{\text{OFFSET}} > 0, \text{Eq. 5})\) so that the gain of the transmission is increased.

8. Same parameters as in 7 but with a reduced reward delay.

These different scenarios can be investigated both in single runs to gain a deep understanding of the interactions between...
the nuclei, and by conducting multiple random runs to determine statistics indicating how successful learning has been. For the behaviour based approach we conduct Monte Carlo based experiments for each scenario to calculate the relative reward. We then use a computational technique known as Model Checking to analyse behaviour during the crucial period between when the agent slows down in anticipation of the reward and speeds up when the reward appears.

2.6 Probabilistic Analysis

2.6.1 Traditional behaviour based runs We need to define a performance parameter which reflects how successful the agent has been in obtaining rewards. Since this paradigm is about waiting for delayed rewards we compare the number of successful rewards against all encounters with the landmark:

\[
rr = \frac{\text{Number of rewards obtained}}{\text{Number of times the landmark has been approached}}
\]  

(11)

This average reward is not just an academic measure but is monitored within the limbic system (Daw et al. 2002) and then drives the levels of both serotonin and dopamine amongst others (Niv 2007). The complete code including scripts running all scenarios are part of our open access repository (Porr et al. 2019).

Traditionally performance measures are obtained by running the experiment many times and performing a statistical analysis. They have the advantage of being close to the biological model (the behaviour of the animal) but are very time consuming to run. An alternative is model checking.

2.6.2 Model checking An alternative approach used extensively in computing science is model checking. We represent the neuronal activity and behaviour via a formal language. We then use an automatic software tool called a model checker to analyse our system using both simulation and verification. The model checker does this by first creating an underlying mathematical representation, which is then explored to evaluate properties. Note that, for convenience, we refer to both the formal description and the underlying mathematical representation as the model in this paper.

Creating a model necessarily requires us to abstract behaviour – to only contain aspects that are relevant to the properties being verified. We use model checking to focus on the core aspect of this paper, namely waiting for a reward.

The property that we want to evaluate using our model is:

\[
pp = \text{collect the reward at some point during its complete journey?}
\]  

(12)

which is directly comparable to the relative reward (Eq. 11) obtained by multiple runs.

We use the model checker PRISM (Kwiatkowska et al. 2011) to determine the probabilities for our 8 scenarios from Section 2.5. PRISM is a probabilistic model checker that allows for the analysis of a number of probabilistic models including Discrete Time Markov Chains (DTMCs), Markov Decision Processes (MDPs) and Continuous Time Markov Chains (CTMCs). All of the models used in this paper are DTMCs. Models in PRISM are expressed using a high level modelling language based on the Reactive Modules formalism (Alur and Henzinger 1999) and properties used in the verification of DTMCs are based on Probabilistic Computation Tree Logic (PCTL) (Hansson and Jonsson 1994). In a Prism model, each module has a set of finite-valued variables which contribute to the module’s state, the global state space of the system is given by the product of the states of each module. Transitions of the model are established by way of commands, where a command consists of an (optional) action label, guard (i.e. a condition which must hold for the transition to be executed) and probabilistic choice between updates. The update specifies how the variables of the module are updated when the command is executed. The probabilities for each update sum to 1. Modules interact through guards and synchronise via action labels.

As outlined above, in contrast to the behaviour based approach we focus on the crucial moment when, after learning, the agent sees the landmark, approaches it and waits in front of it to obtain the delayed reward. Our model assumes a linear search area as depicted in Fig. 6 which is our one dimensional place field from Fig. 1. Central to this is Eq. 3 which controls the speed of the agent while it approaches the landmark. The reward can then appear at any of the seven positions marked on the central line. The agent should then speed up to reach the reward. The variable \( \sigma \) is set in a way that the seven positions are spread evenly over the place field. See Porr et al. (2019) for the complete Prism code, and the appendix B for the parameters.

To represent the behaviour of the agent and the delayed reward our model consists of two interacting modules. These are the limbic_system module, and the reward_spawner module. These modules synchronise after the agent has reached the waiting area and the reward_spawner delays releasing the reward. The behaviour of these modules is illustrated in Fig. 7. Note that the states in Fig. 7 actually correspond to groups of states in the underlying DTMC. The states labelled \( S_i \) or \( t_j \) in the limbic_system and reward_spawner modules correspond to all states for which variables \( s \) and \( t \) have the value \( i \) or \( j \) respectively. Note that from index 2 these
states match those introduced in Fig. 1. States $S_0$ and $S_1$ correspond to the start of the behavioural model and a point at which random movements prior to seeing the landmark have occurred. We use the transition between the two to set speed_type - a variable which will contribute to the likelihood of missing the reward location later in the model.

