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THE MYTHS AND REALITIES OF BAYESIAN CHRONOLOGICAL MODELING REVEALED

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ABSTRACT

We review the history of Bayesian chronological modeling in archaeology and demonstrate that there has been a surge over the past several years in American archaeological applications. Most of these applications have been performed by archaeologists that are self-taught in this method because formal training opportunities in Bayesian chronological modeling are infrequently provided. We define and address misconceptions about Bayesian chronological modeling that we have encountered in conversations with colleagues and in anonymous reviews, some of which has been expressed in the published literature. Objectivity and scientific rigor is inherent in the Bayesian chronological modeling process. Each stage of this process is described in detail and we present examples of this process in practice. Our concluding discussion focuses on the potential Bayesian chronological modeling has for enhancing understandings of important topics.

SPANISH ABSTRACT

En este artículo se revisará la historia de la modelización cronológica Bayesiana en arqueología y se mostrará cómo la arqueología americana ha experimentado en los últimos años un auge en su aplicación. La mayor parte de los análisis han sido desarrollados por arqueólogos que han sido autodidactas en el aprendizaje del método, ya que las oportunidades de formación en el análisis Bayesiano son muy limitadas. Se explicarán cuáles son los errores más comunes en la aplicación de la modelización cronológica Bayesiana con los que nos hemos encontrado al conversar con compañeros, así como en revisiones anónimas, algunas de los cuales ya han sido señaladas en otros trabajos. La objetividad y el rigor científico resultan inherentes al proceso de modelización cronológica Bayesiana. Se describirá en detalle cada etapa de este proceso, presentando ejemplos de su puesta en práctica. Nuestra conclusión se centrará en torno al potencial de este método para mejorar nuestra comprensión sobre temas de gran relevancia.

The past five years have witnessed an explosion in archaeological publications employing Bayesian chronological modeling from all corners of the world (Bayliss 2015), a practice that has been in place in the U.K. (especially in England through the work of Alex Bayliss and others at English Heritage/Historic England) for over 20 years. The body of well-sampled and well-dated sites subjected to Bayesian modeling in the U.K. is quite large, allowing for the first time generational narratives for many periods of British prehistory (Bayliss 2015; Hamilton et al. 2015). Much of this work has been undertaken in collaboration with a small group of archaeological specialists experienced in constructing robust chronologies (Bayliss 2015). In many cases, they have produced chronologies of a higher accuracy, transparency, and reproducibility than those created through informal interpretation. The adaptation of Bayesian frameworks has also allowed for the estimation of detailed settlement histories and precise evaluations of the timing and tempo of social change.

The adoption of Bayesian chronological modeling outside Britain has occurred more slowly, but the method is now used regularly in many areas throughout Europe, Asia, and other parts of the world (Bayliss 2015; Buck and Meson 2015). The impact this work is beginning to have on European prehistory has been profound, and has been referred to by some as a radiocarbon revolution (Bayliss 2009). Bayliss (2015) presents a survey of this literature and demonstrates that the clear majority of these applications are for site chronologies, but the method is also used to create environmental (Blaauw and Christen 2011; Bronk Ramsey 2008; Dye 2011), historical (Levy et al. 2010; Tipping et al. 2014), seriation (Denaire et al. 2017; Whittle et al. 2016), and typological sequences (Conneller et al. 2016; Garrow et al. 2009; Krus 2016).

The shift to chronological interpretation via Bayesian modeling has happened in large part because of the development of freely-available computer programs, which provide user-friendly statistical modeling tools (Buck and Meson 2015). The most widely used Bayesian chronological modeling software programs are BCal (Buck et al. 1999) and OxCal (Bronk Ramsey 1998, 2001, 2008, 2009a), and while the clear majority of applications are being done in OxCal (Bayliss 2015) new computer programs do appear (Jones and Nicholls 2002; Lanos et al. 2016). Additionally, more specialized Bayesian chronological modeling software exists, primarily for age-depth modeling of paleoenvironmental sequences (Blaauw and Christen 2011; Haslett and Parnell 2008). The popularity of OxCal is due in large part to its capability for use in a wide range of applications.

The rapid growth in the implementation of Bayesian models within archaeology outside of the U.K., combined with the dearth of practical learning materials, has led to confusion about the Bayesian process, the propagation of common myths, and in some cases outright skepticism. This story is not altogether unfamiliar from a European perspective, even more so when examined from the perspective of bringing Bayesian modeling from England into standard archaeological practice in Scotland (which we have witnessed first hand).

We believe that it is both necessary and timely to provide a commentary on the state of Bayesian modeling in American archaeology to steer the discipline towards best-practice approaches. Especially because we have come across skepticisms and misconceptions in conversations with colleagues and in anonymous reviews, and some of this has been expressed in the published literature. Many of these beliefs deal with what is required to properly create a meaningful

Bayesian chronological model, while others with how to evaluate Bayesian chronological models. Here we take to task six of these misconceptions.

We further provide a brief overview of the history of the use of the methodology in American archaeology. We describe in detail the Bayesian process, which is critical for understanding this methodology. We provide examples of the use of Bayesian chronological modeling in practice and a commentary on how Bayesian chronological modeling could be used in the future of American archaeology. Our goal in doing this is to bring a greater awareness of the key issues so that the practice can reach levels of quality comparable to that found in the UK and Europe.

