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Optimising the machining time, deviation and energy consumption through a multi-objective feature sequencing approach

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23 **Optimising the machining time, deviation and energy consumption**
24 **through a multi-objective feature sequencing approach**

25 **Abstract:** A considerable amount of global energy consumption is attributable to the ma-
26 chining energy consumption of the machine tool. Thus, reducing the machining energy
27 consumption can alleviate the energy crisis and energy-related environmental pollution.
28 It has been approved that feature sequencing is an effective and economical approach to
29 reduce the machining energy consumption. The single objective model that only mini-
30 mises the machining energy consumption has been developed in previous research. How-
31 ever, the machining time and deviation, which are also affected by the feature sequence,
32 have not been considered. Thus, this article first aims to understand and model the se-
33 quence-related machining time, deviation, and energy consumption (S-MT, S-MD, and
34 S-MEC) while machining a part. Accordingly, a multi-objective feature sequencing prob-
35 lem, which optimises the trade-off among S-MT, S-MD, and S-MEC, is introduced. To
36 solve it, two optimisation approaches, including Non-dominated Inserting Enumeration
37 Algorithm (NIEA) and Non-dominated Sorting Genetic Algorithm II (NSGA-II), are
38 proposed and employed. A case study was conducted to demonstrate the developed mod-
39 els and the optimisation approaches. The experiment results show that the optimal or
40 near-optimal solution sets can be obtained for eight machine parts. By comparison,
41 20.51% S-MT, 5.29% S-MD, and 16.66% S-MEC can be reduced. Between the two al-
42 gorithms, NIEA is recommended for the part that has fewer than 12 features. Finally,
43 more optimisation approaches for the multi-objective problem are proposed and dis-
44 cussed.

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46
47 **Keywords:** Machining energy; Machining deviation; Machining time; Machine tools;
48 Feature sequencing; Multi-objective optimisation.

Abbreviations

| | |
|---------|--|
| BTT | bottom-to-top |
| CNC | computer numerical control |
| GNEA | genetic-based non-dominated enumeration algorithm |
| MOEAs | multi-objective evolutionary algorithms |
| MOPs | multi-objective problems |
| NIEA | non-dominated inserting enumeration algorithm |
| NSGA-II | non-dominated sorting genetic algorithm II |
| PSFP | processing sequence of features of a part |
| PSFPs | processing sequences of features of a part |
| rpm | revolutions per minute |
| SI | supplementary information |
| S-MD | sequence-related machining deviation [μm] |
| S-MEC | sequence-related machining energy consumption [J] |
| S-MP | sequence-related machining process |
| S-MT | sequence-related machining time [s] |
| S-ND | sequence-related non-cutting deviation [μm] |
| S-NEC | sequence-related non-cutting energy consumption [J] |
| S-NT | sequence-related non-cutting time [s] |

Nomenclature

| | |
|----------------------------|--|
| α_A | angular acceleration of the spindle [rad/s^2] |
| B | monomial coefficient in the S-ND model for the feeding activity |
| $d_j^{(F_p, F_q)}$ | S-ND for the j -th feeding activity from the feature F_p to the feature F_q [μm] |
| D_S | total S-MD based on a specific PSFP [μm] |
| $D_{cut}^{S_k}$ | sequence-related cutting deviation for the feature at the k -th position of the sequence [μm] |
| $D_{non}^{(S_k, S_{k+1})}$ | S-ND between the features at the k -th and $k + 1$ -th positions of the sequence [μm] |
| $E_{cut}^{S_k}$ | sequence-related cutting energy consumption for the feature at the k -th position of the sequence |
| $E_{non}^{(S_k, S_{k+1})}$ | S-NEC between the features at the k -th and $k + 1$ -th positions of the sequence [J] |
| E_S | total S-MEC based on a specific PSFP [J] |
| F | a finite set of $n + 2$ features of a part in machining environment, $F = \{F_i\}_{i=0}^{n+1}$, $F_C \subset F$ |
| F_0, F_{n+1} | virtual features to denote the start and end positions of the tool while machining a part |
| F_C | a finite set of n actual features of a part, $F_C = \{F_i\}_{i=1}^n$ |
| F_i | i -th feature in a part |
| F_p, F_q | specific features in a part |
| g | index for the speed change of the spindle rotation |
| i | index for the feature in a part |
| j | index for the feeding activity in a tool path |
| k | index for the position in a feature sequence |
| l_j^{pq} | sequence-related non-cutting distance for the j -th feeding activity between the features F_p and F_q [mm] |
| m | number of feeding activities in a tool path between two features |
| n | number of actual features in a part |
| n_{Sg}^{pq}, n_{Eg}^{pq} | initial and end speed of the g -th speed change of the spindle rotation in the non-cutting from the feature F_p to the feature F_q [rpm] |
| N | population size in NSGA-II |

| | |
|---|---|
| P_t | parent population that is created at the $(t + 1)$ -th generation |
| Q_t | offspring population that is created at the $(t + 1)$ -th generation |
| R_t | population that is created by the combination of P_t and Q_t at the $(t + 2)$ -th generation |
| S | a finite set to indicate all of the positions of the features in a sequence, $S = \{S_k\}_{k=1}^{n+2}$ |
| S_k | feature at the k -th position of a sequence |
| t | index for the generation in NSGA-II |
| $t_{pj}^{(F_p, F_q)}$ | time for the j -th feeding activity in the non-cutting from the feature F_p to the feature F_q [s] |
| $t_{sg}^{(F_p, F_q)}$ | time for the g -th speed change of the spindle rotation in the non-cutting from the feature F_p to the feature F_q [s] |
| $T_{cut}^{S_k}$ | sequence-related cutting time for the feature at the k -th position of the sequence [s] |
| $T_{non}^{(S_k, S_{k+1})}$ | S-NT between the features at the k -th and $k + 1$ -th positions of the sequence [s] |
| T_s | total S-MT based on a specific PSFP [s] |
| $T_{src}^{(F_p, F_q)}$ | S-NT for the spindle speed change in the non-cutting from the feature F_p to the feature F_q [s] |
| $T_{tc}^{(F_p, F_q)}$ | S-NT for the tool change in the non-cutting from the feature F_p to the feature F_q [s] |
| $T_{tp}^{(F_p, F_q)}$ | S-NT for the tool path in the non-cutting from the feature F_p to the feature F_q [s] |
| u | index for the solution in NIEA |
| w | number of speed changes of the spindle rotation between two features |
| z | natural number |
| $\Delta X_j^{pq}, \Delta Y_j^{pq}, \Delta Z_j^{pq}$ | sequence-related relative distances of X-axis, Y-axis, and Z-axis between the start and end coordinate positions in the j -th feeding activity from the feature F_p to the feature F_q [mm] |

51

52 1. Introduction

53 Increasing energy price and requirements to improve energy efficiency are the new challenges faced
54 by modern manufacturing enterprises [1]. Machine tools are widely used in manufacturing sector [2]
55 and consume considerable amounts of energy [3]. For instance, there are over 7 million machine
56 tools in China, whose total power can achieve 70 million kilowatts [4]. Moreover, surveys showed
57 that the energy efficiency of machine tools is generally less than 30% [4]. Thus, reducing the energy
58 consumption of machine tools has been identified as a potential approach to improving manufactur-
59 ing energy efficiency [5], and it has attracted attention from both academic research and industrial
60 applications [6].

61 Energy-aware process planning and scheduling are two effective management approaches to reduce
62 the energy consumption of machine tools [7]. Research on energy-aware scheduling in manufactur-

63 ing has been well conducted [8] and achieved the target for reducing the idle energy consumption [9].
64 On the other hand, research on energy-aware process planning has been focused on process parame-
65 ters optimisation [10] and achieved the target for reducing the machining energy consumption [11].
66 For example, a recent work by Shin [12] presented the novel component modelling and online opti-
67 misation of cutting parameters (feed rate, spindle speed, cutting depth and width) to minimise the
68 milling machining energy consumption in real-time. However, energy-aware feature (operation) se-
69 quencing research is still insufficient, which restricts the energy-aware process planning.

70 The energy-aware feature sequencing aims at determining the processing sequence of features of a
71 part (PSFP) that minimises the machining energy consumption of a machine tool. In existing studies,
72 the single objective is a limitation [13]. In real manufacturing circumstance, it is not reasonable to
73 only reduce the machining energy consumption without controlling the machining time and deviation,
74 which can cause the problems of machine tool tardiness and product quality. In related research, Shin
75 [12] suggested that the machining time could be considered as another objective in addition to the
76 machining energy consumption in the formulation of an optimisation problem. However, there was
77 an opinion that the machining time was positively correlated with the machining energy consumption
78 [14]. As a result, the minimisation of the machining energy consumption could always result in the
79 minimum machining time. If this opinion was true, it would be redundant to develop the machining
80 time model. It is important to investigate this opinion. Yan [15] and Kant [16] verified the conflict
81 between the machining quality (deviation) and energy consumption, and the machining deviation
82 model should be developed. The lack of identification and extraction of the sequence-related machin-
83 ing process (S-MP) is another limitation. The S-MP is defined as the process that is affected by the
84 PSFP. The machining time, deviation, and energy consumption for completing the S-MP are called
85 the sequence-related machining time, deviation, and energy consumption (S-MT, S-MD, and S-
86 MEC). Bridging the gaps and insufficiencies to model and solve the multi-objective problem has mo-
87 tivated this research, and the proposed solutions are the main contributions of this paper.

88 In our study, it is assumed that all of the required processing for a part can be finished on a single
89 machine tool. If a part requires more than one machine tool, the features to be processed on the same
90 machine can be sorted and separately sequenced. Besides, each feature does not have the volumetric
91 intersection with other features. Our study aims at analysing the conflict between the S-MT and the
92 S-MEC when processing a part, and at integrating the S-MT and S-MD models with the existing S-
93 MEC model to obtain the multi-objective model. This article investigates a novel management ap-
94 proach to reduce the S-MT, S-MD, and S-MEC by merely adjusting the PSFP. The multi-objective

95 optimisation in this research is to achieve the optimal trade-offs among the aforementioned three ob-
96 jectives. A deterministic method, Non-dominated Inserting Enumeration Algorithm (NIEA), and a
97 popular evolutionary algorithm, Non-dominated Sorting Genetic Algorithm II (NSGA-II), are pro-
98 posed and used as the optimisation approaches to search for the non-dominated set of optimal solu-
99 tions. Further, a novel hybrid algorithm named Genetic-based Non-dominated Enumeration Algo-
100 rithm (GNEA) is proposed and compared. An optimal solution represents a PSFP that results in the
101 optimal trade-off among the three objectives. Based on case studies, the developed models and opti-
102 misation approaches are demonstrated, compared, and discussed.

103 In the remainder of this paper, the literature review is presented in the next section. The problem de-
104 scription and the multi-objective model are given in Section 3. In Section 4, the working procedures
105 of NIEA and NSGA-II for optimising the three objectives are described. A case study is conducted to
106 demonstrate the multi-objective feature sequencing approach in Section 5. In Section 6, more optimi-
107 sation approaches for the feature sequencing problem are analysed and discussed. Finally, a brief
108 summary and a description of future work are given in Section 7.

109 **2. Literature review**

110 To understand and model the energy-aware feature sequencing problems, Sheng [17] developed a
111 basic model to depict the effects of the PSFP on the machining energy consumption. Newman [18]
112 investigated the energy-aware feature sequencing model for the computer numerical control (CNC)
113 machining based on the experiments. Further, Hu [13] supplemented the mathematic relationship be-
114 tween the PSFP and the actual cutting volume of each feature in the cutting energy consumption
115 model. However, the non-cutting energy consumption has not been provided in their models, though
116 it accounts for a considerable portion [19]. A mathematic model was developed to describe the ef-
117 fects of the PSFP on the non-cutting energy consumption, including the energy of the machine tool
118 consumed for the tool path, tool change [20], and change of spindle rotation speed [21]. In above
119 models, there are some common limitations. Specifically, the machining energy consumption that is
120 not affected by the PSFP has not been identified and removed, thereby leading to the redundant mod-
121 elling. Single objective environment is another limitation.

122 The single objective model has been improved by adding the new objectives, such as the machining
123 time and deviation [22]. In the existing multi-objective model, there are some insufficiencies on
124 modelling the machining time, deviation, and energy consumption, which harm the model's accuracy
125 and reliability. For example, the time and power data of the machine tool were obtained from the hy-

126 pothesis and software [23] instead of an experiment measurement [24]. Besides, the non-cutting time
127 and energy consumption of the machine tool were assumed to be equal for different PSFPs [25]. In
128 practice, the values of the non-cutting time and energy consumption are affected by the PSFPs, be-
129 cause the plan of the non-cutting operations including the tool path, tool change, and change of spin-
130 dle rotation speed can vary based on the different PSFPs [21]. In previous research, the weight was
131 subjectively assigned to the machining time, deviation, and energy consumption [25], and the multi-
132 objective model was transformed to a single objective model [26]. Thus, our multi-objective model
133 aims at solving the above problems to improve its accuracy and reliability, with the support of the
134 advanced modelling approaches for the three objectives [13].

