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Deposited on: 16 January 2018
Measurement of the inclusive-isolated prompt-photon cross section in $p\bar{p}$ collisions using the full CDF data set


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A measurement of the inclusive production cross section of isolated prompt photons in proton-antiproton collisions at center-of-mass energy \( \sqrt{s} = 1.96 \) TeV is presented. The results are obtained using the full Run II data sample collected with the Collider Detector at the Fermilab Tevatron, which corresponds to an integrated luminosity of 9.5 fb\(^{-1}\). The cross section is measured as a function of photon transverse energy, \( E_T^{\gamma} \), in the range 30 < \( E_T^{\gamma} \) < 500 GeV and in the pseudorapidity region \( |\eta| < 1.0 \). The results are compared with predictions from parton-shower Monte Carlo models at leading order in quantum chromodynamics (QCD) and from next-to-leading order perturbative QCD calculations. The latter show good agreement with the measured cross section.

PACS numbers: 12.38.Qk, 13.85.Qk

I. INTRODUCTION

The measurement of the cross section for the production of inclusive prompt photon (\( \gamma \)) in proton-antiproton (pp) collisions is an important test for perturbative quantum chromodynamics (pQCD), probing the parton distribution functions (PDFs), and the parton-to-photon fragmentation functions (FFs) \([1,3]\). In addition, prompt-photon production is a major background for many other standard model (SM) processes such as Higgs-boson decays into photon pairs (\( H \rightarrow \gamma\gamma \)) and in searches for non-SM physics with final states containing photons \([4,8]\).

The term “prompt” identifies photons that are produced directly in the hard interaction and do not arise from hadron decays. In pp collisions, events with prompt photons with transverse energy \( E_T^{\gamma} \) smaller than approximately 100 GeV are produced predominantly via quark-gluon Compton scattering \( qq \rightarrow q\gamma \), while at higher energies the quark-antiquark annihilation process \( qq \rightarrow g\gamma \) plays a dominant role. In addition, prompt photons are produced through the collinear fragmentation of a final-state parton into a photon, e.g., \( qq \rightarrow q\gamma X \), where X can be any set of final state particles.

The first measurement of the prompt-photon production cross section in hadron collisions came from the CERN Intersecting Storage Rings pp collider, followed by measurements at the SppS collider \([8,11]\). More recent prompt-photon measurements have been performed at the Fermilab Tevatron Collider by the CDF and D0 Collaborations using pp collisions collected at a center-of-mass energy \( \sqrt{s} = 1.8 \) TeV and 1.96 TeV \([12,14]\) and at the CERN Large Hadron Collider by the ATLAS and CMS Collaborations using pp collisions at \( \sqrt{s} = 7 \) TeV \([15,19]\), 8 TeV \([20]\), and 13 TeV \([21]\).

This article presents a measurement of the inclusive cross section for isolated prompt photons over the range 30 < \( E_T^{\gamma} \) < 500 GeV, based on the full data set collected by the Collider Detector (CDF) during Run II (2001–2011) of the Fermilab Tevatron collider and corresponding to an integrated luminosity of 9.5 fb\(^{-1}\) \([22]\).
II. THE CDF II DETECTOR

The CDF II detector [23] is a general-purpose spectrometer at the Fermilab Tevatron collider. It has a cylindrical geometry with approximate forward-backward and azimuthal symmetry. It includes a charged-particle tracking system consisting of silicon microstrip detectors and a cylindrical open-cell drift chamber, designed to measure charged-particle trajectories (tracks) and momenta. The tracking system is contained within a 1.4 T axial magnetic field. It is surrounded by electromagnetic (EM) and hadronic calorimeters segmented in projective towers and used to identify and measure the energy and position of photons, electrons, hadrons, and clusters of particles (jets). The central calorimeters cover the region $|\eta| < 1.1$, and have electromagnetic transverse-energy resolution of $\sigma(E_T)/E_T = 13.5\%/\sqrt{E_T}$(GeV) $\oplus$ 1.5% and a tower segmentation of $\Delta\eta \times \Delta\phi \approx 0.1 \times 15^\circ$ in pseudorapidity-angular space [2]. At a depth corresponding approximately to the maximum energy density in the development of a typical EM shower, the EM calorimeters contain detectors that measure the transverse shower profile. The electromagnetic compartments of the calorimeter are equipped with a timing system measuring the arrival time of particles that deposit energy in each tower [24]. Drift chambers and scintillation counters located outside the calorimeters identify muons.