THE STATE OF AFFAIRS IN THE AMERICAS

The first studies using Bayesian chronological modeling in the Americas were published in the 1990s, only several years after the first published applications in Europe (Bayliss 2015). The exposition of the Bayesian method by Christen (1994) might be considered to contain the earliest published Bayesian chronological model for a site in the Americas – the Chancay culture of Peru, but it is the chronological modelling of Zeidler et al. (1998), with its discussion of contextual and taphonomic security and sensitivity analyses, that is more akin to the practice of chronological modeling that we outline in this essay. While, American applications of Bayesian chronological modeling continued to be published only intermittently throughout the 2000s, during this time Bayesian chronological modeling in the Americas appears to have been only used by a handful of American archaeologists. From 2010–2015 there was an enormous increase in the number of studies in American archaeology presenting applications, demonstrating that

Bayesian chronological modeling in the Americas is on the verge of reaching critical mass (Figure 1).

The rapid growth of Bayesian chronological modeling in American archaeology over the past several years and lack for formal training opportunities has led to plug-and-play applications, seemingly by archaeologists lacking clear understanding of the Bayesian process (this problem is described further in Buck and Meson [2015] and Cowgill [2015a:10]). Likewise, there are problems with quality control of published studies due to a scarcity of qualified reviewers.

While there might not necessarily be a vocal demand for formal training opportunities, the need is clearly there. Whether they use Bayesian modeling or not, it is possible that over the next decade almost all archaeologists will see regional and site chronologies transformed from Bayesian modeling, and it is probably better they be critically informed sooner rather than later. Some formal training opportunities we are familiar within the Americas include a free online booklet about the basics of using OxCal (McNutt 2013), training courses that we have offered at various conferences, and a training course run at the University of Arizona in 2015. Other resources often used for training are the OxCal Google Group (<https://groups.google.com/forum/#!forum/oxcal>) and the OxCal online manual (http://c14.arch.ox.ac.uk/oxcalhelp/hlp_contents.html).

These training opportunities provide good introductions, but in many ways, they barely scratch the surface. Becoming fully proficient in Bayesian chronological modeling takes a combination of training and experience, requiring both a critical understanding of archaeology, methods used

in scientific dating, and statistics. For many American archaeologists training in how to use OxCal has come from self-learning, mainly from studying the published literature or through discussions with other American archaeologists that have some modeling experience. This has resulted in myths and misconceptions in the American literature about Bayesian chronological modeling which are fully described in the following section.

MYTHS & MISCONCEPTIONS

Misconception 1: Bayesian statistics is overly complicated hocus-pocus that is not scientifically objective

This belief is articulated by Stephen Lekson (2015:166, 190–191) in several tongue-in-cheek comments in the second edition of his book *The Chaco Meridian*. For example, Lekson (2015:191) states:

Of course, there's a reason statisticians banned Bayes for a couple of centuries- and why Bayes' heresies have been revived almost exclusively by the looser, weaker sciences (i.e., the social sciences). Bayes cheats: picking and choosing dates, modes, and so forth that fit one's preconceptions (or the statistical preconceptions built into OxCal).

Contrary to Lekson's (2015) claim, Bayesian statistics are widely used in the physical/natural sciences (see Supplemental file 2 for an extensive but non-exhaustive list of relevant references). There is a degree of subjectivity in the Bayesian process. This is contained within our prior beliefs that combine to form the structure of the model. These beliefs are our interpretation of the

archaeology and the inferences we make to relate the date of the death of a sample to the date of the formation of the deposit from which it was recovered. A ‘good Bayesian’ does not pick and choose dates to fit one’s preconception, but rather rigorously defends their interpretation of the archaeology in a transparent manner in order to provide weight to the resulting date estimates. The central issue in this myth is the scientific objectivity of the process, which allows us to delve into the underlying mathematics, in brief.

While OxCal is a program with complex underlying algorithms, the fundamental mathematics of all Bayesian applications follow Bayes’ rule (following Bayliss 2009; Buck et al. 1991; 1996). Bayes’ rule (also called Bayes’ Law or Bayes’ Theorem, Equation 1) was proposed by the English mathematician and Presbyterian minister Thomas Bayes in the 1700s (Bayes 1763; Kruschke 2014).

Eq. 1 Bayes’ rule

$$posterior = \frac{\text{likelihood} \times \text{prior}}{\text{evidence}} = p(\theta|D) = \frac{p(D|\theta) \times p(\theta)}{p(D)}$$

$$p(D) = \sum_{\theta} p(D|\theta)$$

The equation provides a model for estimating the probability of a belief after the collection of data that can test the belief. The key factors of a model that follows Bayes’ rule are the belief (θ) being tested, the prior, the likelihood, the evidence (D), and the posterior. In Equation 1, $p(\theta)$ and $p(D)$ are probabilities for observing these two events, independently of one another, whereas

$p(D|\theta)$ and $p(\theta|D)$ are conditional probabilities of observing the first event given the second event is true.

It is too early in the paper to lose readers, so a simplified depiction of Bayes' rule is shown in Equation 2, where the relationship of the likelihood and evidence is simply referred to as the “standardized likelihood” (Buck et al. 1991:811).

Eq. 2 Simplified expression of Bayes' rule

$$\text{Posterior beliefs} = \text{Standardized Likelihood} \times \text{Prior beliefs}$$

This is further refined into terms recognizable to archaeologists with the “standardized likelihood” equivalent to our “dates” and our “prior” which equates to date probabilities in a chronological model (Equation 3).