135 After obtaining the multi-objective model, the optimisation approaches can be employed to find a set
136 of optimal PSFPs that result in the optimal trade-offs among the minimisation of machining time,
137 deviation, and energy consumption. The application of optimisation approaches to solve the energy-
138 aware multi-objective feature sequencing problem can be found. For example, the standard genetic
139 algorithm was employed to find the optimal PSFP by the weighted sum method [25], and the multi-
140 objective optimisation problem was converted into a single objective problem. When using such a
141 method, it has to be run many times to obtain a non-dominated set of solutions, and weak and repeat-
142 ed solutions are usually generated [27]. Multi-objective evolutionary algorithms (MOEAs) can ob-
143 tain a non-dominated set of solutions in a single run and are suitable for multi-objective problems
144 (MOPs) [27]. The application of MOEAs for solving the energy-aware feature sequencing problem is
145 scarce at present. Fortunately, MOEAs have been successfully applied to other energy-aware process
146 planning and scheduling problems, such as process parameters optimisation [28]. These related stud-
147 ies can be used as references for solving our problem.

148 It has been approved that NSAG-II is one of the most effective and popular MOEAs [29]. However,
149 it is inevitable for any MOEAs to trap into the local optima, and the global optimum is not guaran-
150 teed [27]. Thus, deterministic algorithms, which can always find the non-dominated set of Pareto-
151 optimal solutions, have also been proposed and tested for our multi-objective problem. Specifically,
152 NIEA is selected as a deterministic algorithm. In addition, NSGA-II is employed because it normally
153 consumes shorter computation time to solve the medium-to-large problems than a deterministic algo-
154 rithm does. The optimisation results and computation time of the two algorithms are compared in the
155 case study. To obtain the global optimum more quickly for the medium-to-large problems, a novel
156 hybrid algorithm GNEA is further proposed and discussed.

157 According to the literature reviewed, the modelling and optimisation for the aforementioned multi-
 158 objective problem is neither sufficient nor accurate. Accordingly, our multi-objective model is im-
 159 proved by analysing the conflict among the S-MT, the S-MD, and the S-MEC, and developing the
 160 three objectives based on the advanced modelling approaches. Based on the improved model, this
 161 paper investigates a novel and economical approach to optimise the trade-off among the three objec-
 162 tives through adjusting the PSFP. Optimisation approaches based on NIEA, NSGA-II, and GNEA
 163 are first proposed and compared to obtain the optima for our feature sequencing problem. The pro-
 164 posed solutions for modelling and optimising the multiple objectives are the main contributions of
 165 this paper, and they are introduced in the following sections.

166 3. Problem statement and modelling

167 Considering a part that has n actual features, a finite set is used for denoting these n actual features
 168 as:

$$169 \quad F_C = \{F_i\}_{i=1}^n \quad (1)$$

170 where i is the index for the feature, n is the number of actual features in a part, and F_i is the i -th fea-
 171 ture. Because the start and end positions of the tool also affect the S-MT, S-MD, and S-MEC, they
 172 are defined as two virtual features for the part, denoted by F_0 and F_{n+1} . Thus, in machining environ-
 173 ment, there are $n + 2$ features for an n -feature part, which are denoted as a finite set:

$$174 \quad F = \{F_i\}_{i=0}^{n+1}. \quad (2)$$

175 Obviously, the F_C is a subset of the F ($F_C \subset F$). In terms of optimisation, the aim of this research is
 176 to determine the non-dominated set of optimal PSFPs that result in the optimal trade-offs among S-
 177 MT, S-MD, and S-MEC under the precedence constraints.

178 The conflict between the machining deviation and energy consumption was verified in the previous
 179 study [15], and our paper investigates the relationship between the machining time and energy con-
 180 sumption. In **Fig. 1**, a part that has two actual features (holes) is used as an example to explain the S-
 181 MT, the S-MEC, and the possible conflict between them. The two features are denoted as F_1 and F_2 ,
 182 and they are processed by two different spindle rotation speeds of 500rpm and 800rpm. The start and
 183 end positions of the tool, which are virtual features, are denoted as F_0 and F_3 . Two sequences of the
 184 features can be used to process this part: $F_0-F_1-F_2-F_3$ and $F_0-F_2-F_1-F_3$. The tool paths of the two se-
 185 quences are labelled by blue solid lines and red dashed lines, respectively, in **Fig. 1**. In particular, the

186 actual tool paths between B and C , B and D , and D and E are straight lines instead of curves, and the
187 distances from B to H and from D to H are equal. The power profiles of a machine tool when pro-
188 cessing the part according to the aforementioned two sequences are shown in **Fig. 2**. The power pro-
189 files are developed based on the measured data [30] and the prediction method [31].

190 **Fig. 1.** A two-feature part that has two possible processing sequences.

191 The first step is to determine the S-MP. The S-MP is identified by checking whether a machining
192 process (feeding activity) exists in all of the PSFPs or not. If it does not, the machining process is
193 sequence-related, and reserved. Otherwise, the machining process is not sequence-related, and delet-
194 ed. For example, the machining processes from A to B , from B to D , and from D to H do not exist in
195 both of the two PSFPs, as shown in **Fig. 1**, thus these processes are sequence-related, and reserved.
196 The machining processes from B to C to B and from D to E to D exist in both of the two PSFPs, thus
197 these processes are not sequence-related, and deleted, as shown in **Fig. 1**. Further, the corresponding
198 machining energy consumption is removed, and filled with blank in **Fig. 2**. The machining time and
199 energy consumption for the S-MP are namely the S-MT and S-MEC. The S-MEC for the $F_0-F_1-F_2-$
200 F_3 and the $F_0-F_2-F_1-F_3$ are filled with forward blue slashes and red nets, respectively, in **Fig. 2**. The
201 effect of the PSFP on the S-MT and the S-MEC can be found in Hu [21].

202 **Fig. 2.** Power profiles of two different sequences: (a) $F_0-F_1-F_2-F_3$; (b) $F_0-F_2-F_1-F_3$.

203 The possible conflict between the S-MT and the S-MEC is analysed. Specifically, the distance of the
204 tool path from A to B is shorter than that from A to D , and the distances of the other tool paths are
205 equal. Thus, the S-MT for the $F_0-F_1-F_2-F_3$ is shorter than that for the $F_0-F_2-F_1-F_3$. Prior to the final
206 tool path, the S-MEC for the $F_0-F_1-F_2-F_3$ is probably smaller than that for the $F_0-F_2-F_1-F_3$, as reflect-
207 ed by the size of forward blue slashes and red nets in **Fig. 2**. The spindle rotation speed during the
208 final tool path from D to H (800rpm) is higher than that from B to H (500rpm), and the power of the
209 machine tool increases with the spindle rotation speed [32]. Consequently, the total S-MEC for the
210 $F_0-F_1-F_2-F_3$ can be higher than that for the $F_0-F_2-F_1-F_3$ when the point H is far enough to B and D .
211 Hence, this example shows the theoretical possibility that the shorter S-MT can result in the higher
212 S-MEC for a PSFP.

213 In this paper, the dimension error is used as the index for evaluating the machining deviation. The S-
214 MD is not positively correlated with the S-MT and the S-MEC. In other words, the reductions of S-
215 MT and S-MEC may result in the increase of S-MD. The conflict among the three objectives is test-

216 ed and verified in the following case study. Thus, it is required to develop the multi-objective model
 217 for optimising the trade-offs among S-MT, S-MD, and S-MEC.

218 Following the example, the multi-objective model for an n -feature part is developed. Because there
 219 are $n + 2$ features for an n -feature part in machining environment, a finite set is employed to indicate
 220 the positions of the features in a sequence as:

$$221 \quad S = \{S_k\}_{k=1}^{n+2} \quad (3)$$

222 where k is the index for the position in a feature sequence and S_k indicates the feature at the k -th po-
 223 sition of a sequence. For example, $S_k = F_p$ indicates that the feature at the k -th position is the feature
 224 F_p . For any part, the feature at the 1-st and $n + 2$ -th position is F_0 ($S_1 = F_0$) and F_{n+1} ($S_{n+2} = F_{n+1}$),
 225 respectively. The total S-MT and S-MEC based on a specific PSFP can be divided into the sequence-
 226 related non-cutting and cutting time and energy consumption. It is assumed that the S-MD for a
 227 PSFP is accumulated by the cutting and non-cutting deviations of each feature. Thus, the multi-
 228 objective function can be expressed as follows:

$$229 \quad \begin{cases} \text{minimise } T_s = \sum_{k=1}^{n+1} T_{non}^{(S_k, S_{k+1})} + \sum_{k=2}^{n+1} T_{cut}^{S_k} \\ \text{minimise } D_s = \sum_{k=1}^{n+1} D_{non}^{(S_k, S_{k+1})} + \sum_{k=2}^{n+1} D_{cut}^{S_k} \\ \text{minimise } E_s = \sum_{k=1}^{n+1} E_{non}^{(S_k, S_{k+1})} + \sum_{k=2}^{n+1} E_{cut}^{S_k} \end{cases} \quad (4)$$

230 where T_s , D_s , and E_s are the total S-MT, S-MD, and S-MEC, respectively, based on a specific PSFP;
 231 $T_{non}^{(S_k, S_{k+1})}$, $D_{non}^{(S_k, S_{k+1})}$, and $E_{non}^{(S_k, S_{k+1})}$ are the sequence-related non-cutting time, deviation, and energy
 232 consumption (S-NT, S-ND, and S-NEC), respectively, between the features at the k -th and $k + 1$ -th
 233 positions of the sequence; $T_{cut}^{S_k}$, $D_{cut}^{S_k}$, and $E_{cut}^{S_k}$ are the sequence-related cutting time, deviation, and
 234 energy consumption, respectively, for the feature at the k -th position of the sequence.

235 In this presented paper, it is assumed that each feature in the part does not have the volumetric inter-
 236 section with any other features. Consequently, the values of the cutting time, deviation, and energy
 237 consumption for all features keep equal whatever the PSFP is [21]. Thus, the cutting time, deviation,
 238 and energy consumption are not sequence-related, and $T_{cut}^{S_k}$, $D_{cut}^{S_k}$, and $E_{cut}^{S_k}$ are set to zero. Then, Ex-
 239 pression (4) can be simplified as:

240

$$\begin{cases} \text{minimise } T_s = \sum_{k=1}^{n+1} T_{non}^{(S_k, S_{k+1})} \\ \text{minimise } D_s = \sum_{k=1}^{n+1} D_{non}^{(S_k, S_{k+1})} \\ \text{minimise } E_s = \sum_{k=1}^{n+1} E_{non}^{(S_k, S_{k+1})} \end{cases} \quad (5)$$

241 The feature at the k -th and $k + 1$ -th position is F_p ($S_k = F_p$) and F_q ($S_{k+1} = F_q$), respectively. The
 242 non-cutting time of the machine tool can consist of the time consumed for the tool path, tool change,
 243 and spindle speed change [21]. Then, $T_{non}^{(S_k, S_{k+1})}$ can be expressed as:

244

$$T_{non}^{(S_k, S_{k+1})} = T_{non}^{(F_p, F_q)} = T_{tp}^{(F_p, F_q)} + T_{tc}^{(F_p, F_q)} + T_{src}^{(F_p, F_q)} \quad (6)$$

245 where $T_{tp}^{(F_p, F_q)}$, $T_{tc}^{(F_p, F_q)}$, and $T_{src}^{(F_p, F_q)}$ are the S-NT for the tool path, tool change, and spindle speed
 246 change, respectively, in the non-cutting from the feature F_p to the feature F_q .

247 A tool path from F_p to F_q can consist of m sequential feeding activities [20], and the time for the j -th
 248 feeding activity is denoted as $t_{pj}^{(F_p, F_q)}$. Thus, $T_{tp}^{(F_p, F_q)}$ can be expressed as:

249

$$T_{tp}^{(F_p, F_q)} = \sum_{j=1}^m t_{pj}^{(F_p, F_q)}. \quad (7)$$

250 Before calculating $t_{pj}^{(F_p, F_q)}$, it checks whether the feeding activity is sequence-related or not. If not
 251 sequence-related, then $t_{pj}^{(F_p, F_q)} = 0$. For example, in **Fig. 1**, the feeding activity from C to B is the 1-
 252 st feeding activity in the tool path from F_1 to F_2 and it is not sequence-related, thus $t_{p1}^{(F_1, F_2)} = 0$. If
 253 sequence-related, then $t_{pj}^{(F_p, F_q)}$ is calculated according to its feeding approaches (rapid and normal),
 254 and the calculation method can be found in Hu [20].

255 Before calculating $T_{tc}^{(F_p, F_q)}$ in Expression (6), it checks whether the tool change is sequence-related or
 256 not. If not sequence-related, then $T_{tc}^{(F_p, F_q)} = 0$. Otherwise, the value of $T_{tc}^{(F_p, F_q)}$ is calculated accord-
 257 ing to the number of tool stations rotated for changing tools [33].