III. DATA AND SIMULATED SAMPLES

A. Event selection

Photons are reconstructed using clusters of (up to three) adjacent towers above threshold in the central EM calorimeter [25]. The pseudorapidity is restricted to the fiducial region $|\eta| < 1.0$. The data are collected using a three-level online event-filtering system (trigger) [26] that selects events with at least one EM cluster consistent with a photon in the final state. Since there can be multiple collisions in the same bunch crossing, the event primary vertex ($pp$ interaction point) is chosen to be the one that results in the best balance of the $p_T$ of the photon; the $z$ position of the reconstructed primary vertex is required to be within 60 cm of the center of the detector. The photon transverse energy is corrected to account for nonuniformities in the calorimeter response, and calibrated using electrons from reconstructed $Z$-boson decays [27]. Photon candidates are required to satisfy $E_T > 30$ GeV and to meet requirements on calorimeter isolation [28], on track isolation [28], and on the ratio of the energy deposited in the hadronic calorimeter to the energy in the EM cluster [25]. If more than one prompt photon candidate is reconstructed ($\approx 1\%$ of the photon events), that with the highest $E_T$ (leading photon) is chosen.

Events with electrons from $Z$- and $W$-boson decays, which can be misidentified as photons, are removed from the sample by requiring 0 tracks, or at the most one soft track (track isolation $\leq 5$ GeV), pointing to the EM cluster. This track is allowed to account for underlying event and pile-up energy around the cluster. The number of electrons coming from $W$-boson decays is further reduced by requiring the missing transverse energy [7] of the event to be less than 80% of the transverse energy of the photon candidate. This requirement also reduces backgrounds arising from other sources that lead to energy imbalance, such as muons from cosmic rays that may emit bremsstrahlung radiation in the calorimeter, and muons from beam-halo interactions with the beam pipe, which may in turn interact with the detector material producing photons.

After applying all the selection criteria, $2.1 \times 10^6$ events remain in the $\gamma + X$ data sample. The dominant remaining backgrounds are due to jets misidentified as photons.

B. Simulated events

Simulated events from the PYTHIA Monte-Carlo (MC) generator [29] are used in the background estimation, and to evaluate the product of the detector acceptance ($A$) and the efficiency ($\epsilon$) for signal events. Monte Carlo samples are generated with PYTHIA 6.216, a parton-shower generator at leading-order (LO) in the strong-interaction coupling, with the CTEQ5L PDFs [29]. The PYTHIA predictions include $2 \to 2$ matrix-element subprocesses. Higher-order QCD corrections are included by initial- and final-state parton showers.

For the study of systematic uncertainties and for comparisons with the final results, events are also generated with the SHERPA 4.1.4 MC generator [30] with CT10 PDFs [31]. The SHERPA predictions include all the tree-level matrix-element amplitudes with one photon and up to three partons. This calculation features a parton-jet matching procedure to avoid an overlap between the phase-space descriptions given by the fixed-order matrix-element subprocesses and the showering and hadronization in the multijet simulation.

The TUNE A [32,33] underlying event [31] model is used in the PYTHIA calculation. Monte Carlo events are passed through a GEANT-based simulation of the detector [34] and subjected to the same reconstruction and selection requirements as the data.

IV. SIGNAL FRACTION

After the event selection, the remaining background comes from the decays of hadrons (such as $\pi^0 \to \gamma\gamma$); they cannot be rejected on an event-by-event basis, so a statistical background-subtraction technique is used to measure the signal cross section. To evaluate the sig-
nal fraction, an artificial neural network (ANN) is defined using as input the shower-shape, transverse profile, and isolation variables [35]. The inclusive-photon simulation is matched to data by applying the same corrections as derived in Refs. [13, 37]. Further, MC events are reweighted to the observed instantaneous luminosity profile to account for luminosity-dependent effects. The expected ANN output distributions (“templates”) for signal and background samples are constructed using PYTHIA inclusive-photon and dijet MC predictions, respectively. These templates are validated using the $Z \rightarrow e^+e^-$ and dijet data samples [37]. To estimate the prompt-photon rate, the ANN output distribution observed in data is fit to a linear combination of signal and background ANN templates, using a binned maximum-likelihood method that accounts for uncertainties on both data and templates [38]. A fit is performed in each $E_T^\gamma$ bin, yielding prompt-photon fractions in the $E_T^\gamma$ range from 30 GeV up to 500 GeV, as shown in Fig. 1 for an example $E_T^\gamma$ bin. Figure 2 shows the resulting signal frac-