Eq. 3 Simplified expression of how Bayes' rule is used in Bayesian chronological models

$$\text{Posterior beliefs} = \text{The dates (Standardized Likelihood)} \times \text{Archaeological data (Prior beliefs)}$$

Lindley (1985) provides a good overview of Bayesian inference for the non-statistician, while Kruschke (2014) is accessible to the mathematically-minded reader. The Bayesian process is very much like the way that we intuitively learn as humans and change our beliefs to improve our individual understandings. We start with our prior beliefs about how and why things and events happen. Then through our life experience we modify our beliefs to suit what we have

experienced. If our experience confirms our beliefs, then they are supported. If our experience is contrary to our beliefs, then our beliefs may change.

Radiocarbon and other scientific chronological information are used in Bayesian chronological modeling to calculate the standardized likelihood, and are modeled in different ways to reflect the prior strength of our beliefs about the functional relationship of the data (Bayliss 2009). The posterior probabilities estimated by OxCal serve as posterior probabilities for functions specified in the model such as individual radiocarbon calibrations and model boundaries. To do this OxCal (v4 and above) uses a Markov chain Monte Carlo (MCMC) and Metropolis-Hastings algorithm to generate random draws from a target distribution, and produce a range of posterior probabilities (Bronk Ramsey 2009a; Gelfand and Smith 1990; Gilks et al. 1996). Finer details about the algorithms used for this process are described in Bronk Ramsey (1998; 2001; 2009a).

It is critical that users of Bayesian modeling software understand the Bayesian modeling process, the mathematics of the software packages used, and how to avoid ‘black boxing’ the presentation and interpretation of their models. If careless modeling is published due to a lack of a critical evaluation then the results should probably be treated very skeptically. Analytical transparency is key for evaluation but also for expanding upon the modeling in the future. Bayliss (2015) and Buck and Meson (2015) describe in detail what ‘good’ Bayesian modeling studies should include.

Misconception 2: Old radiocarbon measurements with large errors should be ignored

Occasionally we come across the belief that legacy radiocarbon dates with large standard errors are of little interpretative value because of their greater imprecision. For example, Connolly (2000) rejects radiocarbon measurements with errors greater than 100 years in an analysis of dates from Poverty Point. Additionally, it may be questionable if a legacy radiocarbon date is even an accurate measurement, for example, calibrations of dates from Alaska, made by the Dicarb laboratory, have been noted in some cases to be too young (Reuther et al. 2005).

It is easy to understand why someone might want to exclude these measurements, if the aim with the Bayesian model is to improve chronological precision. The ‘traditional’ methods of evaluating radiocarbon dates (e.g. summed probabilities or ‘eye-balling’ calibrations) will be significantly affected by the addition of these results, whereas a Bayesian model can handle these data much more effectively. Despite their issues, legacy dates with large standard errors can be informative data for a Bayesian model (see Bayliss et al. 2011; Jay et al. 2012; Krus et al. 2015). Modeling this data can be difficult, it is sometimes unclear exactly what was dated and what dating methods were followed (a problem often associated with legacy dates with smaller errors as well!). Finding this information can involve much research, including contacting the original submitters and laboratories, but this is necessary to fully evaluate the accuracy of the data and to decide how to include them in a Bayesian model. In cases where legacy dates are questionable, they could be crosschecked by re-dating the original samples or contemporaneous material.

Additionally, alternative models, or ‘sensitivity analyses’, should be considered, which is a key element in Bayesian chronological modeling (Bayliss et al. 2011; also see Kruschke 2014), but can often be found lacking in most Bayesian models in archaeology. With a sensitivity analysis

we amend the prior information to determine which of the model components are most critical in estimating the posteriors. Bayliss et al. (2011) praise the strength of this technique and emphasize that it is useful for demonstrating the robusticity of a preferred model.

Misconception 3: Stratigraphic relationships between samples are needed to make a Bayesian chronological model

Following this belief, Bayesian chronological modeling is not possible in circumstances where there is little-to-no stratigraphy between radiocarbon samples. To the contrary, there are numerous published models from radiocarbon data that are not constrained by stratigraphic relationships (see for example Bayliss et al. 2007; Hamilton and Kenney 2015). This is possible because these models use a uniform prior distribution (UPD) that assumes that any event in the model is equally likely to have occurred in any individual year covered by the data (Bronk Ramsey 1998:470). Whereas stratigraphic relationships are an *informative* type of prior information, uniform prior distributions are an *uninformative* belief that structure data as a continuous period of activity (Bayliss and Bronk Ramsey 2004:33; Bronk Ramsey 2009a:354). It is only justifiable to use a UPD if the dated activity is believed to be continuous, whether it be for a short or long time or at a slow or fast tempo.

A couple of recent American studies have approached modeling without stratigraphy by placing dates in a sequence from oldest to youngest (for example see R. Cook et al. 2015; Lekson 2015:190). Unfortunately, this informative prior information is unsubstantiated. Priors that are not reflective of the archaeology should not be used. Even if they help provide more precise

posterior probabilities, the underpinning assumptions are unfounded (Buck and Meson 2015:571).

Misconception 4: The date for a diagnostic prehistoric artifact or expected time range of activity should be included in the model to provide a chronological constraint

Calendar dates can be used in a Bayesian model to constrain the model results by specific years. For example, a site containing an abundance of artifacts of a presumed date, could be modeled to constrain independent dates from the site to this specific period. However, results will then conform to this expectation, such that you build a model to ensure you never learn something new!