Figure 7. States and transitions for the Prism model

To describe our model we refer to Fig. 7. The states associated with the limbic_system module are described below:

$S_0$: Initially a probabilistic choice is made as to the position of the reward (represented by the first transition in the limbic_system module - probabilistic choice is denoted by a dashed line). There is an equal probability of the reward appearing at each of the positions $r + k\sigma$, for $k \in \{-3, -2, -1, 0, 1, 2, 3\}$ (as illustrated in Fig. 6).

$S_1$: One of three speed types is probabilistically chosen (which will control the speed of the agent). In the behaviour-based simulation this speed variation is due to different angles at which the agent approaches the landmark and fluctuations of the weights controlling the speed. Both of these factors are abstracted to the three different speed types.

$S_2$: The agent can see the landmark ($vis_1 = 1$) and approaches it. The speed of the agent is set via Eq. 3 to: $reward\_unseen\_speed = mPFC$.

$S_3$: The agent has reached the edge of the place field. At this point under normal conditions the serotonin concentration has increased and the agent should slow down. Different pathological conditions and/or interventions might change this and these will be the crucial part of our investigation (see Section 2.5).

At the same time as the agent enters the place field a timer is started which allows us to delay the release of the reward. The reward_spawner module then waits a predefined number of time steps (delay) before the reward is released. The two modules synchronise during this period (denoted by transitions with thick lines in Fig. 7), preventing the agent from speeding up until the reward has appeared.

However, if the agent is impatient and does not slow down sufficiently it will reach the (empty) landmark prematurely and miss the reward. This is reflected in the model by an immediate transition to final state $S_6$.

$S_4$: At this point the timer has reached the set delay time and the reward spawner makes the reward appear ($vis_2 = 1$) so that now both $vis_1 = 1$ and $vis_2 = 1$. According to Eq. 3, the speed now ($reward\_seen\_speed$) is set to a higher value to obtain the reward. Again, this might be compromised or improved because of pathological cases or interventions.

$S_5$: The reward is collected if it has appeared and missed otherwise.

$S_6$: The final state - entered whether the reward has been obtained or not.

3 Results

We present our results in three subsections. First we describe instructive single simulation runs which show the activities in the different nuclei and relate these to the activities. We then give statistical results from traditional behaviour based simulations followed by our model checking results.

3.1 Single simulation runs

In this section we show how we can use our simulation model to examine the different activities in a qualitative way to gain an intuition of the processing involved in this complex cortical and subcortical network. This is done by performing eight single instructive simulation runs according to the different scenarios (section 2.5).

3.1.1 Control run

Fig. 8 shows the signal traces of a successful run where the agent learns to approach the green landmark and to wait in front of it. The numbers in the figure correspond to those we used previously in Fig. 5. Before step 1 the agent wanders randomly. The visual signal $vis_{1,G}$ indicates that the agent sees the green landmark. It is strongest when the agent is close to it.
Figure 8. Control: Successful learning and waiting. Signal traces of (from top to bottom): 1) Place field around the reward site (dashed) and visual distal landmark signal $vis_1$, 2) visual signal of the reward $vis_2$, 3) output of the medial prefrontal cortex (mPFC, Eq. 3), 4) dorsal raphe nucleus (DRN) activity (Eq. 10), 5) synaptic weight in the NAcc core to approach the green landmark (Eq. 7), 6) activity in the ventral tegmental area (VTA, Eq. 14) and 7) Nucleus accumbens core (NAcc core) activity switching on approach behaviour towards the green landmark (Eq. 6). The numbers in the signal traces correspond to the steps in section 2.4 linking behaviour to the signals.

1. The agent accidentally waits in front of the green landmark which then delivers food before the agent wanders off so that the agent also has a non zero $vis_2,G$. At the moment the agent receives the food at 1) the VTA is triggered which then causes long term potentiation in the NAcc core so that its weight grows. This will cause the agent to approach the green landmark from a distance next time. The agent is returned to its starting point. At this point the agent also associates the place field around the green landmark with the reward which will cause a rise in the DRN activity next time and subsequent strengthening of this association. This is entirely done by the OFC which keeps track of the reward value.