![Image](https://via.placeholder.com/150)

**FIG. 1.** Observed ANN output distribution (points), the templates for signal and background processes, and the resulting fit of the templates to the data distribution, for events restricted to the photon transverse energy bin 110–130 GeV. The left-hatched histogram (blue in color) represents the background and the right-hatched histogram (red in color) represents the signal, normalized so that the scale of the sum of the templates equals the total number of data events.

tion (photon purity) as a function of $E_T^\gamma$.

The systematic uncertainty on the signal fraction is estimated by varying the fit configurations and the values of the ANN input variables within their uncertainties. The dominant uncertainty on the shape of the ANN templates originates from the modeling of calorimeter isolation energy. The overall systematic uncertainty on the signal fraction is estimated to be 8% at low $E_T^\gamma$, 6% at high $E_T^\gamma$, and 3% on average for the intermediate $E_T^\gamma$ range 40 < $E_T^\gamma$ < 300 GeV.

![Image](https://via.placeholder.com/150)

**FIG. 2.** Signal fraction as a function of leading-photon $E_T^\gamma$. The points are plotted at the average $E_T^\gamma$, of the data within each bin. The error bars represent the statistical uncertainty, while bands represent the total systematic uncertainty.

V. CROSS SECTION MEASUREMENT

The differential cross section for the production of isolated prompt photons in a given phase-space bin is calculated as $d^2\sigma/(dE_T^\gamma d\eta^\gamma) = (N f^\gamma)/((\Delta E_T^\gamma \Delta \eta^\gamma \mathcal{L}) A \times \epsilon)$, where $N$ is the number of data events in a given $E_T^\gamma$ bin after applying the full selection, $f^\gamma$ is the signal fraction, $\Delta E_T^\gamma$ is the width of the $E_T^\gamma$ bin, $\mathcal{L}$ is the integrated luminosity, and $A \times \epsilon$ is a correction factor. Since the cross section is measured for $|\eta^\gamma| < 1.0$, $\Delta \eta^\gamma$ is set to 2.0. The factor $A \times \epsilon$ combines corrections for acceptance, resolution effects and efficiencies for selecting and reconstructing the photon to infer the results at the particle level (i.e., generator level). The correction is computed from the bin-by-bin fraction of simulated particle-level prompt photons in the reconstructed signal events, as determined by the PYTHIA MC calculation. The numerator is obtained by applying the same requirements to the PYTHIA-simulated events as those applied to data. The denominator is obtained by selecting generated particles [39] in the fiducial region, with $E_T^\gamma > 30$ GeV and the same energy isolation requirement as in the data. The photon efficiency is calibrated by comparing the selection efficiencies for $Z \rightarrow e^+e^-$ events in data and in simulation [37].

The largest sources of systematic uncertainty arise from the photon energy scale at high $E_T^\gamma$ (≈ 6%) and from the $A \times \epsilon$ factor (≈ 8%). The latter is determined by a comparison of results from the PYTHIA and SHERPA MC calculations.

VI. THEORETICAL PREDICTIONS

The predicted prompt-photon production cross section is calculated using the fixed-order next-to-leading-order (NLO) program MC$\text{F}$M 6.8 including nonperturba-
tive fragmentation at LO [10]. The calculation uses the MRST2008 NLO PDFs and the GdRG LO FFs [41]. The 
MCFM prediction is a parton-level calculation that does not include a model for the underlying event energy. This prediction is corrected for the nonperturbative effects of parton-to-hadron fragmentation and underlying event energy. A correction factor $C_{UE}$ is defined as the overall ratio of the cross section obtained using the PYTHIA MC generator, with and without modeling of both multiple-parton interactions and hadronization [13].

The nominal renormalization ($\mu_R$), factorization ($\mu_F$), and fragmentation ($\mu_F$) scales are set to the photon transverse energy ($\mu_R = \mu_F = \mu_F = E_T^\gamma$). The scale uncertainty is evaluated by varying the three scales simultaneously between the extreme values $E_T^\gamma/2$ and $2E_T^\gamma$.