Including calendar years within a model can only be justified if they reflect the known time of an historic or geological event strongly related to the archaeology. Otherwise this practice becomes fuzzy, especially where the evidence is diagnostic artifacts not obviously linked to specific calendar years (e.g. pottery vs coins). If applied loosely, this practice will result in a tautological loop, where the scientific dates are provided to produce independent estimates but are modeled to fit the preconceived beliefs about the timing of the associated artifacts. Further, there are taphonomic considerations and the final (re-)deposition of diagnostic artifacts may be greatly removed from the timing of their creation, such that their incorporation into a model often only provides a *terminus post quem (TPQ)* – or ‘limit after which’ – for the formation of the deposit from which they were recovered. If calendar years are used to constrain the model, then a

sensitivity analyses should be used to show how the results change when calendar year constraints are removed.

Misconception 5: The agreement indices in OxCal are a useful tool for determining which competing model is more probable

We occasionally see papers and presentations where Agreement indices are misinterpreted as values indicating a most probable model (for example see Riede and Edinborough 2012).

OxCal's Agreement indices are *like* Bayes factors, which is a type of calculation used to directly compare the probability of Bayesian models (Gilks et al. 1996; Kruschke 2014). Importantly, OxCal's Agreement indices *are not* actual Bayes factors, but rather pseudo Bayes factors, and should only be used to determine if a model is consistent or inconsistent (Bronk Ramsey 1995:427–428, 2001:355). They are numerical values for the agreement between the OxCal model and data. Values less than 60 indicate the chronological data and model are inconsistent while those greater than 60 indicate consistency (Bronk Ramsey 1995:427-428), with the value of 60 similar to the 95% probability in a chi-square test. A_{model} provides a value for the agreement of the entire model and A_{overall} is a function of agreement indices of the individual dates.

Misconception 6: Bayesian modeling is not necessary if you have a widely accepted site/regional chronology

The final misconception is that Bayesian modeling is not necessary for a site or region where a chronology is already established through diagnostic artifacts or perhaps other forms of scientific or historic dating. The reality is that it is impossible to know the results from Bayesian modeling if not attempted. If the modeling produces the same interpretation as pre-existing chronological beliefs, then that is noteworthy finding as it makes those beliefs stronger. If the modeling has a different interpretation, that too is important. If it is between reaffirming older interpretations and forging new ones, then the application of Bayesian modeling should result in a discussion worth having.

THE BAYESIAN PROCESS

In the previous section, we tied the major misconceptions regarding Bayesian modeling directly to a lack of fundamental understanding regarding how the process works both in theory and in practice. Here we wish to lay bare the process to make clear that there is both objectivity and scientific rigor inherent in the choices made throughout the chain. The modeling approach can be distilled into the schematic shown in Figure 2, which is derived from and described in much more practical detail by Bayliss and Bronk Ramsey (2004).

Assess Existing Data and Knowledge

‘Existing data and knowledge’ refers primarily to legacy dating, but other forms of chronological information should be noted (e.g. probable date based on artifacts), as these can also be useful to help inform some of the decisions made further along. Any legacy radiocarbon dates – old dates

that a project has inherited from other archaeologists – will need to be thoroughly critiqued. Many archaeologists that have developed, or acquired, large radiocarbon databases have recently been undertaking some form of ‘data cleansing’ prior to analysis and interpretation, but this can be an exercise (i.e. if error > 100 then reject ¹⁴C age) that misses the importance of holistically understanding the sample, context, and date. At the very least, it is necessary to have a description of the dated sample, the specific laboratory methods, and where the sample came from in relation to the archaeological features. As mentioned above, this process can be very laborious. Recently we were faced with a series of radiocarbon dates from the SunWatch site near Dayton, Ohio that were not chosen by us, but which we wanted to model (Krus et al. 2015). One of the dates (M-1965) had contradictory information, where the Michigan date list indicated the sample was made up of “small pieces of charcoal from 6 or 8 of 20 refuse pits excavated” (Crane and Griffin 1970:166), yet this sample is most likely from a single refuse pit, Feature 6/8. The unidentified nature of the charcoal was still problematic, since there could conceivably be fragments that would otherwise incorporate an ‘old-wood’ offset, at least we were confident that the material came from a single feature and was not a composite from many different features!

In critiquing the legacy dates, the aim is to produce a commentary of reasons why each date accurately reflects the date of the deposit within which its sample was found. Furthermore, to provide clear explanations for the scientific and/or taphonomic issues associated with any dates that are deemed to provide unreliable dating evidence for the formation of its context. The connection between a sample, its context, and the ‘event’ under consideration is the most critical and tenuous link in the Bayesian modeling process (also see Dean 1978). Not only does it apply

to how we critique our legacy dates, but it also informs which samples are suitable for dating, and ultimately the types of chronological questions we can approach.

Define Problems

The most basic and common problem or question pertaining to site-based models concerns the timing and span of activity, and for many sites, in many periods, these can be answered satisfactorily with as few as a dozen well-chosen dates and no stratigraphy. As the archaeology and models become more complex, more nuanced chronological questions might arise, such as the date when a specific transformation to the site (e.g. building of a palisade or digging of a ditch) or internal event (e.g. construction of a house) occurred. Where there are multiple re-built houses or re-dug ditches, we might be able to delve into the realm of the tempo of change and search for temporal regularities to activity that might be interpretable within the scale of a single human lifetime.