2. After an unsuccessful attempt the agent sees the landmark from a distance at 2) and approaches it.

3. The agent enters the place field around the green landmark and the DRN activity rises. This now creates the crucial drop in activity in the mPFC which is caused by the activation of the 5HTR1 and 5HTR2 receptors as described in Section 2.2.2. The suppression of mPFC activity is crucial here. This can clearly be seen at the point at which the DRN activity increases. This makes the agent stop as no activity is fed downstream to the NAcc core and consequently no action is triggered. The agent waits. Any smaller distracting signals would be suppressed.

4. The reward appears and with that $vis_2,G > 0$. The overall effect is a much stronger input to the mPFC in the region of $input_G = 2$, so Eq. 3 now receives a strong input from both $vis_1,G$ and $vis_2,G$ which are now both amplified due to the high 5HT concentration. The high 5HT concentration makes the agent focus on the strong signal and approach the target.

5. The agent receives the food and obtains a reward. This further strengthens the association between the green landmark and the place field.

The agent is not perfect. It might miss the food because of its limited viewing angle or because it is not able to turn around quickly enough to approach the food. If this happens a negative reward prediction error is generated and the agent experiences long term depression.

Overall our simulation shows that the agent obtains rewards because 5HT causes it to wait. This is achieved by suppressing smaller signals feeding into the mPFC at high 5HT concentrations. This makes the agent wait and only approach the landmark once the additional stimulus from the food creates an overall strong and thus salient signal.

We now examine how this behaviour is altered when the 5HT is reduced and which interventions are effective.

3.1.2 DRN activity reduced Fig. 9 shows a typical run where the activity in the DRN is suppressed (i.e. $DRN_{SUPP} > 0$ in Eq. 10) in addition to the inhibition from the RMTg.

As before the the agent receives a reward at 1) but the next time it approaches the landmark it does not wait and thus does not receive a reward. This causes a negative reward prediction error and with that a decay of the weights in the NAcc. This means that the successful association with the landmark is unlearned and we see this in the decay of the
Figure 9. The DRN activity is reduced due to excessive inhibition of the DRN. Signal traces: 1) Place field and visual landmark signal $\text{vis}_1$, 2) visual reward signal $\text{vis}_2$, 3) mPFC: medial prefrontal cortex, 4) DRN: dorsal Raphe nucleus, 5) $\rho_g$: nucleus accumbens core weight to approach the green landmark, 6) VTA: ventral tegmental area and 7) NAcc core G: nucleus accumbens core activity to approach the green landmark.

Figure 10. DRN activity reduced due to excessive inhibition but serotonin reuptake inhibitors (SSRI) cause a tonic serotonin concentration modelled here mathematically by introducing a shift in the DRN trace. Signal traces: 1) Place field and visual landmark signal $\text{vis}_1$, 2) visual reward signal $\text{vis}_2$, 3) mPFC: medial prefrontal cortex, 4) DRN: dorsal Raphe nucleus, 5) $\rho_g$: nucleus accumbens core weight to approach the green landmark, 6) VTA: ventral tegmental area and 7) NAcc core G: nucleus accumbens core activity to approach the green landmark.

weight. Thus, no waiting leads to fewer rewards and negative prediction errors which will lead to even fewer rewards in the future.

So far we have focused on sub-cortical processing. However it is well known that OFC tracks reward value as well as the NAcc shell. Indeed the OFC is possibly the more important area. We stressed earlier that this brain area is much more influenced by 5HT than by DA. Plasticity is also likely to be driven by 5HT. With reduced 5HT release plasticity changes will become slower. As a result it will be longer before the OFC learns that the area around the green landmark is potentially rewarding. This can be seen by the
Figure 11. DRN activity reduced because of excessive GABA-ergic inhibition. Psychedelics stimulate the 5HTR2 receptor which cause a strong output from the mPFC because of increased transmission gain. Signal traces: 1) Place field and visual landmark signal vis1, 2) visual reward signal vis2, 3) mPFC: medial prefrontal cortex, 4) DRN: dorsal Raphe nucleus, 5) ρg: nucleus accumbens core weight to approach the green landmark, 6) VTA: ventral tegmental area and 7) NAcc core G: nucleus accumbens core activity to approach the green landmark.

slow rise of the DRN activity which eventually saturates at a lower level than in the healthy condition.

In summary there are two effects caused by a depletion of 5HT:

1. Poor signalling that a reward is imminent means that the agent does not wait for the reward. This leads to fewer rewards in total.