In addition to comparison with the perturbative-QCD prediction above, we also compare the measured cross section to predictions from the PYTHIA and SHERPA MC generators. Both are calculated at the particle level, meaning that the photon isolation energy is estimated using generated hadrons and the selection criteria are applied to the hadron jets and are directly comparable to our measurement.

VII. RESULTS

The differential cross section results for the production of isolated prompt photons are listed in Table I, together with statistical and systematic uncertainties. The additional 6% luminosity uncertainty is not included in the table.

<table>
<thead>
<tr>
<th>$E_T^\gamma$ (GeV)</th>
<th>$\langle E_T^\gamma \rangle$ (GeV)</th>
<th>$d^2\sigma/(dE_T^\gamma d\eta^\gamma)$ (pb/(GeV))</th>
<th>$\delta\sigma_{syst}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>30–40</td>
<td>34.1</td>
<td>$(5.49 \pm 0.41) \times 10^{-1}$</td>
<td>23.3</td>
</tr>
<tr>
<td>40–50</td>
<td>44.3</td>
<td>$(1.72 \pm 0.23) \times 10^{1}$</td>
<td>17.2</td>
</tr>
<tr>
<td>50–60</td>
<td>54.3</td>
<td>$(6.72 \pm 0.11) \times 10^{1}$</td>
<td>14.9</td>
</tr>
<tr>
<td>60–70</td>
<td>64.4</td>
<td>$(2.95 \pm 0.04) \times 10^{1}$</td>
<td>14.6</td>
</tr>
<tr>
<td>70–80</td>
<td>74.5</td>
<td>$(1.45 \pm 0.02) \times 10^{1}$</td>
<td>13.7</td>
</tr>
<tr>
<td>80–90</td>
<td>86.5</td>
<td>$(6.87 \pm 0.10) \times 10^{1}$</td>
<td>13.2</td>
</tr>
<tr>
<td>90–110</td>
<td>101.7</td>
<td>$(3.03 \pm 0.05) \times 10^{1}$</td>
<td>12.8</td>
</tr>
<tr>
<td>110–130</td>
<td>118.7</td>
<td>$(1.32 \pm 0.03) \times 10^{1}$</td>
<td>12.7</td>
</tr>
<tr>
<td>130–150</td>
<td>138.8</td>
<td>$(5.65 \pm 0.15) \times 10^{2}$</td>
<td>13.1</td>
</tr>
<tr>
<td>150–175</td>
<td>160.9</td>
<td>$(2.37 \pm 0.08) \times 10^{2}$</td>
<td>12.6</td>
</tr>
<tr>
<td>175–200</td>
<td>185.9</td>
<td>$(1.03 \pm 0.03) \times 10^{2}$</td>
<td>12.4</td>
</tr>
<tr>
<td>200–240</td>
<td>216.8</td>
<td>$(4.01 \pm 0.12) \times 10^{-3}$</td>
<td>13.2</td>
</tr>
<tr>
<td>240–290</td>
<td>259.2</td>
<td>$(1.16 \pm 0.05) \times 10^{-3}$</td>
<td>14.1</td>
</tr>
<tr>
<td>290–350</td>
<td>309.4</td>
<td>$(3.08 \pm 0.23) \times 10^{-4}$</td>
<td>15.1</td>
</tr>
<tr>
<td>350–500</td>
<td>387.6</td>
<td>$(1.83 \pm 0.29) \times 10^{-5}$</td>
<td>16.1</td>
</tr>
</tbody>
</table>

These results are compared with the theoretical predictions in Fig. 3. The ratio of the measured cross section over the predicted ones is shown in Fig. 3. The full error bars on the data points represent statistical and systematic uncertainties summed in quadrature. There are two error bars that show statistical uncertainties only. The NLO predictions are shown with their theoretical uncertainties arising from the choice of factorization, renormalization, and fragmentation scales.