Site-based questions can be scaled up to consider the timing of events and temporality of processes at regional, or even continental, scales. Regional chronologies are constructed in many ways, but the Bayesian approach almost invariably starts with an evaluation of the dates on a site-by-site, and context-by-context, basis. The types of models that are not wedded to site-based models are usually concerned with the currency of an artifact type, whereby dating the artifact directly (e.g. bone comb) or organic material in direct association with the artifact (e.g. organic residue on a pot) provides the required connection between sample, date, and question.

Identify Samples

Armed with the questions you want to answer, it is time to identify the contexts that contain samples suitable for dating, thereby giving you the best chance at success. Bear in mind that just because problems have been defined, samples suitable to achieve a satisfactory solution may not be available, so that the availability of suitable samples can dictate the range of possible questions.

This is usually the point where we would consider a sort of hierarchy of sample types, but to rank the samples on a ladder is potentially misleading as a high-ranking sample might have low utility for some questions (cf. Bayliss 2015). The general point about ranking your samples is to have samples that you can demonstrate, or argue, provide an accurate date for the deposit from which they were recovered. This does not mean that simply because a deer femur was recovered from a ditch fill, it dates when the ditch open or infilling. In many instances a disarticulated animal bone provides a low level of confidence, especially the smaller ones that easily can be bioturbated or anthropogenically redeposited. However, if part of a deer was recovered in articulation (e.g. foot bones) from this ditch, then we could argue that it went into the ground soon after the death of the animal and should accurately date when that deposit formed. Our disarticulated femur provides, at best, a *TPQ* for the infilling of the ditch.

In addition to articulated remains, samples functionally related to their deposit usually make a sound choice. Here we might select charcoal or charred grain from a hearth or oven, where we can make a sound inference that the material in the feature had recently died and been burnt *in*

situ. We might also extend this to a discrete dump of burnt material in a pit or ditch that has been interpreted as perhaps hearth waste. While there is likely an unknown lag between when the wood was collected and used, and when the hearth was cleaned out, this offset is almost certainly negligible, and in this example likely not to be even a year.

Build Simulation Models, Submit Samples, and Assess Results

With a solid understanding of the questions to be tackled and a list of the suitable samples available, it is time to construct simulation models and assess the possible results given these inputs and our current archaeological knowledge (see Bayliss et al. 2007; Steier and Rom 2000). This stage of the process is very much about trying to understand how the number of dates available (constrained either by physical suitable samples or finances), the relevant area of the calibration curve, and such information as the relationship between samples or shape of the prior probabilities applied to the dates all combine to produce an answer. This stage of ‘getting a feel for the data’ is critical in the Bayesian process, it is the point where the modeler becomes so familiar with how the priors and data work together that they can intuit how a change to one part of the model might affect the outcomes (Buck and Meson 2015).

Guided by the simulation results, samples are submitted. The role of the simulation is to optimize the sample selection process, but only a portion should be submitted in the initial round. Most dating programs following a Bayesian approach will have several rounds of dating. After receiving the results, we go back to our pool of potential samples and begin to simulate the results for adding radiocarbon results from another round of dating, and loop the process. By

going through a series of simulations before submitting each round of samples we can see what effect results from additional samples in specific areas of the model will have, thereby enabling us to problem-solve at each stage and manage expectations.

Finalizing Models

Developed simulations should lead to the construction of the primary model. If there are multiple readings of the archaeology or other prior information that can be added to the analysis, then additional models will be constructed for a sensitivity analysis. Further, as part of the modeling process it is always important to undertake quality assurance in the form of replication of some of the dates. Replication might include submission of two samples of the same type (e.g. charcoal of different species) or different types (e.g. grain and animal bone) from the same context as a means of checking the security of the deposit or to look for offsets. In some cases, it may even be desirable to split a sample and send it to two different laboratories as a means of independently verifying the results. While there is no hard rule on the level of replication one should undertake, we would suggest replicating somewhere on the order of 10 percent of the dates, with more replication occurring where there is greater uncertainty in the taphonomic security or general overall quality of the samples.

Publish Results and Interpretations

After all the work in dating samples and developing models, the results and interpretations are written up for publication. It is at this stage all the assumptions and choices that went into

constructing the models should be put forth in an accessible manner, allowing the reader to properly critique the work. Oftentimes, it is here that the level of transparency can be found lacking. While this paper is neither a ‘how-to’ manual for Bayesian modeling or a set of ‘best practice’ guidelines, the following are a few tips that will be helpful for a reviewer/reader:

- 1) Clearly define the model structure in the publication and link the ‘death’ of the dated sample to the formation of the deposit or archaeological event of interest. If a radiocarbon date does not fit expectations, explain why and determine the reason for the misfit (e.g. contamination, insecure context, lab error, statistical outlier).
- 2) Include the full model figure that shows the structure that has been described (e.g. the OxCal brackets and keywords). This should allow other researchers to recreate the model precisely, for all but the most sophisticated solutions. Consider including the raw code used to create the model as supplemental data. Similarly, consider including any prior probabilities that are not clearly defined.
- 3) Where durations are given in the text (e.g. span of an occupation, time between two events), include a figure of that probability. This is especially useful to demonstrate that a span might be skewed to a younger or older range.

In addition, there are a few conventions to reporting the modeled probabilities to bear in mind that may reduce any confusion in a reader.