2. Because of a lack of 5HT in the OFC plasticity is not increased when there is the potential of a reward. The OFC thus does not effectively learn the association between rewards and reward-potential cues.

3.1.3 Restoring activity with SSRIs

Serotonin reuptake inhibitors (SSRIs) are important and effective drugs against depression. Fig. 10 shows the traces of a run where we have simulated the action of the SSRIs: because 5HT is not re-absorbed it continues to stimulate the receptors at a certain baseline level. We have simulated this with a bias added to the 5HT concentration ($DRN_{OFFSET} > 0$ in Eq. 10). In order to make it visible in the traces we have added the bias to “DRN” which is identical from the perspective of the simulation, namely that the receptors experience a constant stimulation.

The shift in the baseline has two positive effects on the learning. Learning of the reward value in the OFC is much faster because it initiates the positive feedback between OFC and DRN as soon as a reward has been triggered. We see that the increase of the DRN activity is much faster and saturates only after a few contacts with the landmark. In addition the maximum concentration of 5HT is higher which leads to the agent waiting in front of the landmark, so receiving more rewards.

In summary the SSRIIs provide good relief against the problems caused by low DRN activity: enhanced plasticity in the OFC and greater reward value due to a higher 5HT signal. A point to note is that learning will become less specific due to the increase in plasticity. However, because learning is still triggered by the reward from the LH this is of minor concern.

3.1.4 Restoring activity with psychedelics

Recently psychedelics have been suggested as a means to counteract the effect of loss of 5HT. Fig. 11 shows a relevant simulation run. Psychedelics particularly stimulate the 5HTR2 receptor which is responsible for the gain of the neuronal transmission. In order to understand how this is beneficial we recall the different contributions of the 5HTR1 and 5HTR2 receptors. The 5HTR1 receptor decides how small signals are to be treated. At low concentrations of 5HT small signals are amplified whereas at high 5HT concentrations they are suppressed. When the DRN is not able to release much 5HT small signals are amplified even more. This means that the agent will approach potential food sources even if their stimulus is small (and so the agent will approach any object). On the other hand the stimulation of the 5HTR2 receptor introduces a bias on the 5HTR2 receptor so that it constantly boosts the gain of the target neuron. We have simulated this by adding a constant value ($HTR2_{OFFSET} > 0$) to the 5HTR2 activation in Eq. 5.

Returning to Fig. 11 we can observe the effect of this bias. As the agent was attracted to the blue landmark as well as the green one it did not receive a reward until time step 6700. On the other hand, learning is probably enhanced because of higher 5HT activity. This leads to a mild beneficial effect overall and the agent eventually learns to wait in front of the landmark.
In summary the benefit of 5HT2 agonists are in their ability to enhance exploration. This leads to more contact with the landmarks but also more disappointment.

Having developed our model and obtained intuition as to how processing in cortical and subcortical areas works, we now perform a quantitative evaluation of the overall reward obtained. First we use the simulator from the previous section by running all experiments many times. We then show the results of using model checking to investigate the crucial stage of waiting for a reward.

3.2 Statistical evaluation

For our eight scenarios defined in section 2.5 we ran traditional statistical runs in which the simulated rat experiment was run 63 times with different start directions in the arena. The simulations ran until the simulated rat had reached the landmark 50 times (irrespective of whether food was shown) and the number of rewards obtained was counted. The resulting values of $rr$ calculated via Eq. 11 were averaged over the 63 runs and their standard deviation calculated. These values are shown in Fig. 12A, ordered from bottom to top according to the eight interventions described in Section 2.5. We have compared the results for each case using a two sided t-test for dependent distributions ($p < 0.05$) which indicated significant differences between all 24 unique pairs. We now describe our findings for each scenario.

In the control condition in about 75% of all approaches to the landmark the agent receives the reward. This marginally increases when the reward is presented early.

Suppression of the DRN activity generates a very poor performance with about 25% success and a very narrow error rate. An earlier reward can improve this significantly as can the administration of SSRIs. Combining the use of SSRIs with a shorter reward delay increases performance to about 50%. This means that the agent receives the reward about half of the time. In contrast, the chance of an agent running aimlessly through the arena receiving the reward is close to zero. The improvement is still not as good as the control but has a significant improvement against the pure “DRN suppress” condition with about twice as many rewards obtained. This means that the circuits in the limbic system which track reward value will reach a higher level which in turn will feed back into the cortex.