258 In the non-cutting from F_p to F_q , the spindle rotation speed can change more than one time. Thus, in
 259 Expression (6), $T_{src}^{(F_p, F_q)}$ can be expressed as:

260

$$T_{src}^{(F_p, F_q)} = \sum_{g=1}^w t_{sg}^{(F_p, F_q)} \quad (8)$$

261 where $t_{sg}^{(F_p, F_q)}$ is the time for the g -th speed change of the spindle rotation in the non-cutting from F_p
 262 to F_q , w is the number of speed changes of the spindle rotation, and g is the index for a speed change
 263 of the spindle rotation. It checks whether the speed change of the spindle rotation is sequence-related
 264 or not. If not sequence-related, then $t_{sg}^{(F_p, F_q)} = 0$. Otherwise, $t_{sg}^{(F_p, F_q)}$ is calculated as:

$$265 \quad t_{sg}^{(F_p, F_q)} = \frac{2\pi(n_{Eg}^{pq} - n_{Sg}^{pq})}{60\alpha_A} \quad (9)$$

266 where n_{Sg}^{pq} and n_{Eg}^{pq} are the initial and end speed of the g -th speed change of the spindle rotation
 267 [rpm], and α_A is the angular acceleration of the spindle [rad/s²].

268 In Expression (5), $D_{non}^{(S_k, S_{k+1})}$ consists of the S-ND for m sequential feeding activities [20], and the S-
 269 ND for the j -th feeding activity is denoted as $d_j^{(F_p, F_q)}$. Then, $D_{non}^{(S_k, S_{k+1})}$ can be expressed as:

$$270 \quad D_{non}^{(S_k, S_{k+1})} = D_{non}^{(F_p, F_q)} = \sum_{j=1}^m d_j^{(F_p, F_q)}. \quad (10)$$

271 It is assumed that the machining deviation has a positive linear correlation with the machining dis-
 272 tance. Then, $d_j^{(F_p, F_q)}$ can be expressed as:

$$273 \quad d_j^{(F_p, F_q)} = B \times l_j^{pq} \quad (11)$$

274 where l_j^{pq} is the sequence-related non-cutting distance for the j -th feeding activity between the fea-
 275 tures F_p and F_q [mm]; coefficient B can be obtained by linear regression based on experiment data.
 276 For the three-axis CNC machine tools, the l_j^{pq} can be calculated by [32]:

$$277 \quad l_j^{pq} = \sqrt{(\Delta X_j^{pq})^2 + (\Delta Y_j^{pq})^2 + (\Delta Z_j^{pq})^2} \quad (12)$$

278 where ΔX_j^{pq} , ΔY_j^{pq} , and ΔZ_j^{pq} are the sequence-related relative distances of X-axis, Y-axis, and Z-axis
 279 between the start coordinate position $(x_{j-1}^{pq}, y_{j-1}^{pq}, z_{j-1}^{pq})$ and the end coordinate position $(x_j^{pq}, y_j^{pq},$
 280 $z_j^{pq})$ for the j -th feeding activity. Before calculating ΔX_j^{pq} , ΔY_j^{pq} , and ΔZ_j^{pq} , it checks whether the
 281 relative distance at the corresponding axis is sequence-related or not. The calculation for ΔX_j^{pq} is
 282 taken as example. If not sequence-related, then $\Delta X_j^{pq} = 0$. Otherwise, $\Delta X_j^{(F_p, F_q)} = |x_j^{pq} - x_{j-1}^{pq}|$.

283 In Expression (5), $E_{non}^{(S_k, S_{k+1})}$ is modelled based on the identification of the S-MP and the models in
284 Hu [21].

285 The constraint equations of the model are developed according to the precedence constraints among
286 the features [34]. For example, one of the precedence constraints is that a feature F_p should be pro-
287 cessed prior to a feature F_q , and then the constraint equation can be expressed as:

$$288 \quad \begin{cases} S_k = F_p \\ S_{k+z} = F_q \\ z \geq 1 \end{cases} \quad (13)$$

289 where z is a natural number. A feasible PSFP (solution) should satisfy all of the constraint equations.
290 The S-MT, the S-MD, and the S-MEC for the corresponding PSFP are set to infinity “ ∞ ” once any
291 feature and its pre- or post- features in a sequence violate any constraint equation.

292 **4. Multi-objective optimisation**

293 After developing the multi-objective (S-MT, S-MD, and S-MEC) model, the optimisation approach-
294 es such as deterministic algorithms and evolutionary algorithms can be employed to obtain the non-
295 dominated set of optimal solutions. According to the number of features in a part, suitable optimisa-
296 tion approaches can be selected. Normally, deterministic algorithms are used for the part with a small
297 number of features, and evolutionary algorithms are used for the part with a large number of features.
298 In existing research, the approach to clearly define the number of features as “small” or “large” has
299 not been provided.

300 In single objective (S-MT) optimisation, Wiener [35] presented that the computation time of deter-
301 ministic algorithms was short when the number of features in a part was fewer than 14. Thus, the
302 number of features fewer than 14 could be defined as “small”. When the number of features in-
303 creased to 20, the computation time of deterministic algorithms was intolerant [34]. Thus, the num-
304 ber of features more than 20 could be defined as “large”. Should the number of features between 14
305 and 20 be defined as “small” or “large”? Experiments are conducted in Section 5 to define them ac-
306 cording to the computation time.

307 The multi-objective model is more complex than the single objective (S-MT) model, thereby increas-
308 ing its computation time. As a result, the number of features fewer than 14 is probably classified as
309 “large” in the multi-objective optimisation for its long computation time.

310 4.1. *Optimisation for the part with a small number of features*

311 When the number of features in a part is small, the total number of feasible PSFPs will not be large.
312 The S-MT, S-MD, and S-MEC for all feasible PSFPs can be enumerated, calculated, and compared
313 in a short time. Non-dominated Inserting Enumeration Algorithm (NIEA) is proposed to optimise the
314 three objectives for the part with a small number of features. As a deterministic approach, NIEA can
315 accurately find the global optimal solution set in each run. According to the flowchart of NIEA in
316 **Fig. 3**, the working procedures for solving the multi-objective problem are as follows.

317 **Fig. 3.** Flowchart of NIEA.

318 Step 1: The index u for the solution (PSFP) is initialised to 1. According to Expression (2) and lexi-
319 cographical order [36], the 1-st solution is generated. If the solution does not satisfy Equation (13), it
320 is illegal and eliminated. Otherwise, the solution is inserted into the non-dominated set.

321 Step 2: The index is operated by $u = u + 1$, and the u -th solution is generated according to Expres-
322 sion (2) and lexicographical order.

323 Step 3: The legality of the u -th solution is checked. If the u -th solution does not satisfy Equation (13),
324 it is illegal and eliminated. Otherwise, Step 4 is performed.

325 Step 4: The u -th solution is verified and inserted into the non-dominated set based on the non-
326 dominated inserting operator. The non-dominated inserting operator is performed as follows. If the
327 u -th solution is non-dominated by all solutions in the current non-dominated set, the u -th solution is
328 inserted into the set, and the solutions dominated by the u -th solution are removed from the set. Oth-
329 erwise, the u -th solution itself is eliminated. For this operator, the rule for comparing two solutions is
330 as follows. If any objective value among S-MT, S-MD, and S-MEC of the solution X is greater than
331 that of the solution Y and the other two objectives values of the solution X are not smaller than those
332 of the solution Y, the solution X is dominated by (inferior to) solution Y. Otherwise, the solution X
333 is non-dominated by (not inferior to) the solution Y. The objectives values are calculated by Expres-
334 sion (5).

335 Step 5: NIEA checks whether the stopping conditions have been met or not. If the stopping condi-
336 tions are met, all of the solutions (PSFPs) in the latest non-dominated set and their values of S-MT,
337 S-MD, and S-MEC are reported, and NIEA stops. Otherwise, NIEA returns to Step 2. The index is

338 operated again by $u = u + 1$, and the next solution is generated and verified. The stopping condi-
339 tions can be that the u -th solution has been the end of the lexicographical order.

340 The performance of NIEA for optimising the parts with different number of features is tested in Sec-
341 tion 5.

342 4.2. *Optimisation for the part with a large number of features*

343 In real manufacturing environment, the complex parts normally have more than 20 features. If still
344 using NIEA, its computation time will be intolerant. As one of the most popular and effective non-
345 dominated sorting-based MOEAs [29], NSGA-II normally consumes much less time to obtain a sat-
346 isfying solution set [37] for the medium-to-large problems [38]. Thus, NSGA-II is used for the part
347 with a large number of features. However, NSAG-II can be easily trapped into the local optima, and
348 finding the global optimal solution set is not guaranteed [29]. Hence, experiments are conducted in
349 Section 5 to test the performance of NSGA-II in the solution quality. According to the flowchart of
350 NSGA-II in **Fig. 4**, the working procedures for solving the multi-objective problem are as follows.

351 **Fig. 4.** Flowchart of NSGA-II.

352 Step 1: The PSFP is encoded. According to Expression (2), the features to be encoded are collected.
353 According to Expression (3), the PSFPs are obtained. Each PSFP is encoded to a chromosome by
354 integer coding [39]. Each gene in the chromosome represents a specific feature. For example, a PSFP
355 $F_0-F_5-F_7-F_3-F_6-F_1-F_4-F_2-F_8$ can be encoded to a chromosome [057361428]. The gene 3 represents
356 the feature F_3 .

357 Step 2: An initial population P_0 that has N chromosomes is randomly generated. If the gene sequence
358 in a chromosome does not satisfy Equation (13), the corresponding chromosome is illegal. Then, the
359 gene sequence in the illegal chromosome is adjusted according to precedence constraints until Equa-
360 tion (13) has been met.

361 Step 3: All chromosomes in the population P_0 are ranked using two sorting procedures [27]: 1) a
362 non-dominated sorting procedure and 2) a crowding distance sorting procedure. The details about the
363 two sorting procedures can be referred to Deb [27]. In general, the chromosomes with the smaller S-
364 MT, S-MD, and S-MEC have the higher rank (fitness), and the three objectives values are calculated
365 according to Expression (5).

366 Step 4: The offspring population Q_0 is generated. At the 1-st generation, the GA operators, including
367 the selection, crossover, and mutation, create the offspring population Q_0 of N chromosomes. The
368 selection operator aims at selecting chromosomes in the current generation to reproduce offspring. A
369 binary tournament is adopted as the selection operator: between two chromosomes, the one with the
370 higher rank is selected [1]. The rank of each chromosome is determined as follows: the chromosomes
371 on the lower non-dominated level have the absolute higher rank; on the same non-dominated level,
372 the chromosomes with the greater value in the crowding distance have the higher rank [1]. More de-
373 tails about this selection operator can be referred to Blicke [40]. The partially mapped crossover [41]
374 and the swap mutation [1] are adopted as the crossover operator and the mutation operator, respec-
375 tively, and more details can be referred to Goldberg [41] and Liu [1].

376 Step 5: The generation number is operated by $t = t + 1$. At the t -th ($t \geq 2$) generation, the parent
377 population P_{t-2} and its offspring population Q_{t-2} are combined to create a new population as R_{t-2}
378 with a size of $2N$. The $2N$ chromosomes in the R_{t-2} are also ranked using the aforementioned two
379 sorting procedures. The N chromosomes with the highest rank are selected from the R_{t-2} to form the
380 new parent population P_{t-1} .

381 Step 6: The new offspring population Q_{t-1} that has N chromosomes is created through the selection,
382 crossover, and mutation operators.

383 Step 7: NSGA-II checks whether the stopping conditions have been met or not. If the stopping condi-
384 tion is met, the final population is decoded to report the set of optimal PSFPs that result in the opti-
385 mal trade-offs among S-MT, S-MD, and S-MEC, and NSGA-II stops. Otherwise, NSGA-II returns to
386 Step 5. The generation number is operated by $t = t + 1$, and the next population is created. This
387 generational process is repeated until a stopping condition has been met [42]. The stopping condition
388 can be the specified maximum generation number that is reached.

389 5. Case study

390 5.1. Case description, modelling, and optimisation

391 Three parts are used as the case studies to demonstrate the developed multi-objective models and op-
392 timisation approaches. Both part A and part B have 8 actual features (holes) denoted by $F_1 - F_8$ and 2
393 virtual features (F_0 and F_9), as shown in **Figs. 5** and **6**. The surfaces X and Y are selected as the pri-
394 mary positioning reference for part A, as marked in **Fig. 5**. Part C has 14 actual features denoted by

395 $F_1—F_{14}$ and 2 virtual features (F_0 and F_{15}), as shown in **Fig. 7**. In parts A, B, and C, each feature
 396 does not have volumetric intersections with the other features, and there is no specific constraint on
 397 the PSFP. A vertical machining centre (XHF-714F) manufactured by Hangzhou CNC Machine Tool
 398 Co., Ltd. of China is used to process the three parts. The experiment setup for the power data collec-
 399 tion on the XHF-714F is shown in **Fig. 8**. The key parameters of the XHF-714F required for calculat-
 400 ing the S-MT and the S-MEC are listed in Hu [21]. The coefficient B in the S-MD model is: $B =$
 401 0.001. They have been obtained through experiment measurement and regression analysis [32]. The
 402 spindle rotation speeds for each feature in parts A, B, and C are listed in **Table 1**, and the feed rates
 403 for all of the features are 0.09mm/rev. They have been obtained from the process files. On the basis
 404 of the above and additional case information provided in Hu [21], the S-MT, the S-MD, and the S-
 405 MEC can be calculated.