- 1) Round modeled probabilities outward to 5 years. This is not a ‘rule’ by any means, but the IntCal13 calibration curve is constructed using a 5-year random walk algorithm and

much of the data underpinning the curve is from decadal tree-ring samples. In addition, the rounding often accounts for slight differences in results from the different runs of a model, and is easier for most people to retain in their heads.

- 2) Make certain to refer to any modeled or calibrated dates as ‘cal BC/BCE’ or ‘cal AD/CE’ (or ‘cal BP’).

Italicize modeled dates to set them apart from simple calibrated dates and inform the reader that you have done so because they are the result of an interpretative model.

A final note – uncalibrated radiocarbon ages are given as means and standard errors, thus approximating a normal distribution, making reference to one- and two-sigma ranges perfectly acceptable. However, calibrated radiocarbon dates and modeled probabilities are in no way normally distributed, and so their ranges should be referred to by the percent of the area of the probability represented below the curve (i.e. 68.2 percent or 95.4 percent). Oftentimes, when rounding the date ranges, the precision of the percent beneath the curve can be found to be truncated simply to 68 percent or 95 percent.

THE BAYESIAN PRACTICE

While a discussion of the Bayesian Process, as abstracted above, will sit well with many readers, we present here briefly an example of the process in practice. We consider a site consisting of negative (i.e. cut) features, with a rectangular post-built structure with central hearth, a few pits, and an enclosure ditch. The aim with this hypothetical example is to elucidate the thought process of the Bayesian modeler, while highlighting those areas of the modeling process that can

be especially challenging. In this example, we use the terminology implemented in the OxCal program, but the ideas remain the same whether using OxCal, BCal or other programs. For ease, we have use **Courier** font to denote the specific OxCal commands.

Defining the Problem

The first thing is to define the archaeological questions. In this case, we might want to know: 1) When did activity begin; 2) When did activity end; and 3) For how long did this activity take place? These are the most basic questions asked of any site-based model, because they refer to the broadest level of chronological enquiry. We cannot stress enough that these questions are almost never answerable by a single radiocarbon date, but are estimates derived from a chronological model that is composed of dates related to the activity that occurred between the actual start and end date at the site. While there may be instances that the modeled probability for a specific radiocarbon date is important or interesting (e.g. a burial, material associated with a specific artifact), more often than not, it is the ‘events’ that occur before, after and between the archaeological residues, which form the sampled material, that have particular meaning.

The two main building blocks of models are the ordered (**Sequence**) and unordered (**Phase**) groups. Thinking of the site described above, we might feel safe in assuming it is all a single period of occupation (there may even be artifactual evidence from across the site to suggest that it is all broadly contemporary). We have no defined relative ordering (e.g. stratigraphy) between any of the features, and so we can begin thinking about our radiocarbon dates ‘existing’ as an unordered group – a **Phase**. Given our assumption that the features are all related to a single

period of activity, we can progress and add two elements in the form of a ‘start’ and ‘end’ **Boundary**, and situate these three elements within a **Sequence**. By doing this, we have explicitly instructed the computer program that at some point in time in the past, for which we do not have a date, activity began on the site. The activity went on for some unknown duration, and then it ended. Furthermore, we have also defined that activity began before it ended.

At the most basic level, a **Boundary** defines the time that the dated activity begins and ends (Steier and Rom 2000; Bronk Ramsey 2001). They are placed within a **Sequence** as this sets up the necessary ordered relationship that activity begins, material that can be dated is deposited, and activity ends. Often boundaries are used to represent that start or end of activity at a settlement or of a phase of discrete activity within a settlement. Crucially, the time of a **Boundary** is estimated in a Bayesian chronological model, which provides archaeologists probabilistic estimates for events (such as the start of activity at a settlement) that cannot be directly dated. Figure 3 visually demonstrates how **Boundary**, **Phase**, and **Sequence** are incorporated into a simple Bayesian chronological model for an archaeological settlement with no dates from intercutting features. Algebraically, this model can be expressed as

$\alpha_{\text{settlement}} > \Theta_{\text{settlement}} > \beta_{\text{settlement}}$, where $\Theta_{\text{settlement}}$ is the set of dated events $\theta_1 . . . \theta_n$ from the continuous phase of settlement activity, represented by the radiocarbon-dated samples.

When using the standard **Boundary** parameters in OxCal, the program will apply a Uniform Prior Distribution (UPD) to the radiocarbon dates contained within the **Phase**. The UPD essentially indicates that activity goes from nil to maximum intensity, stays at maximum intensity for some time, and then switches back to nil. This is the simplest form of chronological

model, with the UPD being an *uninformative* prior, helping to constrain the dates based on the statistical scatter within the group. There are different ‘boundaries’ that can be used, enabling the start and end to be modeled as a steady or steep ramp, thereby altering the prior distribution being applied to the dates (Lee and Bronk Ramsey 2012). Despite the ability to alter the prior that is applied to the group of dates, the UPD has been shown to be extremely flexible and robust (Bayliss and Bronk Ramsey 2004), and we would suggest that in most cases, if alternative priors are used, that the UPD be run as a sensitivity analysis so that it is possible to see just how much an affect the different boundaries have on the final results.

The simple model described above is often referred to as a ‘Phase model’ or ‘Bounded Phase model’, and takes its name from the OxCal command that is similarly named – **Phase**. It is important to stress here that this is in no way similar to a traditional archaeological phase based on such things as ceramic or projectile point typologies. This type of model is extremely versatile and finds use in any situation where there is no relative ordering between samples (e.g. series of pits or the posts from a house).