The other approach is the use of psychedelics to increase the number of obtained rewards. In accordance with the single trial run psychedelics make it worse in this scenario where the agent needs to be patient. Stimulating the 5HT2 receptor increases the gain of cortical processing which means that the animal becomes more impulsive and won’t wait. This leads to a significantly worse performance with 5HT2 agonists against in particular the 3rd scenario “DRN suppress”. However, this can be significantly improved when the reward is presented earlier. This points to an interesting twist revealing under which conditions psychedelics will work: they will only work in conjunction with environmental changes - just administrating them could make the situation worse.

However the application of SSRIs plus an earlier reward is significantly better than the administration of 5HT2 agonists in conjunction with an earlier reward.

Overall these simulations show that even a slightly earlier reward is beneficial in both cases but is essential for 5HT2 agonists such as LSD. This is because they increase the impulsivity of the agent meaning that it cannot cope with long delayed rewards.

3.3 Model Checking

Fig. 12B shows the results of model checking which can be compared to those using traditional statistical methods shown in Fig. 12A. Overall we observe that model checking confirms the results from the behavioural simulation where the relative rewards track closely the reward probabilities. This is particularly the case from control up to scenario 6 involving the intervention with SSRIs. However, for the scenarios involving psychedelics there is a stronger difference between the pure 5HT2 agonist and the situation where the reward is delivered early. This means that the environmental contribution is much more emphasised during model checking. Remember that our model checking model uses a one dimensional abstraction of the behaviour so that in the case of an impatient agent there is little chance of “accidentally” waiting for the reward by detouring...
via intermittent distractions. Our abstraction from the behavioural model allows us to show a distinct advantage of the SSRI approach against psychedelics, at least for the delayed reward paradigm, by focusing on one key aspect – namely how 5HT changes the neuronal transfer function (Eq. 3) turning sensor stimuli into action.

4 Discussion

We have investigated how serotonin shapes the action selection process in a simulated experiment where a rat has to wait for a delayed reward. Waiting is achieved by 5HT tuning cortical processing. At high levels of 5HT cortical processing only reacts to well learned and relevant stimuli, whereas at low levels even smaller stimuli can trigger behaviour. The pathological case of less 5HT release was then investigated with the main finding that because of less waiting the agent receives fewer rewards which in turn causes negative prediction error and eventually the unlearning of reward associations for both actions and the reward value system. This causes a downward spiral. In order to counteract this we then employed three different interventions: SSRIs, psychedelics and environmental changes making it easier to obtain the reward. Here clearly SSRIs, environmental changes and their combination provide the best results while the introduction of psychedelics leads to mixed results.

The first computational models of the role of serotonin are rooted in the opponent interactions between serotonin and dopamine introduced by Daw et al. (2002) where the positive part of the phasic reward prediction error (RPE) is represented mostly by dopaminergic neurons and the negative part mostly by serotonin. In addition dopamine carries a tonic reward signal and serotonin codes a tonic/average punishment signal. In contrast in our model serotonin exhibits only tonic activity (Nakamura et al. 2008; Li et al. 2016) but this activity increases in anticipation of a reward. See Fig. 5 which shows the cartoon version of 5HT starting to increase when the agent is inside the place field, and the actual activity traces in Figs. 8, 9, 10 and 11. The opponency theory was further refined by Bourreau and Dayan (2011) where serotonin is viewed as an inverted dopamine signal but in relation to both reward (punishment) and behavioural approach (inhibition/avoidance). At the neuronal circuit level this is achieved with the help of an inhibitory projection from the DRN to the VTA which is able to suppress VTA activity and interpreted as an opponent signal to that of the VTA. Interestingly, while the opponency theory has been abandoned (Dayan and Huys 2015) this does not contradict our model at the circuit level because the DRN activity could also be used to help to calculate the reward prediction error (RPE) by providing a different source of inhibition to the VTA (see Fig. 4). Recall that the RPE is calculated by inhibiting the primary reward information to the VTA which arises mainly from the LH. Instead of inhibiting the VTA via the OFC-shell-VP-LHb-RMTg pathway to calculate the reward prediction error (RPE), the OFC could also inhibit the VTA via the DRN and is thus able to assert a direct inhibition on the VTA bypassing the pathway through the Nacc shell.