406 **Fig. 5.** Part A with 8 actual features and 2 virtual features.

407 **Fig. 6.** Part B with 8 actual features and 2 virtual features.

408 **Fig. 7.** Part C with 14 actual features and 2 virtual features.

409 **Fig. 8.** Diagram of the experiment setup for power data acquisition.

410 **Table 1** Spindle rotation speeds for the features in parts A, B, and C.

411 For parts A and B with 10 features, considering the position of the 2 virtual features on the sequence
 412 ($S_1 = F_0$, $S_{10} = F_9$), there are 81 [(10-1)*(10-1)] possible pairs of features. Similarly, there are 225
 413 [(16-1)*(16-1)] pairs of features for part C. In the following, the value calculation procedures for the
 414 S-NT, the S-ND, and the S-NEC between processing F_2 and F_6 ($T_{non}^{(F_2,F_6)}$, $D_{non}^{(F_2,F_6)}$, and $E_{non}^{(F_2,F_6)}$) in part
 415 A are used as examples.

416 Based on the above and Expression (6), the S-NT from F_2 to F_6 is:

$$417 T_{non}^{(F_2,F_6)} = T_{tp}^{(F_2,F_6)} + T_{tc}^{(F_2,F_6)} + T_{src}^{(F_2,F_6)}$$

418 where $E_{tp}^{(F_2,F_6)}$, $E_{tc}^{(F_2,F_6)}$, and $E_{src}^{(F_2,F_6)}$ are the S-NT for the tool path, tool change, and spindle speed
 419 change, respectively, in the non-cutting process from F_2 to F_6 .

420 There are three feeding activities in the non-cutting from F_2 to F_6 , as shown in **Fig. 5**. Thus, $T_{tp}^{(F_2, F_6)}$
 421 can be expressed as: $T_{tp}^{(F_2, F_6)} = t_{p1}^{(F_2, F_6)} + t_{p2}^{(F_2, F_6)} + t_{p3}^{(F_2, F_6)}$.

422 As shown in **Fig. 5**, the 1-st feeding activity (from A to B) and the 3-rd feeding activity (from C to D)
 423 are not sequence-related, thus $t_{p1}^{(F_2, F_6)} = 0s$ and $t_{p3}^{(F_2, F_6)} = 0s$. The 2-nd feeding activity (from B to C)
 424 is sequence-related, thus $t_{p2}^{(F_2, F_6)}$ is calculated as follows. The feeding approach from B to C is rapid
 425 feeding, and the coordinates of the points B and C are $(0, 60, 7)$ and $(25, 15, 7)$, respectively. Based
 426 on the time model for rapid feeding in Hu [20], the value of $t_{p2}^{(F_2, F_6)}$ is $0.225s$. Then, $T_{tp}^{(F_2, F_6)}$ is calcu-
 427 lated as: $T_{tp}^{(F_2, F_6)} = 0 + 0.225 + 0 = 0.225s$.

428 In the non-cutting from F_2 to F_6 , there is no tool change, thus $T_{tc}^{(F_2, F_6)} = 0s$.

429 There is only one speed change of the spindle rotation within this case. According to Expression (8),
 430 $E_{src}^{(F_2, F_6)}$ is expressed as: $T_{src}^{(F_2, F_6)} = t_{s1}^{(F_2, F_6)}$. The spindle rotation speeds for F_2 and F_6 are $550rpm$ and
 431 $800rpm$ according to **Table 1**, thus $n_{s1}^{26} = 550rpm$ and $n_{E1}^{26} = 800rpm$. The angular acceleration is
 432 $1047.20rad/s^2$. Then, Equation (9) is employed to calculate $t_{s1}^{(F_2, F_6)}$ as: $t_{s1}^{(F_2, F_6)} = \frac{2\pi \times (800 - 550)}{60 \times 1047.20} =$
 433 $0.025s$.

434 By summing $T_{tp}^{(F_2, F_6)}$, $T_{tc}^{(F_2, F_6)}$, and $T_{src}^{(F_2, F_6)}$, the S-NT from F_2 to F_6 is:

$$435 T_{non}^{(F_2, F_6)} = 0.225 + 0 + 0.025 = 0.250s.$$

436 According to Expression (10), the S-ND from F_2 to F_6 is:

$$437 D_{non}^{(F_2, F_6)} = d_1^{(F_2, F_6)} + d_2^{(F_2, F_6)} + d_3^{(F_2, F_6)}.$$

438 As shown in **Fig. 5**, the 1-st feeding activity and the 3-rd feeding activity are not sequence-related,
 439 thus $d_1^{(F_2, F_6)} = 0\mu m$ and $d_3^{(F_2, F_6)} = 0\mu m$. The 2-nd feeding activity (from B to C) is sequence-related.
 440 The coordinates of the points B and C are $(0, 60, 7)$ and $(25, 15, 7)$, respectively. The relative dis-
 441 tance at the Z -axis axis is not sequence-related. According to Expressions (11)-(12) and coefficient
 442 $B = 0.001$, $d_2^{(F_2, F_6)}$ is calculated as:

$$443 d_2^{(F_2, F_6)} = 0.001 \times \sqrt{(25)^2 + (-45)^2 + (0)^2} = 51.48\mu m.$$

444 Finally, $D_{non}^{(F_2, F_6)}$ is: $D_{non}^{(F_2, F_6)} = 0 + 51.48 + 0 = 51.48\mu\text{m}$.

445 Based on the identification of the S-MP and the models in Hu [21], the value of $E_{non}^{(F_2, F_6)}$ is 438.89J.

446 Following the calculations of $T_{non}^{(F_2, F_6)}$, $D_{non}^{(F_2, F_6)}$, and $E_{non}^{(F_2, F_6)}$, the S-NT, the S-ND, and the S-NEC for
447 the other 80 pairs of features in part A are calculated based on the similar procedures, and the results
448 are listed in **Tables 2, 3, and 4**. In addition, the S-NT and the S-NEC for 81 and 225 pairs of features
449 in parts B and C are provided in **Tables S1, S2, S3, and S4** of the Supplementary Information (SI).
450 To test the conflict between the S-NT and the S-NEC, the S-ND for parts B and C is set to zero. In
451 this case, the feeding approach for all sequence-related feeding activities is rapid feeding. The rapid
452 feeding speeds of the X-axis, the Y-axis, and the Z-axis of the machine tool (XHF-714F) are high,
453 which are 12m/min, 12m/min, and 10m/min, respectively. Thus, the values of the S-NT between the
454 features in the three parts are small.

455 **Table 2** S-NT for 81 pairs of features in part A.

456 **Table 3** S-ND for 81 pairs of features in part A.

457 **Table 4** S-NEC for 81 pairs of features in part A.

458 Based on the data and models above and the supplementary tables in the SI, two solution algorithms,
459 NIEA and NSGA-II, are employed as optimisation approaches. In this research, NIEA and NSGA-II
460 are developed on Dev C++ 5.11.0 software with the programming language C++. The C++ code of
461 NIEA can be found at the SI. The computing platform is Intel (R) Core (TM) i7-2630 QM CPU with
462 2.00 GHz frequency; 4.00 GB RAM; Windows 7 (64bit) operating system. The parameter values
463 used in NSGA-II are obtained by fine tuning, and their values are as follows: population size = 50;
464 crossover probability = 0.9; mutation probability = 0.15; generation number = 100 (parts A and B)
465 or 200 (part C).

466 The S-MD is set to zero first. NIEA and NSGA-II are run 10 times for parts A, B, and C, respective-
467 ly, according to standard deviation. The results from using NIEA and NSGA-II for optimising the
468 feature sequences of these parts are summarised and compared in **Table 5** and **Figs. 9, 10, and 11**. As
469 a deterministic algorithm, NIEA can always obtain the non-dominated set of Pareto-optimal solutions
470 for parts A, B, and C. The results are listed in **Table 5**, including the set of the optimal PSFPs and
471 their objectives values. In particular, there is only one solution for part B, and it means the PSFP with

472 the minimum S-MEC also results in the minimum S-MT. The optimal solution sets for parts A, B,
473 and C obtained by NIEA are also shown in **Figs. 9, 10, and 11.**

474 **Table 5** The results obtained by BTT and NIEA for parts A, B, and C.

475 **Fig. 9.** Comparison of solution quality between NIEA and NSGA-II for part A.

476 **Fig. 10.** Comparison of solution quality between NIEA and NSGA-II for part B.

477 **Fig. 11.** Comparison of solution quality between NIEA and NSGA-II for part C.

478 Then, the S-MD for part A is set to the values in **Table 3**, and NIEA is employed to find the set of
479 optimal solutions (PSFPs) that result in the optimal trade-offs among S-MT, S-MD, and S-MEC. The
480 solution set of part A is listed in **Table 6**, and its computation time is 0.1763s. It demonstrates that
481 the reduction of S-MD can result in the increase of S-MT and S-MEC.

482 **Table 6** The solutions obtained by NIEA for the multi-objective model of part A.

483 5.2. Results and analysis

484 To demonstrate the effectiveness of the proposed approaches in reducing the S-MT, the S-MD, and
485 the S-MEC, the following comparison is performed. A feature sequence produced by the sequencing
486 technique Bottom-to-Top (BTT) [43] serves as the benchmark to represent the traditional approach to
487 arranging the PSFP. Then, the benchmark PSFP for parts A, B, and C is $F_0 - F_1 - F_5 - F_6 - F_7 - F_4$
488 $- F_3 - F_2 - F_8 - F_9$, $F_0 - F_4 - F_5 - F_8 - F_3 - F_1 - F_6 - F_7 - F_2 - F_9$, and $F_0 - F_4 - F_{14} - F_6 - F_5 - F_{11}$
489 $- F_{10} - F_7 - F_1 - F_3 - F_9 - F_8 - F_{12} - F_{13} - F_2 - F_{15}$, respectively. Based on the data in **Table 2**,
490 **Table 4**, and supplementary tables in the SI, the S-MT and the S-MEC for the benchmark PSFPs are
491 calculated and listed in **Table 5**. According to **Table 3**, the S-MD based on the benchmark PSFP for
492 part A is 553.28 μ m.

493 By comparing the S-MT and S-MEC values in **Table 5**, 23.00% [(4.022-3.097)/4.022] to 25.41%
494 [(4.022-3.000)/4.022] S-MT and 19.47% [(6321.99-5091.26)/6321.99] to 22.33% [(6321.99-
495 4910.49)/6321.99] S-MEC are reduced for part A; 33.13% [(3.737-2.499)/3.737] S-MT and 26.86%
496 [(5790.27-4235.01)/5790.27] S-MEC are reduced for part B; 39.14% [(6.728-4.095)/6.728] to 41.90%
497 [(6.728-3.909)/6.728] S-MT and 33.68% [(9871.92-6547.28)/9871.92] to 38.36% [(9871.92-
498 6085.46)/9871.92] S-MEC are reduced for part C. The results verify the conflict between the mini-
499 misation of S-MT and S-MEC. According to the processing constraints for the S-MT, the optimal

500 PSFP can be selected from the solution set. For example, the S-MT for parts A and C is restrained to
501 be not longer than 3.000 and 4.000 seconds, respectively. Thus, the 1-st sequence $F_0 - F_6 - F_8 - F_7$
502 $- F_4 - F_2 - F_3 - F_5 - F_1 - F_9$ and the 3-rd sequence $F_0 - F_1 - F_7 - F_8 - F_2 - F_9 - F_{10} - F_3 - F_{13} - F_{12}$
503 $- F_{11} - F_{14} - F_6 - F_4 - F_5 - F_{15}$ are selected for parts A and C, as shown in **Figs. 5** and **7**, because
504 they consume the minimum S-MEC under the S-MT constraints.

505 By comparing the three objectives values generated by NIEA and BTT according to **Table 6**, 20.51%
506 $[(4.022-3.197)/4.022]$ to 25.41% $[(4.022-3.000)/4.022]$ S-MT, 5.29% $[(553.28-524.01)/553.28]$ to
507 27.90% $[(553.28-398.92)/553.28]$ S-MD, and 16.66% $[(6321.99-5268.75)/6321.99]$ to 22.33%
508 $[(6321.99-4910.49)/6321.99]$ S-MEC are reduced for part A through the multi-objective optimisation.