The **Sequence** is especially powerful, with the temporal relationship it sets up between dates acting as an *informative* prior. Like the **Phase**, the **Sequence** can form the basis of the model structure, such as with a series of dates from an environmental core. But, its versatility lies in the ability to function as a building block within a more complex model structure. Thinking to our hypothetical site, if we dated sequential charcoal lenses in the ditch, then we could place those dates into a **Sequence** within the overall unordered group of dates within the **Phase**. The

informative prior only affects those stratigraphically-related dates, but allowing them to contribute to the mathematics applied to the overall group.

Not only can **Sequences** exist within a **Phase**, but a **Phase** can exist within a **Sequence**.

This nesting of ordered and unordered groups of dates allows the construction of complex models from complex archaeological sites. This level of model complexity is beyond the immediate scope of this paper, but we direct the reader to the work of Harris (1989) for a discussion of single-context recording and the production of ‘Harris matrices’, as well as Dye and Buck (2015) for further discussion of the use of matrices and diagrams for developing models and displaying their structure.

Creating models using the building blocks (**Phase** and **Sequence**) is a straight-forward exercise, often what is being modeled are the relationships observed or inferred between samples or dated contexts. However, the easiness of this element of the process can have the deleterious effect of leading people to simply take a plug-and-play approach to chronological modeling, and not focus on the most tenuous element of the entire chain: the relationship between the date of the sample and the date of the context.

Selecting the Samples

As the prior information becomes more informative (e.g. stratigraphic relationships are included), it becomes increasingly important to minimize the time-lag between the date of the death of the sample and the date of the formation of the deposit. This is where the notion of the

hierarchy of samples, alluded to above, becomes a useful device. While there is no strict ‘best’ to ‘worst’ sample, our goal in almost every case is to select a sample whose radiocarbon date is the same as the date it was buried in the context from which it was recovered. Taphonomic understanding is critical for understanding how the dates of the two events (sample death and context formation) are related, and for this reason, bone that is recorded as articulated during excavation, or noted as likely having been articulated when undergoing post-excavation analysis, is often considered to be the ‘gold standard’ for site-based models. These samples are highly unlikely to have remained intact for any long duration before burial. Unfortunately, these samples are a rarity on most archaeological sites, and so many of the modeled samples will either have a functional or inferred relationship made between the sample and formation of its context.

Defining a functional relationship between a sample and context is not a difficult task, and one which archaeologists regularly do as part of the excavation process. Arguably, the most ubiquitous sample from a site is charcoal, and if that charcoal comes from a hearth, it is possible to define this functional relationship to explain both *how* and *why* that sample was recovered from that feature. Another sample that has a clear functional relationship is a charred food residue on a sherd of pottery, the date from which should reflect the date of the foodstuff that was burnt (this is barring any potential reservoir offset in the date).

The next tier sample is where the relationship to the context can be inferred, and here we are referring to things such as: discrete dumps of charred material that may be interpreted as the debris cleaned out from a hearth, or charred debris from the use of a structure that has filtered down into the post-pipe that forms as an internal post decays. In all cases, it is important that the

relationship be defined, and the more tenuous it is, the more rigorously it be defended. Turning back to our hypothetical site, we would be looking first and foremost for samples, such as articulated/ing animal bone in the pits or ditch, or short-lived samples of charcoal or charred cereals in the hearths, and finally for similar charred debris in the post-pipes of the houses or as discrete fills in the ditch.

Dealing with Age Offsets, Outliers, and Misfits

Even after defining realistic problems and selecting and submitting secure samples for dating, it is likely that some of the dates will not conform to prior expectations. The results can be either older or younger than expected, and as a rule of thumb, all samples should be considered residual until otherwise demonstrated. Beyond re-evaluating the probable taphonomic history of a sample, consideration should be made of other potential sources for error, including the possibility for an in-built age offset or sample contamination.

In-built age offsets describe instances where the radiocarbon age is older than would be expected, given the date the organism died. Generally, when dealing with samples that have not been mishandled or undergone any form of conservation, there are two primary age offsets that we must consider: (1) old wood offset; and (2) reservoir offset, commonly in the form of a dietary offset.

Demonstrated old wood offsets in charcoal (Schiffer 1986) are often used as a reason to discount ‘archaeologically unacceptable’ radiocarbon results. The reality is that *all* wood samples that are

not bark or the final ring will have a radiocarbon age that is a weighted mean (by mass) of the radiocarbon content of all the rings in the sample. By selecting short-lived species, or twiggy pieces of wood from a sample, the offset is minimized, and when the models also include animal bone and seeds, the minor offset in the charcoal samples will be negligible to the model results. Where there is some confusion, or lack of documentation, about what charcoal was dated, rather than exclude a date from a model it is completely acceptable to include the result as a *TPQ* for the formation of the deposit. Furthermore, formalized statistical tools are available in OxCal that allow for an old wood offset in charcoal to be modeled, in the form of a Charcoal Outlier Model (Bronk Ramsey 2009b). This form of model can be especially useful when attempting to achieve very high precision and nearly all the samples are on charcoal (see Hamilton and Kenney [2015] for a worked example), as the dates in the model most likely to be outliers have their effect on the results downweighted.