While Daw et al. (2002) use an actor/critic model (i.e. TD-learning) to be close to observations from biology, the model of Balasubramani et al. (2014) is based on the more abstract Q-learning. This has an additional “risk prediction” error which alters the Q values in such a way that an animal avoids risks in case of anticipated gains and seeks risks in case of anticipated losses. In the context of this abstract model serotonin codes the strength of risks taken into account. However, the serotonin signal is kept at a constant value throughout an experiment and has no dynamics which would relate to simply straight lines in Figs. 8, 9, 10 and 11 averaging out the distinct temporal dynamic of the 5HT concentration (Nakamura et al. 2008; Li et al. 2016) during reward based learning.

The action of 5HT is often delayed by weeks and has been attributed to a slow de-sensitisation of, in particular, 5HT1 and 5HT2 receptors (Stahl 1994). Another explanation is the ability of 5HT to boost plasticity so that neurons learn new positive associations (Scholl and Klein-Flügge 2018; Igaya et al. 2018). For that reason we have controlled cortical plasticity with 5HT. In contrast to intrinsic neuronal effects such as 5HT receptor de-sensitisation we argue that the slow recovery of depressed patients is because they receive more rewards causing the reward system to attach more value to sensor events. This in turn increases motivation via both the shell-vp-md-cortex pathway and an increase in tonic dopamine via the shell-vp-VTA pathway (Cofer 1981; Dayan 2001; Niv 2007). We argue that improvements in the 5HT system need to filter down to the DA system and should be coupled with behaviour.

While the activity of the 5HT releasing DRN has been extensively recorded and documented (Nakamura et al. 2008; Li et al. 2016), the role of the different 5HT receptors is hotly debated. In particular the two oldest subtypes 5HT1 and 5HT2 seem to play important roles where the 5HT1 is inhibitory and the 5HT2 is excitatory (Celada et al. 2013). One might argue that these two effects cancel each other out but this is not the case: it is well established that the application of 5HT usually causes a strong depression of neuronal activity (Celada et al. 2013). This emphasises the fact that the influence of the 5HT1 receptor on signal processing is non-linear, leading to distinctly different processing according to the level of 5HT (see Eq 3).

Recently the role of psychedelics such as LSD as antidepressants has been widely discussed (Carhart-Harris and Nutt 2017; Bryson et al. 2017). The argument is that they enhance cortical processing by boosting activity in the cortex and activating 5HT2 receptors. However, this might not always be desirable, in particular in tasks which require patience due to the fact that the activation of 5HT2 receptors increase the gain of cortical processing (Andrade 2011; Carhart-Harris and Nutt 2017; Shimpei et al. 2016). This might lead to more rewards because of more (random) activity but won’t provide measured goal directed behaviour. Psychedelics might work in situations where rewards are readily available and increased random encounters with rewards boost the reward system so increasing mood. For this reason we argue that interventions with drugs requires matching environmental interventions.

While we focus on reinforcement learning and on the importance of the dynamics of serotonin release during reward related behaviours (Nakamura et al. 2008;
Bromberg-Martin et al. 2010; Li et al. 2016), the model by (Carhart-Harris and Nutt 2017) focuses on stress and how under these conditions the two receptor sub-types 5HTR1 and 5HTR2 are up- or down-regulated. Central to their narrative is the claim that 5HTR2 receptors are mainly located in the cortex and that 5HTR1 receptors are located only in subcortical/limbic areas. In particular the 5HTR2 receptors, mainly located in the cortex, can foster open-mindedness, environmental sensitivity and learning/unlearning. On the other hand the subcortical structures harbour more 5HTR1 receptors representing stress, impulsivity resilience, patience and emotional blunting. This leads to the suggested therapy against depression, namely activating 5HTR2 receptors in the cortex only via pharmacological means, in particular with psychedelics. However this contradicts the findings of Palacios et al. (1990); Varnäs et al. (2004); Mengod et al. (2009); Andrade (2011). In particular Andrade (2011) reports that 80% of pyramidal neurons have both 5HTR1 and 5HTR2 receptors co-localised. In addition they assume that serotonin is released in both subcortical and cortical areas in comparable concentrations. Contrarily our model is based on the hypothesis of Roberts (2011); Linley et al. (2013) that serotonergic neurons of the DRN project mainly to the cortex which also has the highest density of both 5HTR1 and 5HTR2 receptors (Varnäs et al. 2004) and much less so to the subcortical structures which also have a lower density for both 5HTR1 and 5HTR2 receptors (Varnäs et al. 2004). Our model assumes that both receptors 5HTR1 and 5HTR2 are co-located in the cortex (Palacios et al. 1990; Andrade 2011) and that serotonergic influence is more important in this brain region than in subcortical areas (Roberts 2011). This leads to our proposed interplay between these two serotonin receptors in the cortex, namely that they shape the signal to noise processing mainly in the cortex. Adaptation to different situations is achieved by reward related serotonin release in the cortex. On the other hand Carhart-Harris and Nutt (2017) focus on extreme situations of anxiety where the important aspect is not timed serotonin release but rather up- and down-regulation of the serotonin receptors themselves which in turn modulate target neurons over longer time scales. In terms of sub-cortical areas dopamine rather than serotonin is our primary neuromodulator which has well established strong projections from the VTA to subcortical areas such as the NAcc (Beckstead et al. 1979; Breton et al. 2019) and to some cortical areas while Carhart-Harris and Nutt (2017) solely focus on serotonin in their model. In terms of environmental factors (Hartogsohn 2016) the paper by Carhart-Harris and Nutt (2017) stresses as we do that they are important for a successful therapy particularly for a brain in which activity is ramped up by LSD to a higher level of “Entropy” and plasticity (Carhart-Harris et al. 2014). In this situation the right environment is required to obtain rewards as we have shown here.