509 Further, the performances between the two algorithms (NIEA and NSGA-II) for parts A, B, and C
510 are compared and summarised in **Table 7**. The deterministic algorithm, NIEA, can always return the
511 global optimum. By comparison, NSGA-II can find an optimal or near-optimal solution set. Particu-
512 larly, NSGA-II obtained the global optimum for part B sometimes, but it has never obtained the
513 global optimum for parts A and C in our trials.

514 **Table 7** Performance comparison between NIEA and NSGA-II for parts A, B, and C.

515 The hypervolume indicator is employed to evaluate the solution quality of the two algorithms [44].
516 The maximum objectives values of the 10 trials are taken as the coordinate values of the reference
517 point. Then, the reference points of parts A, B, and C are A(3.098, 5111.05), B(2.585, 4398.92), and
518 C(4.205, 6560.02), respectively, as shown in **Figs. 9, 10, and 11**. Based on the reference points and
519 the objectives values of the solutions, the hypervolume indicator of NIEA and NSGA-II for parts A,
520 B, and C can be obtained by calculating the size of the dominated subspaces. In **Figs. 9, 10, and 11**,
521 the spaces surrounded by red solid lines and blue dotted lines represent the dominated subspaces by
522 the solutions of NIEA and NSGA-II, respectively. The higher hypervolume indicator reflects the bet-
523 ter solution quality. The calculated hypervolume indicators and the computation time are summarised
524 in **Table 7**. The hypervolume indicators of NIEA for parts A, B, and C are 14.41, 14.10, and 120.88,
525 respectively. By comparison, the median hypervolume indicators of NSGA-II for parts A, B, and C
526 are 10.69, 10.37, and 68.80, respectively. Thus, it verifies that NIEA performs better than NSGA-II
527 in solution quality.

528 Although the computation time of NIEA for parts A and B is shorter than that of NSGA-II, its com-
529 putation time for part C (21970s) is much longer than that of NSGA-II (54.95s). To better compare

530 the computation time between NIEA and NSGA-II, the algorithms are performed for the other five
531 parts from 9 to 13 actual features, and the results are listed in **Table 8**. According to **Tables 7** and **8**,
532 NIEA performs better than NSGA-II in both solution quality and computation time for the part with
533 fewer than 12 features, thus NIEA is recommended. For the part with 12 or more features, the com-
534 putation time of NIEA becomes longer than that of NSGA-II, and it is required to make a trade-off
535 between the computation time and the solution quality when selecting an algorithm. While the num-
536 ber of features of a part is increasing, the computation time of NIEA increases sharply whereas the
537 computation time of NSGA-II increases slightly, as reflected in **Tables 7** and **8**. For example, for part
538 B that has 8 features, the computation time of NIEA is only 0.128% ($0.0274/21.33$) of that of NSGA-
539 II. However, when the number of features increases to 14 such as in part C, the computation time of
540 NIEA becomes 399 ($21970/54.95$) times more than that of NSGA-II. Hence, when the number of
541 features of a part increases to 14 or more, NSGA-II may be more preferable to get a near-optimal so-
542 lution set within a tolerable computation time.

543 **Table 8** Computation time comparison between NIEA and NSGA-II for the other five parts.

544 **6. Discussion**

545 The case study has shown that the computation time of NIEA is intolerant when the number of fea-
546 tures increases to 14. Although NSGA-II consumes a short computation time, its solution quality is
547 not high. The algorithms with better performance in computation speed and solution quality should
548 be designed and discussed. Research has proved that hybridising the deterministic algorithm with the
549 evolutionary algorithm can improve the algorithm performance [45]. In this paper, the proposed
550 NIEA hybridises with NSGA-II to develop a novel hybrid algorithm for solving our multi-objective
551 feature sequencing problem, and this hybrid algorithm is named Genetic-based Non-dominated
552 Enumeration Algorithm (GNEA). GNEA is an improved enumeration algorithm.

553 In proposed GNEA, NSGA-II is performed first to obtain the set of optimal or near-optimal PSFPs as
554 an initial upper bound [46] before performing NIEA. With the help of this initial bound, many inferi-
555 or PSFPs can be efficiently pruned, thereby reducing the computation time of GNEA. As a kind of
556 enumeration algorithm, the solution quality of GNEA is the same as that of NIEA, and the global op-
557 timum is guaranteed. Experiments are performed to test the computation time of GNEA.

558 GNEA is programmed by language C++, and part C with 14 actual features is used as an example.
559 The computation time of GNEA is 5960s, which is 72.87% [$(21970-5960)/21970$] shorter than that

560 of NIEA. It validates that the proposed hybrid algorithm GNEA is an effective deterministic optimi-
561 sation approach for solving the medium-to-large feature sequencing problem. However, the perfor-
562 mance of GNEA is not always better than that of NIEA in computation time. Specifically, the com-
563 putation time of GNEA is longer than that of NSGA-II because NSGA-II is entirely included in
564 GNEA. As a result, the computation time of GNEA is longer than that of NIEA for the part with
565 fewer than 12 features, and NIEA is still recommended.

566 **7. Conclusions and future work**

567 It has been approved that the machining energy consumption can be reduced through sequencing the
568 features of a part at the process planning stage. The single objective model that only minimises the S-
569 MEC has been developed in previous research. However, the S-MT and the S-MD have not been
570 considered. In this article, the conflict between the S-MT and the S-MEC has been verified, and the
571 S-MT and the S-MD have been developed as two new objectives. Further, the developed S-MT and
572 S-MD models are integrated with the existing S-MEC model to obtain the multi-objective model.
573 The time and power data of the machine tool in the model are obtained from experiment measure-
574 ment. Accordingly, a multi-objective feature sequencing problem, which minimises the S-MT, the S-
575 MD, and the S-MEC, is introduced. To solve this problem, the two algorithms (NIEA and NSGA-II)
576 are proposed as the optimisation approaches that obtain the non-dominated set of optimal solutions.
577 An optimal solution represents a PSFP that results in the optimal trade-off among the three objectives.
578 Because NIEA can always find the global optimum, the results obtained by NSGA-II can be com-
579 pared and evaluated.

580 In the case study, the optimal solution sets for three parts with 8, 8, and 14 actual features have been
581 found. According to the optimisation results, NSGA-II usually returns a near-optimal solution set. By
582 comparison, NIEA always returns the global optimal solution set. Therefore, NIEA performs better
583 than NSGA-II in terms of solution quality. Based on the experiment results of the two algorithms for
584 eight parts, NIEA is recommended for the part with fewer than 12 actual features because it con-
585 sumes the shorter computation time than that of NSGA-II. For the part with 12 or more features, the
586 computation time of NIEA becomes longer than that of NSGA-II, and a trade-off between the com-
587 putation time and the solution quality should be made when selecting an algorithm. By using the
588 multi-objective feature sequencing approach, 20.51% S-MT, 5.29% S-MD, and 16.66% S-MEC can
589 be reduced. To obtain the global optimum more quickly for the 14-feature part, a novel hybrid algo-

590 rithm GNEA is proposed and compared. The computation time of GNEA is 72.87% shorter than that
591 of NIEA for the 14-feature part.

592 In this presented paper, the model is only suitable for the parts without the feature intersection. In
593 real manufacturing circumstance, the feature intersections widely exist in the parts. The model can be
594 improved for the parts with the feature intersections, through developing the sub-models for the se-
595 quence-related cutting time, deviation, and energy consumption. Further, the model can be improved
596 by considering more objectives, such as the machining roughness, tolerance, reliability, and cost, and
597 the mathematic relationship between these new objectives and the PSFP should be developed. The
598 single machine environment is a limitation of this presented research. Usually, more than one ma-
599 chine is required to finish a part, with consuming the time and energy of machine tools for setup
600 change and machine change. In the next step, the S-MT and the S-MEC in multi-machine environ-
601 ment should be modelled. For the optimisation approaches, the computation speed of deterministic
602 algorithms and the solution quality of evolutionary algorithms can be further improved. In the future,
603 the proposed feature sequencing approach will be combined with the existing energy-aware schedul-
604 ing approach to promote the energy-aware integrated process planning and scheduling.

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610 **Appendix A. Supplementary data**

611 Supplementary data related to this article can be found at the Supplementary Information (SI).

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Table 1 Spindle rotation speeds for the features in parts A, B, and C.

| The i -th feature in part A | The i -th feature in part B | The i -th feature in part C | Spindle rotation speed [rpm] |
|-------------------------------|-------------------------------|-------------------------------|------------------------------|
| F_1 | F_1, F_3 | F_1, F_3 | 500 |
| F_2 | F_2, F_4 | F_2, F_4 | 550 |
| F_3 | F_5, F_6 | F_5 | 700 |
| F_4 | F_7, F_8 | F_6 | 650 |
| F_5 | | F_7, F_8 | 600 |
| F_6 | | F_9, F_{10} | 800 |
| F_7 | | F_{11}, F_{12} | 450 |
| F_8 | | F_{13}, F_{14} | 750 |

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Table 2 S-NT for 81 pairs of features in part A.

| Time [s] | F_1 | F_2 | F_3 | F_4 | F_5 | F_6 | F_7 | F_8 | F_9 |
|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| F_0 | 0.575 | 0.880 | 0.785 | 0.855 | 0.660 | 0.805 | 1.095 | 1.200 | ∞ |
| F_1 | ∞ | 0.305 | 0.210 | 0.505 | 0.185 | 0.455 | 0.756 | 0.850 | 0.582 |
| F_2 | 0.306 | ∞ | 0.205 | 0.200 | 0.230 | 0.250 | 0.461 | 0.545 | 0.887 |
| F_3 | 0.213 | 0.207 | ∞ | 0.386 | 0.126 | 0.325 | 0.668 | 0.720 | 0.794 |
| F_4 | 0.507 | 0.201 | 0.385 | ∞ | 0.321 | 0.130 | 0.283 | 0.345 | 0.864 |
| F_5 | 0.186 | 0.231 | 0.125 | 0.320 | ∞ | 0.270 | 0.592 | 0.665 | 0.668 |
| F_6 | 0.459 | 0.253 | 0.326 | 0.132 | 0.273 | ∞ | 0.365 | 0.406 | 0.816 |
| F_7 | 0.755 | 0.460 | 0.665 | 0.280 | 0.590 | 0.360 | ∞ | 0.205 | 1.101 |
| F_8 | 0.853 | 0.548 | 0.721 | 0.346 | 0.667 | 0.405 | 0.209 | ∞ | 1.210 |

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Table 3 S-ND for 81 pairs of features in part A.

| Deviation [μm] | F_1 | F_2 | F_3 | F_4 | F_5 | F_6 | F_7 | F_8 | F_9 |
|--------------------------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| F_0 | 120.93 | 204.02 | 164.84 | 213.10 | 153.05 | 188.22 | 246.98 | 279.02 | ∞ |
| F_1 | ∞ | 84.85 | 43.91 | 105.11 | 38.08 | 86.31 | 152.07 | 175.57 | 0 |
| F_2 | 84.85 | ∞ | 43.91 | 43.91 | 51.48 | 51.48 | 96.57 | 105 | 0 |
| F_3 | 43.91 | 43.91 | ∞ | 76 | 26.42 | 67.07 | 128.66 | 144.68 | 0 |
| F_4 | 105.11 | 43.91 | 76 | ∞ | 67.07 | 26.42 | 53.60 | 70.52 | 0 |
| F_5 | 38.08 | 51.48 | 26.42 | 67.07 | ∞ | 50 | 115.43 | 137.57 | 0 |
| F_6 | 86.31 | 51.48 | 67.07 | 26.42 | 50 | ∞ | 65.76 | 91.79 | 0 |
| F_7 | 152.07 | 96.57 | 128.66 | 53.60 | 115.43 | 65.76 | ∞ | 38.08 | 0 |
| F_8 | 175.57 | 105 | 144.68 | 70.52 | 137.57 | 91.79 | 38.08 | ∞ | 0 |

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Table 4 S-NEC for 81 pairs of features in part A.

| Energy [J] | F_1 | F_2 | F_3 | F_4 | F_5 | F_6 | F_7 | F_8 | F_9 |
|------------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| F_0 | 1065.33 | 1624.95 | 1435.98 | 1767.06 | 1330.39 | 1711.47 | 1973.30 | 2316.91 | ∞ |
| F_1 | ∞ | 556.07 | 358.34 | 788.00 | 302.77 | 723.91 | 1027.85 | 1323.86 | 965.80 |
| F_2 | 539.45 | ∞ | 368.00 | 343.83 | 338.89 | 438.89 | 670.02 | 770.05 | 1497.85 |
| F_3 | 274.29 | 303.94 | ∞ | 495.99 | 166.65 | 521.41 | 862.89 | 1012.12 | 1210.50 |
| F_4 | 732.75 | 303.73 | 517.21 | ∞ | 468.08 | 241.95 | 369.65 | 540.18 | 1576.99 |
| F_5 | 265.85 | 320.30 | 210.69 | 487.93 | ∞ | 423.28 | 769.88 | 1026.68 | 1173.12 |
| F_6 | 588.21 | 319.80 | 472.50 | 167.03 | 327.08 | ∞ | 440.08 | 639.07 | 1407.35 |
| F_7 | 1040.89 | 701.29 | 956.58 | 445.90 | 819.09 | 599.01 | ∞ | 357.04 | 1898.72 |
| F_8 | 1225.92 | 685.17 | 990.69 | 494.74 | 963.61 | 663.50 | 224.78 | ∞ | 2053.42 |