The NLO calculations agree with the data up to the highest $E_T^\gamma$ values considered. Observed cross sections are moderately larger than the central values for the NLO calculation for low $E_T^\gamma$, but agree within the theoretical uncertainty of the NLO calculation. The PYTHIA and SHERPA predictions are also shown in Figs. 3 and 4. The shape of the measured cross section distribution is well described by both models. The PYTHIA prediction underestimates the observed cross section by more than a factor of 1.5 across the whole $E_T^\gamma$ range. This is possibly due to the lack of higher-order terms in the PYTHIA photon+jet matrix-elements. The SHERPA calculation is approximately 1.1 to 1.2 times larger than the observed cross section, nearly uniformly

![FIG. 3. Measured $\gamma + X$ cross section as a function of leading photon transverse energy. Data (markers) are centered at the average $E_T^\gamma$ of each bin for illustration of the steeply falling spectral shape. Data are compared with the PYTHIA, SHERPA and MCFM predictions (dashed lines). The vertical error bars show statistical uncertainties, while the shaded areas show the systematic uncertainties. The 6% luminosity uncertainty on the data is not included. A correction $C_{UE}$ to account for parton-to-hadron fragmentation and underlying event effects is applied to the MCFM theoretical predictions, as explained in the text.](image-url)
sive rates of photon production through fragmentation. MISTUNED FRAGMENTATION subprocesses leading to excesses related to nonperturbative QCD processes, such as plain the discrepancy with data. Other possible reasons elements of the subprocesses, which could possibly ex-

ton, but it is missing virtual corrections in the matrix across the $E_T^\gamma$ range. This calculation includes up to three jet emissions associated with the observed photon, but it is missing virtual corrections in the matrix elements of the subprocesses, which could possibly explain the discrepancy with data. Other possible reasons are related to nonperturbative QCD processes, such as mistuned fragmentation subprocesses leading to excessive rates of photon production through fragmentation.

**VIII. CONCLUSIONS**

A measurement of the differential cross section for the inclusive production of isolated prompt photons in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV is presented using the full data set collected with the CDF II detector at the Tevatron. The cross section is measured as a function of photon transverse energy $E_T^\gamma$ in the central pseudorapidity region $|\eta^\gamma| < 1.0$. The measurement spans the $E_T^\gamma$ kinematic range from 30 GeV to 500 GeV, thus extending the reach by 100 GeV from the previous CDF measurement [13]. Comparisons of our measurement to three theoretical predictions are discussed. Both PYTHIA and SHERPA predictions correctly describe the shape of the differential cross section. The PYTHIA generator predicts a smaller cross section compared to the data and the SHERPA prediction. The data are in good agreement with the fixed-order NLO MCFM calculation.

**ACKNOWLEDGEMENTS**

We thank the Fermilab staff and the technical staffs of the participating institutions for their vital contributions. This work was supported by the U.S. Department of Energy and National Science Foundation; the Italian Istituto Nazionale di Fisica Nucleare; the Ministry of Education, Culture, Sports, Science and Technology of Japan; the Natural Sciences and Engineering Research Council of Canada; the National Science Council of the Republic of China; the Swiss National Science Foundation; the A.P. Sloan Foundation; the Bundesministerium für Bildung und Forschung, Germany; the Korean World Class University Program, the National Research Foundation of Korea; the Science and Technology Facilities Council and the Royal Society, United Kingdom; the Russian Foundation for Basic Research; the Ministerio de Ciencia e Innovación, and Programa Consolider- Ingenio 2010, Spain; the Slovak R&D Agency; the Academy of Finland; the Australian Research Council (ARC); and the EU community Marie Curie Fellowship Contract No. 302103.

[7] A cylindrical coordinate system $(r, \phi, z)$ is used with origin at the geometric center of the detector; $r$ is the radius from the nominal beam line, $\phi$ is the azimuthal angle, and the $+z$ axis points along the incident proton beam direction. The polar angle $\theta$ with respect to the proton beam is used to define the pseudorapidity $\eta = -\ln(\tan(\theta/2))$. Transverse energy and transverse momentum are defined as $E_T = E \sin(\eta)$ and $p_T = E \cos(\eta)$, respectively. The missing transverse energy is given by $E_T^m = \sum_i E_T^i \hat{n}_i$ where $i$ is the calorimeter tower number and $\hat{n}_i$ is a unit vector perpendicular to the beam axis and pointing at the ith calorimeter tower.
The calorimeter isolation is defined as the transverse energy deposits in the EM calorimeter in the isolation cone minus the transverse energy in the EM cluster of the photon. The isolation cone is defined to have a radius $R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} = 0.4$. The track isolation is defined as the scalar sum of the transverse momenta of all tracks originating from the primary vertex of the event and lying within a cone of radius $R = 0.4$.

The underlying event is that part of the event final state that cannot be directly associated with the primary hard $2 \rightarrow 2$ parton-parton scattering and consists of the beam remnants plus possible contributions from initial- and final-state gluon radiation and additional parton-parton interactions.