While LSD acts directly on the serotonergic system, NMDA receptor antagonists such as Ketamine have also shown promising results (Chaudhury et al. 2015; Llamosas et al. 2019). The positive effects of Ketamine can be related to increased serotonin release either through less GABA-ergic inhibition on the DRN (Chaudhury et al. 2015) or increased spontaneous activity of DRN neurons (Llamosas et al. 2019). The exact mechanisms are still being investigated (Pham and Gardier 2019) but the action in this case is distinctly different because Ketamine increases 5HT release while LSD acts specifically on the 5HTR2 receptor. In this respect we predict that Ketamine acts in a similar way to SSRIs while LSD has a very different effect as outlined above.

In this paper we have shown how 5HT helps in the acquisition of rewards when patience is required. In our experiments 5HT made the rat focus on the relevant stimulus. A related effect would be faster response to the omission of rewards (i.e. learning to reprocess due to negative reward prediction errors (Homberg 2012)). Reversal learning will be part of future investigations.

A Behaviour based model

**Lateral hypothalamus (LH)** The LH fires when a primary reward has been received.

\[
LH = reward
\]  

(13)

**Ventral Tegmental Area (VTA)** The VTA receives its activity from the LH and is inhibited by the rostromedial tegmental nucleus (RMTg).

\[
VTA = \frac{LH + VTA_0}{1 + RMTg \cdot shunting\_inhibition\_factor}
\]  

(14)

where shunting inhibition factor = 200 defines the amount of shunting inhibition on the VTA. This constant is identical for any shunting inhibition in this model. VTA_0 is the baseline firing rate of the VTA. At baseline neither LTP nor LTD is invoked. If the activity drops below the baseline LTD is invoked in the targets and if above baseline it is LTP.

**Orbitofrontal Cortex (OFC)** Crucial for our model are the plastic pathways with weights \(\rho_{PF,G/B}\) connecting the place fields (PF) to the OFC:

\[
OFC = \rho_{PF,G/B} \cdot PF_G + \rho_{PF,B} \cdot PF_B
\]  

(15)

\[
\Delta \rho_{PF,G/B} = \mu_{OFC} \cdot DRN \cdot PF_{G/B}
\]  

(16)

where \(\mu_{OFC} = 0.01\) is the learning rate.

**Lateral nucleus accumbens shell** The accumbens shell also receives place field information and associates it with the help of the plastic weights \(\gamma_{PF,G/B}\):

\[
\gamma_{lShell} = \gamma_{PF,G} \cdot PF_G + \gamma_{PF,B} \cdot PF_B
\]  

(17)

\[
\Delta \gamma_{PF,G/B} = \mu_{shell} \cdot (VTA - VTA_0) \cdot PF_{G/B}
\]  

(18)

where \(\mu_{shell} = 0.001\) is the learning rate in the nucleus accumbens shell.