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Table 5 The results obtained by BTT and NIEA for parts A, B, and C.

| | BTT | | NIEA | | |
|--------|----------|-----------|---|----------|-----------|
| | S-MT [s] | S-MEC [J] | The set of the optimal PSFPs | S-MT [s] | S-MEC [J] |
| Part A | 4.022 | 6321.99 | $F_0 - F_6 - F_8 - F_7 - F_4 - F_2 - F_3 - F_5 - F_1 - F_9$ | 3.000 | 5091.26 |
| | | | $F_0 - F_1 - F_5 - F_3 - F_2 - F_4 - F_7 - F_8 - F_6 - F_9$ | 3.001 | 5024.09 |
| | | | $F_0 - F_1 - F_5 - F_3 - F_2 - F_4 - F_8 - F_7 - F_6 - F_9$ | 3.022 | 4997.88 |
| | | | $F_0 - F_1 - F_3 - F_2 - F_4 - F_7 - F_8 - F_6 - F_5 - F_9$ | 3.026 | 4961.82 |
| | | | $F_0 - F_1 - F_3 - F_2 - F_4 - F_8 - F_7 - F_6 - F_5 - F_9$ | 3.047 | 4935.61 |
| | | | $F_0 - F_1 - F_3 - F_2 - F_8 - F_7 - F_4 - F_6 - F_5 - F_9$ | 3.097 | 4910.49 |
| Part B | 3.737 | 5790.27 | $F_0 - F_1 - F_6 - F_2 - F_7 - F_3 - F_8 - F_4 - F_5 - F_9$ | 2.499 | 4235.01 |
| Part C | 6.728 | 9871.92 | $F_0 - F_7 - F_1 - F_8 - F_2 - F_9 - F_{10} - F_{13} - F_{12} - F_3 - F_{11} - F_{14} - F_6 - F_4 - F_5 - F_{15}$ | 3.909 | 6547.28 |
| | | | $F_0 - F_1 - F_7 - F_8 - F_2 - F_9 - F_{10} - F_{13} - F_{12} - F_3 - F_{11} - F_{14} - F_6 - F_4 - F_5 - F_{15}$ | 3.913 | 6288.12 |
| | | | $F_0 - F_1 - F_7 - F_8 - F_2 - F_9 - F_{10} - F_3 - F_{13} - F_{12} - F_{11} - F_{14} - F_6 - F_4 - F_5 - F_{15}$ | 3.980 | 6121.71 |
| | | | $F_0 - F_1 - F_7 - F_8 - F_2 - F_9 - F_{10} - F_3 - F_{12} - F_{13} - F_{14} - F_{11} - F_6 - F_4 - F_5 - F_{15}$ | 4.095 | 6085.46 |

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Table 6 The solutions obtained by NIEA for the multi-objective model of part A.

| The set of optimal feature sequences of part A | S-MT [s] | S-MEC [J] | S-MD [μm] |
|--|----------|-----------|------------------------|
| $F_0-F_6-F_8-F_7-F_4-F_2-F_3-F_5-F_1-F_9$ | 3.000 | 5091.26 | 524.01 |
| $F_0-F_1-F_5-F_3-F_2-F_4-F_7-F_8-F_6-F_9$ | 3.001 | 5024.09 | 456.72 |
| $F_0-F_1-F_5-F_3-F_2-F_4-F_8-F_7-F_6-F_9$ | 3.022 | 4997.88 | 447.61 |
| $F_0-F_1-F_3-F_2-F_4-F_7-F_8-F_6-F_5-F_9$ | 3.026 | 4961.82 | 486.13 |
| $F_0-F_1-F_3-F_2-F_4-F_8-F_7-F_6-F_5-F_9$ | 3.047 | 4935.61 | 477.02 |
| $F_0-F_1-F_5-F_3-F_2-F_8-F_7-F_4-F_6-F_9$ | 3.072 | 4972.76 | 452.44 |
| $F_0-F_1-F_3-F_2-F_8-F_7-F_4-F_6-F_5-F_9$ | 3.097 | 4910.49 | 481.85 |
| $F_0-F_1-F_5-F_3-F_2-F_6-F_4-F_8-F_7-F_9$ | 3.129 | 5152.33 | 415.84 |
| $F_0-F_1-F_5-F_6-F_7-F_8-F_4-F_2-F_3-F_9$ | 3.146 | 4965.48 | 471.19 |
| $F_0-F_1-F_5-F_3-F_2-F_6-F_4-F_7-F_8-F_9$ | 3.172 | 5268.75 | 398.92 |
| $F_0-F_1-F_5-F_6-F_4-F_7-F_8-F_2-F_3-F_9$ | 3.197 | 4948.77 | 476.02 |

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Table 7 Performance comparison between NIEA and NSGA-II for parts A, B, and C.

| Part names | | Part A | Part B | Part C |
|---------------------------|-------------------------------|--------|--------|--------|
| Number of actual features | | 8 | 8 | 14 |
| NIEA | Hypervolume indicator | 14.41 | 14.10 | 120.88 |
| | Computation time [s] | 0.0286 | 0.0274 | 21970 |
| NSGA-II | Maximum hypervolume indicator | 11.08 | 14.10 | 99.34 |
| | Median hypervolume indicator | 10.69 | 10.37 | 68.80 |
| | Computation time [s] | 20.37 | 21.33 | 54.95 |

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Table 8 Computation time comparison between NIEA and NSGA-II for the other five parts.

| Part names | | Part D | Part E | Part F | Part G | Part H |
|---------------------------|---------|--------|--------|--------|--------|--------|
| Number of actual features | | 9 | 10 | 11 | 12 | 13 |
| Computation time [s] | NIEA | 0.297 | 1.048 | 10.42 | 121.2 | 1554 |
| | NSGA-II | 22.71 | 23.73 | 24.86 | 25.14 | 27.35 |

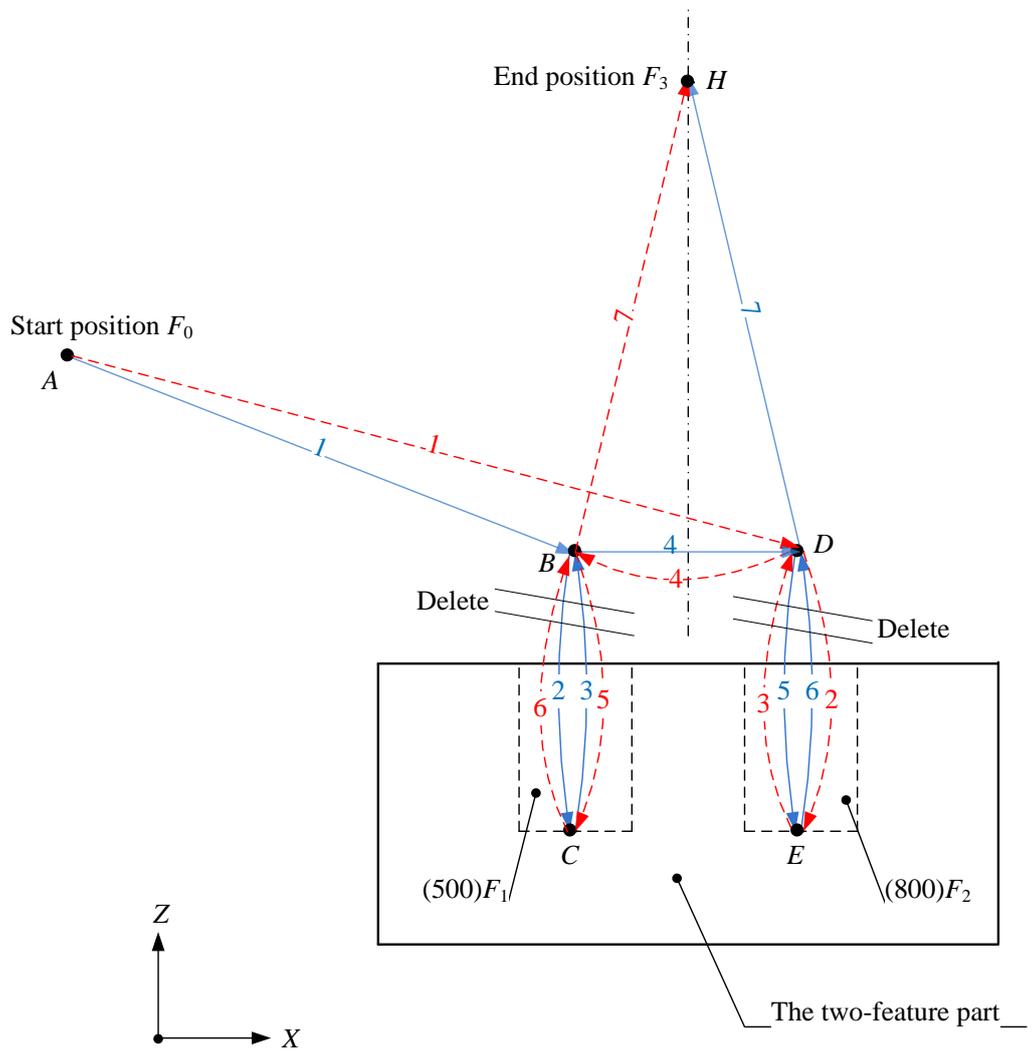
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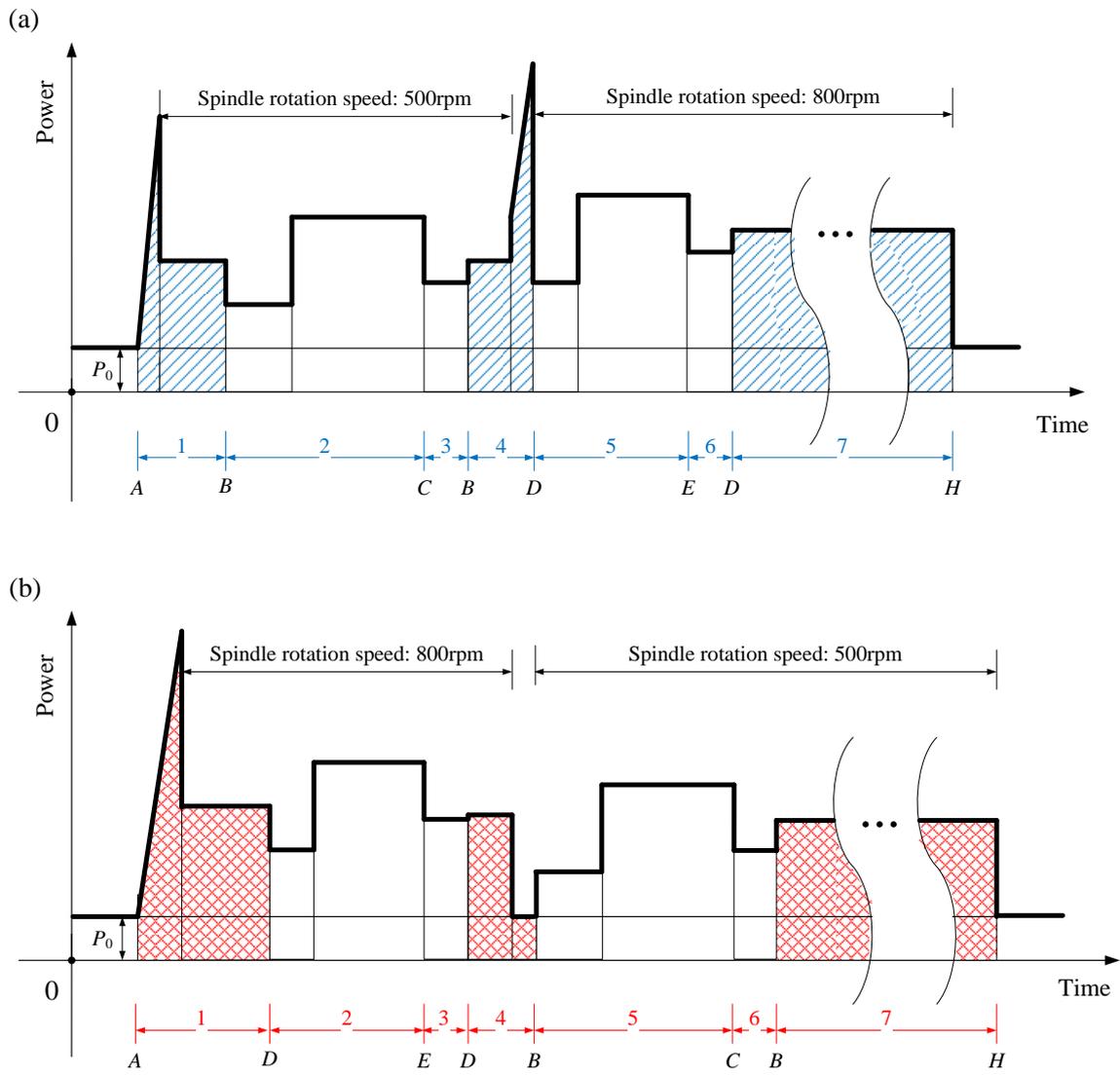
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Fig. 1. A two-feature part that has two possible processing sequences.

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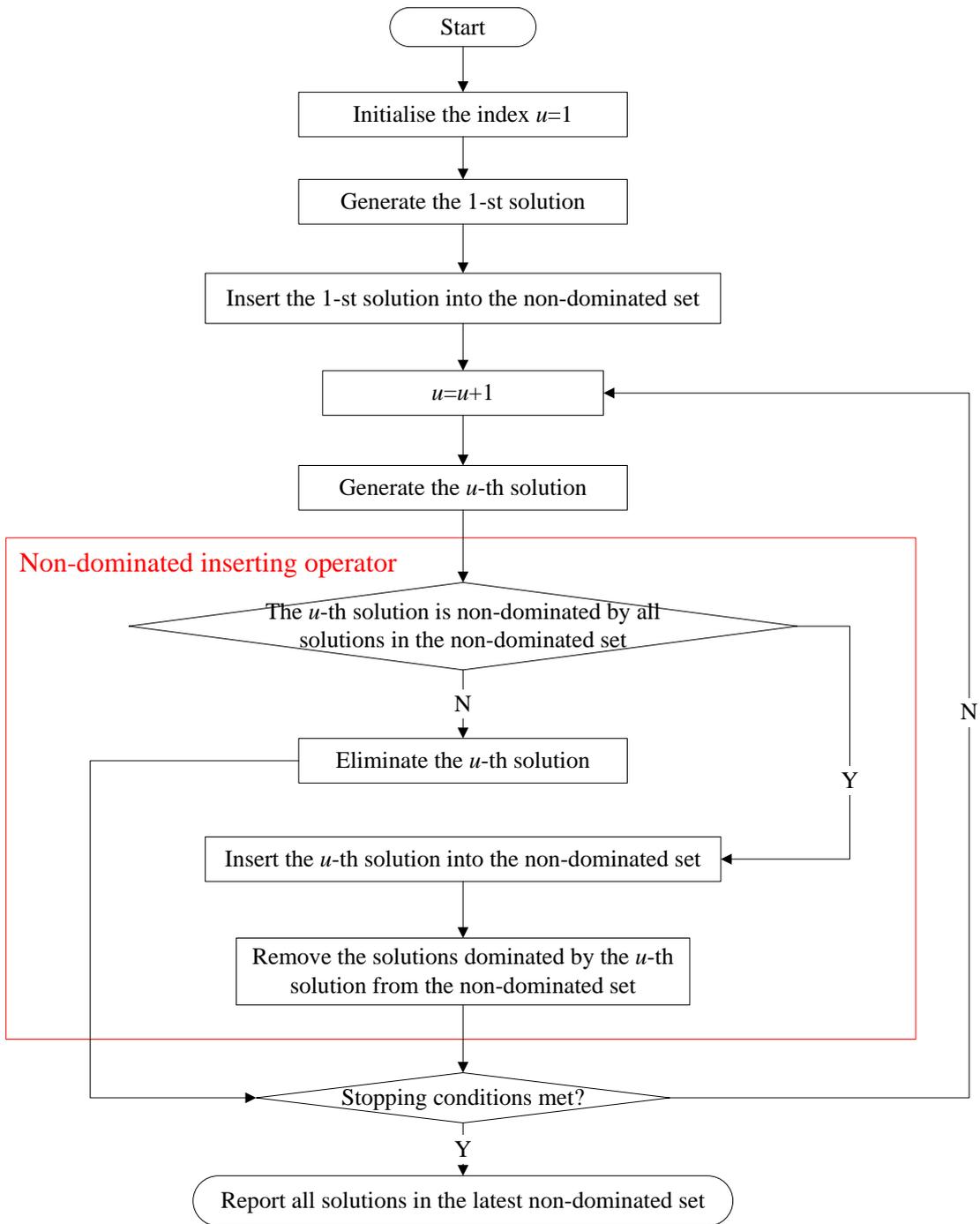
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Fig. 2. Power profiles of two different sequences: (a) $F_0-F_1-F_2-F_3$; (b) $F_0-F_2-F_1-F_3$.

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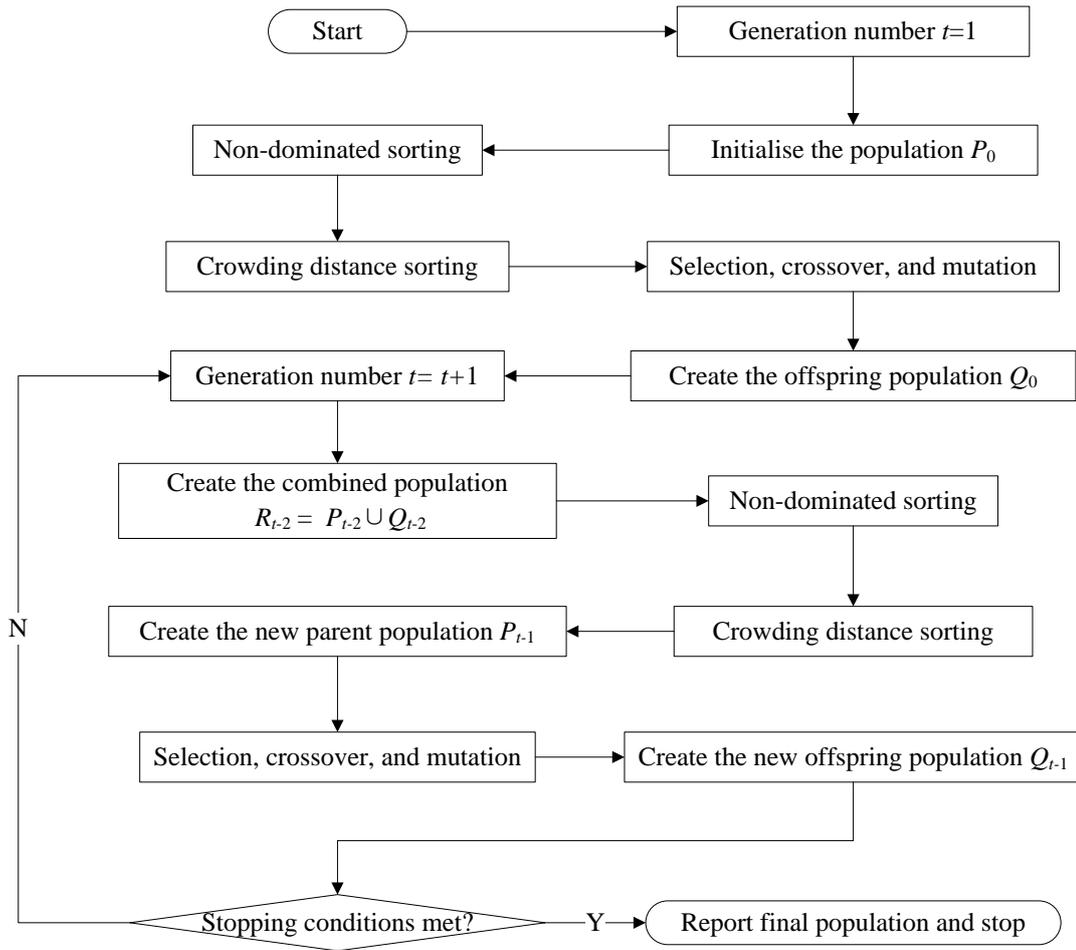
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Fig. 3. Flowchart of NIEA.

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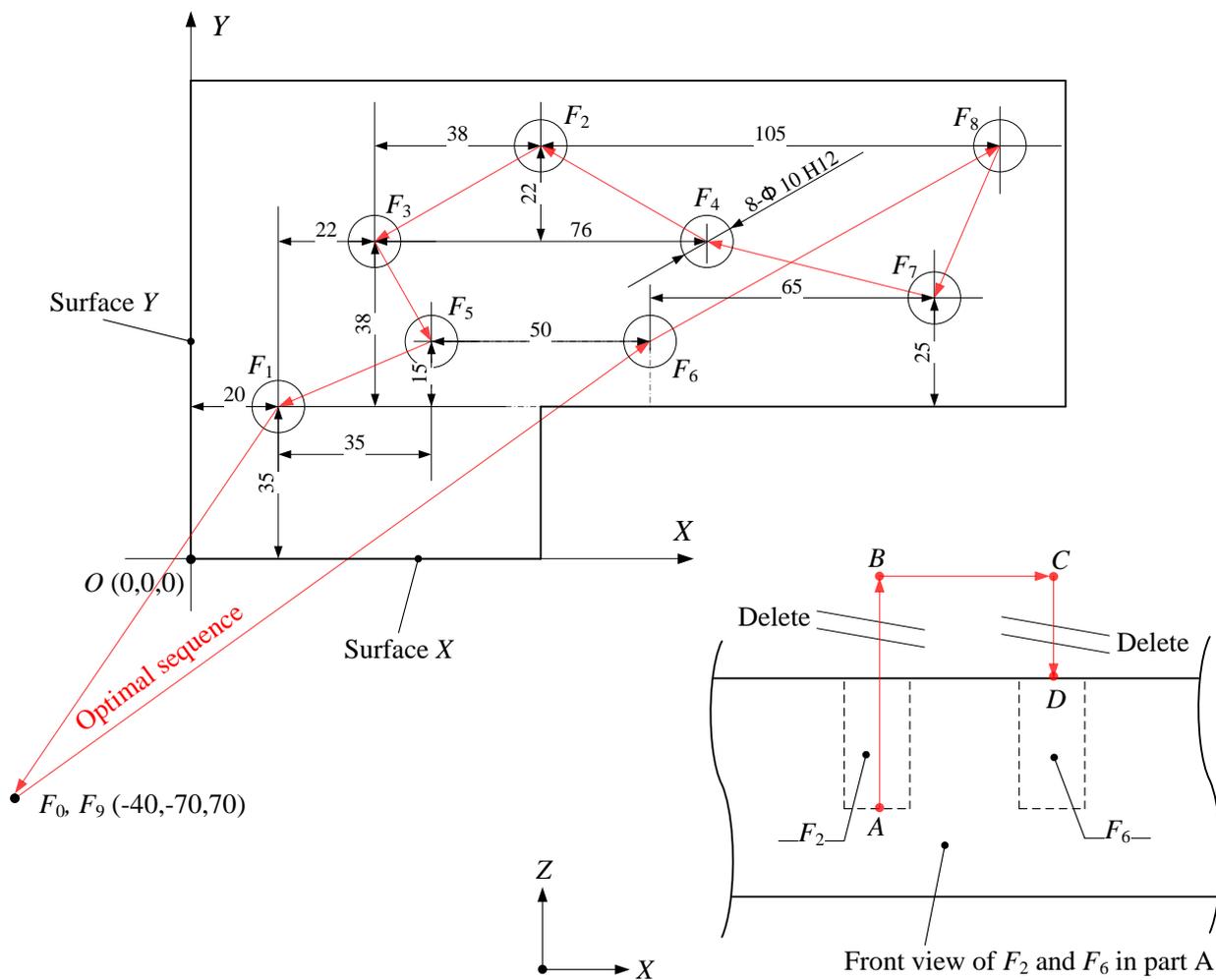
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Fig. 4. Flowchart of NSGA-II.

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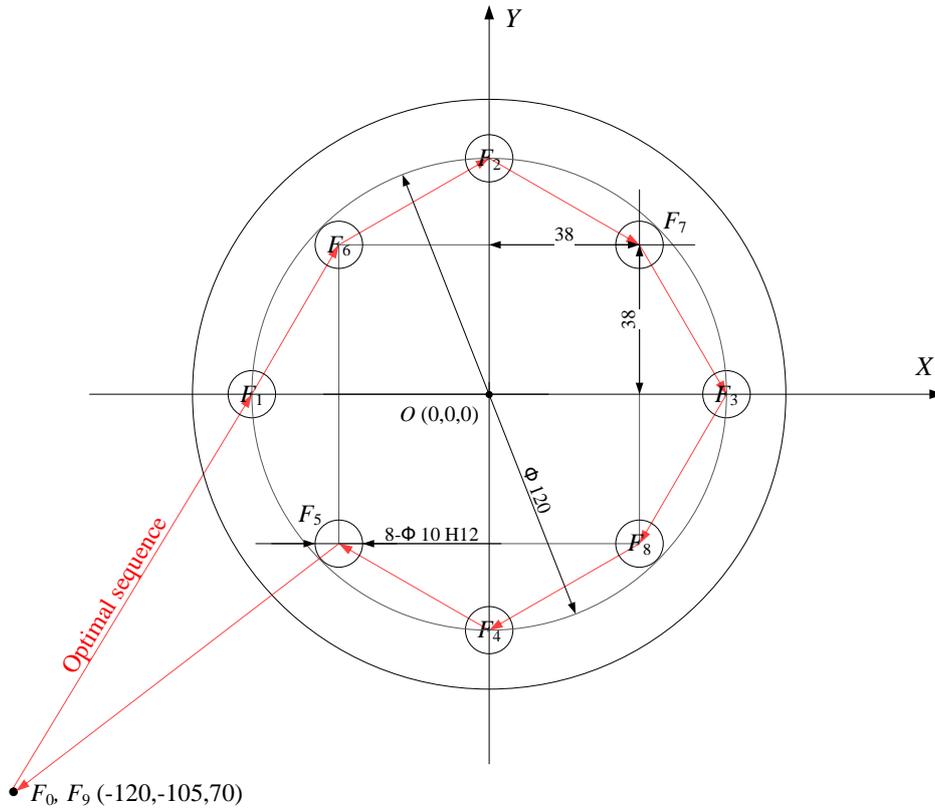
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Fig. 5. Part A with 8 actual features and 2 virtual features.