**Dorsolateral ventral pallidum (dVP)** The shell inhibits the dVP:

\[
dVP = \frac{1}{1 + lShell \cdot shunting\_inhibition\_factor}
\]  

(19)

**Entopeduncular Nucleus (EP)**

\[
EP = \frac{1}{1 + dVP \cdot shunting\_inhibition\_factor}
\]  

(20)
Lateral habenula (LHb)

\[ LHb = EP \]  

Rostromedial tegmental nucleus (RMTg)

\[ RMTg = LHb \]  

Nucleus Accumbens core

\[
N_{\text{Acc}}_{\text{core},G/B} = \rho \cdot m_{\text{PFC}}_{G/B} \\
\Delta_{\text{PG/B}} = \mu_{\text{core}}(DA - DA_0) \cdot m_{\text{PFC}}_{G/B} \\
DA_0 = 0.05
\]  

where \( \mu_{\text{core}} = 0.075 \) is the learning rate in the core. The core will then disinhibit motor commands via a polysynaptic pathway involving basal ganglia structures and the motor cortex which is modelled in an abstract way. Below the agent performs exploration activity with a NAcc core activity of 0.25. Above that threshold the agent/simulated rat approaches the green or blue landmark respectively depending on which is stronger.

**Figure 13.** Reproduced from Cano-Colino et al. (2014) showing the action of the 5HT1 receptor on the response curve of a cortical neuron where the firing rate of the neuron is plotted against an injected depolarising current. A) shows the response curve at low serotonin concentrations and B) the response curve at high serotonin concentration.

**Medial Prefrontal Cortex** (see also Fig. 13)

\[
m_{\text{PFC}}_{G/B}(\text{inputs}_{G/B}, 5\text{HT}1, 5\text{HT}2) = \\
\left(1 - e^{-(\text{inputs}_{G/B} \cdot \text{5HT}2)}\right) \cdot 5\text{HT}2
\]

\[
a_{5\text{HT}1} = 1 + 5\text{HT}
\]

\[
a_{5\text{HT}2} = 2 + 5\text{HT} + 5\text{HT2OFFSET}
\]

where **5HT2OFFSET** = 0 under normal conditions and **5HT2OFFSET** = 1 under the influence of LSD.

**Dorsal Raphe Nucleus (DRN)**

\[
\text{DRN} = \frac{LH + a_{\text{OF}}}{1 + (b_{\text{RMTG}} + \text{DRN}^{\text{SUPP}})} + \text{DRN}^{\text{OFFSET}}
\]

where **DRNOFFSET** = 0 under normal conditions and **DRNOFFSET** = 0.15 under the influence of SSRIs. The term **DRNSUPP** = 0 under normal conditions but is **DRNSUPP** = 4 when simulating a suppressed DRN activity due to excessive inhibition.

**B  Prism model**

The full Prism code is available at Porr et al. (2019).

The values of \( r \) and \( \sigma \) (from Fig. 6) and the speed of the agent after the reward has appeared are constants and \text{reward}^{\text{unseen speed}} and \text{speed}^{\text{uncertainty}} (representing the delay in the reward appearing once the agent has reached the place field, the speed of the agent while waiting for the reward to appear, and the uncertainty in the speed - a proportion of \text{reward}^{\text{unseen speed}}) are varied for each experiment.

The two modules \text{limbic system} and \text{reward spawner} synchronise after the agent has reached the waiting area and the \text{reward spawner} delays releasing the reward. This is achieved in Prism via the use of action labels. Specifically all synchronised transitions have the action label ([timed]). This forces any such transition enabled in the \text{limbic system} module to synchronise with an enabled transition in the \text{reward spawner} module with the same label (if such a transition exists).

**References**


### C Biographies

**Bernd Porr** has a PhD in computational neuroscience and a broad interest ranging from computational neuroscience over machine learning to robotics. He has been working on models of the limbic system for more than a decade, developed numerous machine learning algorithms, co-invented the biped robot RunBot, and devised a biologically realistic learning rule for spike timing dependent plasticity. Recently he founded Glasgow Neuro LTD. to use machine learning in commercial products.

**Alice Miller** has a PhD in Mathematics but now works in Computing Science. Her primary research interest is in formal verification, particularly model checking. Recent research includes probabilistic modelling for strategy generation for UAVs and using abstraction and embedded C code to model a biologically inspired reinforcement algorithm. Earlier work includes model checking techniques for concurrent software and symmetry reduced model checking for probabilistic and non-probabilistic systems.

**Alex Trew** is a Masters student in the School of Computing Science at the University of Glasgow. He is interested in the use of model checking for the study of biological adaptive systems. For his Masters thesis Alex has developed a suite of models and logical properties and used the model checkers Spin and Promela to analyse a range of learning-based scenarios.