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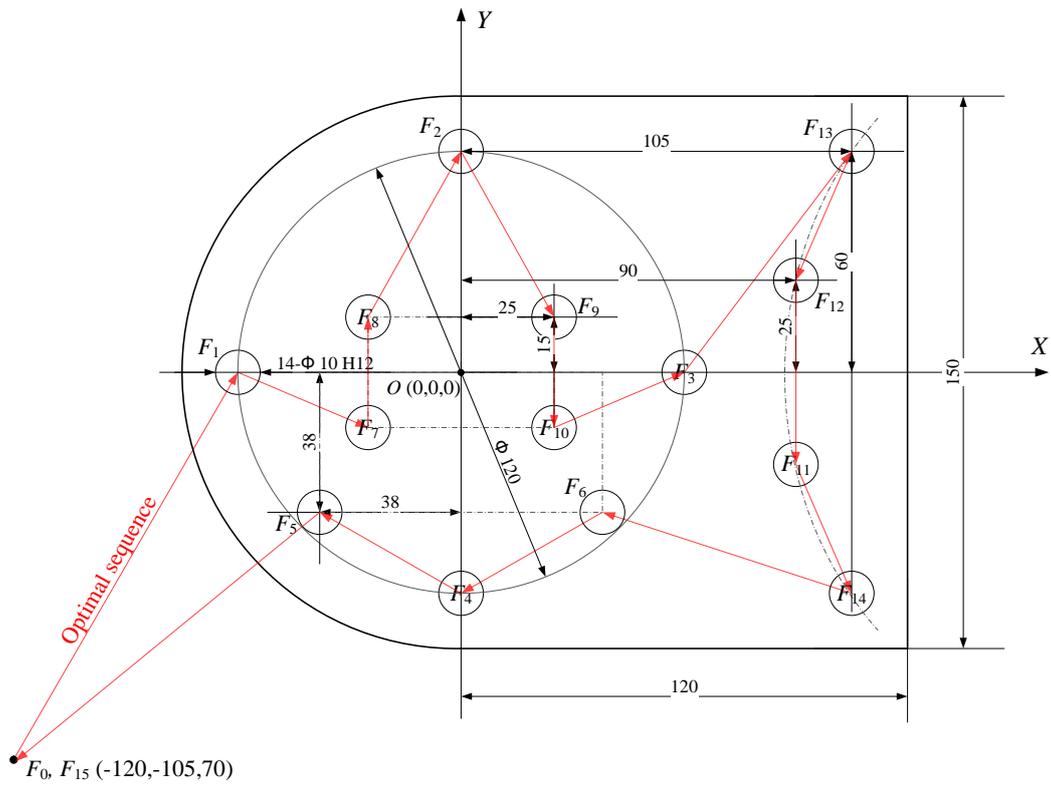
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Fig. 6. Part B with 8 actual features and 2 virtual features.



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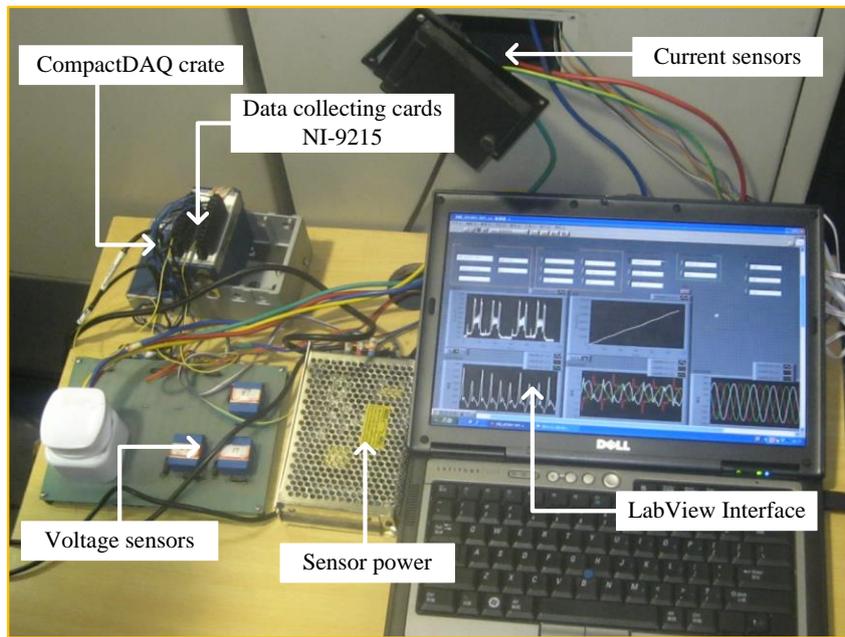
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Fig. 7. Part C with 14 actual features and 2 virtual features.

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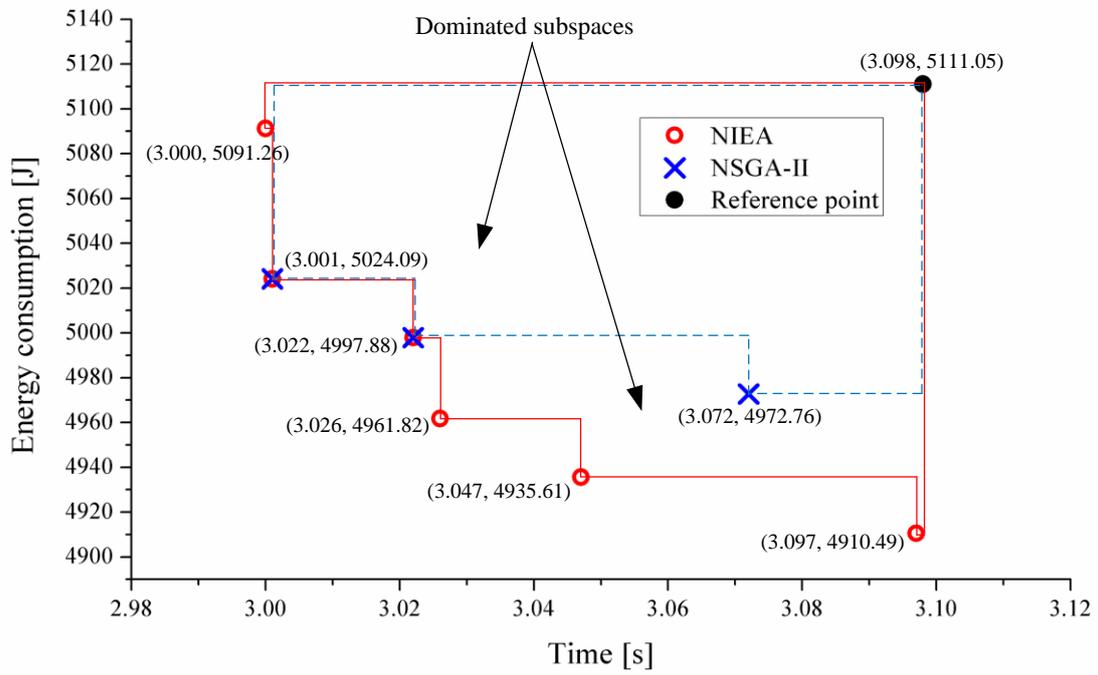
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Fig. 8. Diagram of the experiment setup for power data acquisition.

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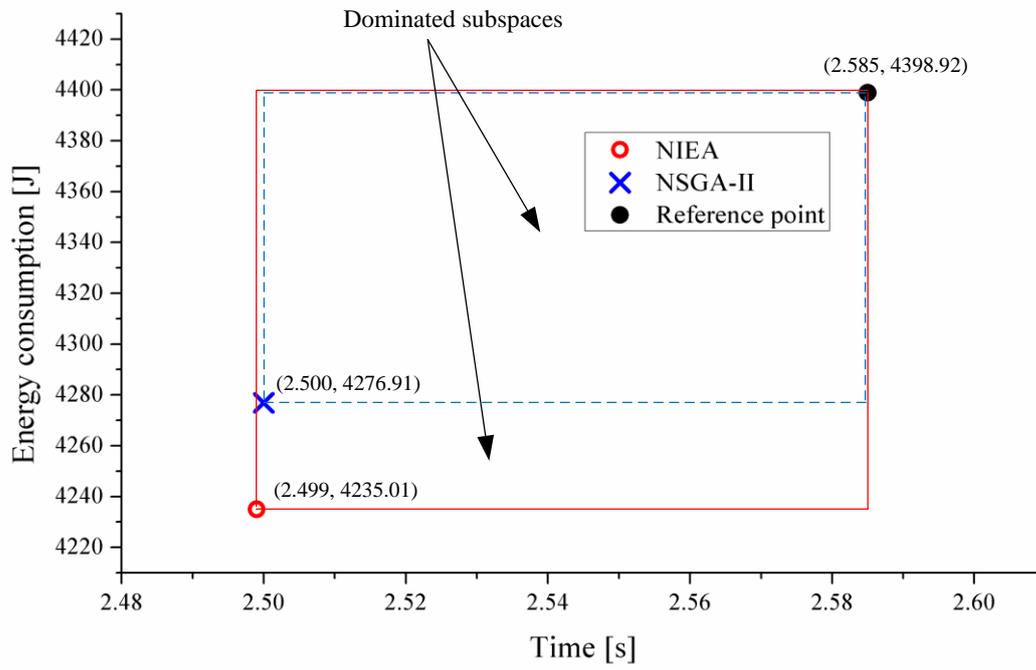
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Fig. 9. Comparison of solution quality between NIEA and NSGA-II for part A.

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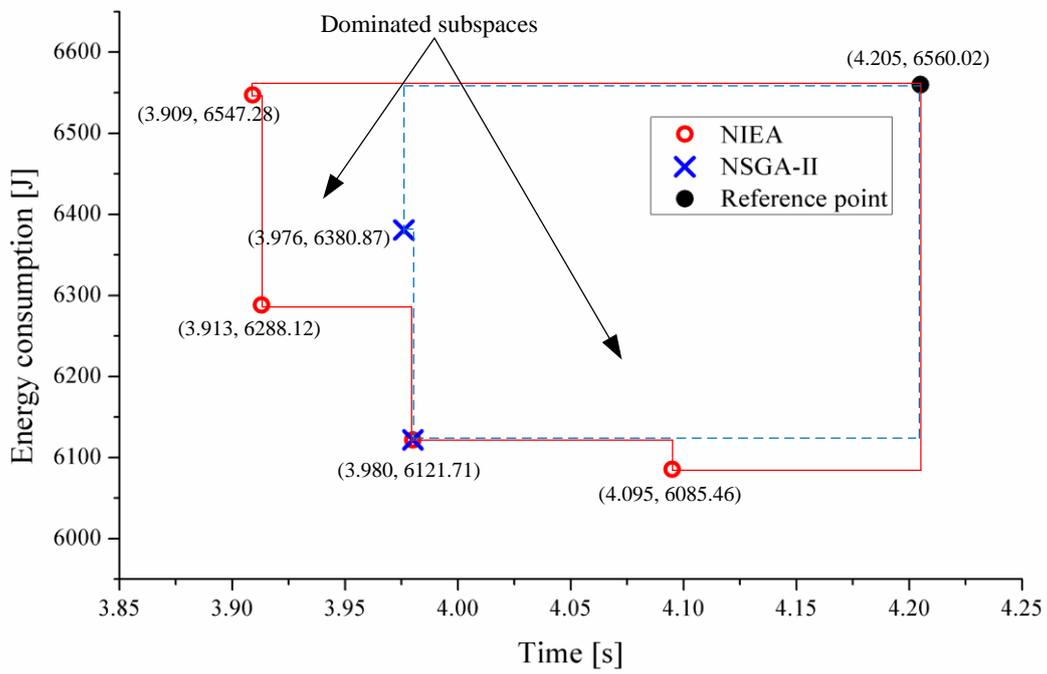


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715 **Fig. 10.** Comparison of solution quality between NIEA and NSGA-II for part B.

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Fig. 11. Comparison of solution quality between NIEA and NSGA-II for part C.

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