The second offset we consider is a result of the carbon in the sample not being in equilibrium with the terrestrial biosphere, a reservoir offset. This commonly occurs through a marine reservoir effect (MRE), with the global average marine offset equivalent to approximately 400 years, but can also take the form of a freshwater reservoir effect (FRE), usually the result of dissolved geologic carbon (e.g. radioactively ‘dead’ in terms of ^{14}C) in a freshwater lake or stream. When plants photosynthesize in these environments by taking in CO_2 from the water, they incorporate this age offset, which propagates along the food chain. While MRE and FRE add a layer of complexity to analyzing and interpreting radiocarbon dates, it is possible to accurately model the dates of species from the marine environment (e.g. fish, seals, whales) and even model the dates from omnivores that received all or part of their dietary protein from

marine species (G. Cook et al. 2015). Correcting for FRE is slightly more difficult as it requires calculating the FRE for a specific place and time, with the correction made to the uncalibrated radiocarbon age. Using new Bayesian tools to ‘unmix’ the contribution of terrestrial, marine, and freshwater protein to an individual’s diet, it is possible to robustly model the dates of individuals who consumed animals with both an MRE and FRE (Sayle et al. 2016).

After considering these forms of offset and error, it is important to remember that even radiocarbon laboratories can make mistakes. While labs have stringent internal quality assurance protocols, there are instances where a date is simply incorrect with no indication what went wrong. This is one reason why replication is important, and if possible the replication should be made using a second laboratory as the additional check. Finally, it is important to remember that the radiocarbon dating process is a statistical one, where the ‘result’ received from the laboratory is a probabilistic statement – a measurement mean and standard error – that at 2σ (95.4 percent probability) should contain the *real* radiocarbon age. Therefore, we should expect 1 in 20 radiocarbon ages to fall outside of the 95.4 percent probability range, and can only hope that it is not so far outside that range to make our interpretations importantly wrong.

CONCLUSIONS

Many American Archaeologists are becoming increasingly aware of studies employing Bayesian chronological modeling and are either experimenting with applications for the first time or working with collaborators. Bayesian modeling amongst professionals and students in the Americas is rapidly increasing (Figure 1). Recently, George Cowgill (2015b) in a *Latin*

American Antiquity forum essay strongly encouraged American archaeologists to adopt Bayesian chronological methods. In addition to the published literature, this interest is evident from the increasing number of presentations we see each year at the Society for American Archaeology meeting and regional conferences in the Americas using Bayesian chronological models.

We hope this essay brings a wider awareness to the noted issues and that journal editors and grant proposal reviewers familiarize themselves with these issues and the best practice methods provided in Bayliss (2015) and Buck and Meson (2015). We further recommend that anthropology departments and regional archaeological organizations offer more courses and other training activities that cover the fundamentals of Bayesian chronological modeling methods, because these methods will soon be considered part of the standard American archaeological toolkit.

It is especially important that archaeologists using these methods always consider that results with low precision are likely accurate and that pre-existing beliefs, while sometimes very precise, might be inaccurate. Like Michezyński's (2007) conclusions regarding best practice for interpretations of probabilistic radiocarbon calibration, it is also important that 95 percent and 68 percent posterior probability ranges receive the most interpretative weight, even when the model results are largely imprecise. It is also important that archaeologists understand how calibration curve wiggles, such as the 'Hallstatt plateau' and others, affect the precision of their modeled results. Poor awareness of calibration curve wiggles can lead to misinterpretations (as described in Baillie [1991], Guilderson et al. [2005], and Krus et al. [2015]). While imprecise modeling results are unfortunate, conclusions can still be drawn from those situations and can include

discussions of the future scientific work to produce finer chronologies. Importantly, experiments with simulated radiocarbon data should be run in Bayesian chronological modeling software to precisely estimate the number of radiocarbon dates needed to produce precise and accurate models, which is a highly effective practice for determining the number of dates are needed to overcome calibration curve wiggles.

Finally, it is important that American archaeologists understand that Bayesian chronological modeling is both a scientific and a theoretical revolution for our discipline (Bayliss 2009). Future work in the Americas has potential to greatly improve our understandings of lived experiences, temporality and cultural change derived probabilistically from posterior probabilities. When discussing the future of Bayesian chronological modeling, Buck and Meson (2015:577–579) emphasize that radiocarbon simulations have thus far been underused as a tool for improving the research designs of chronology building programs and that these simulations are enormously useful for informing the selection of radiocarbon research designs. Similarly, at the 2017 Society for American Archaeology meeting, we noticed that most of the presented chronological modeling dealt with the analysis of legacy dates, with almost no discussion about how the Bayesian process will be used to inform the selection of new data.

We hope this essay brings a greater awareness of how the Bayesian process can be used to shape all aspects of an archaeological research design, from the initial formation of a data collection strategy to the publication of results. While this essay can be read as an introduction, we encourage readers to review the literature in the works cited section to learn more, and to contact established individuals who are publishing Bayesian models for practical advice.

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Supplemental Materials. Supplemental files 1–2 are accessible as supplemental materials linked to the online version of the paper, which is accessible via the SAA member login at www.saa.org/members-login.

Supplemental file 1. The references for the papers in Figure 1 not cited in text.

Supplemental file 2. Some references for the use of Bayesian statistics in the physical/natural sciences not cited in text.

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Figure Captions

Figure 1: Histogram for the number of published Bayesian chronological modeling applications in American archaeology from 1990–1999, 2000–2009, and 2010–2015

Figure 2: The Bayesian method in practice (after Bayliss and Bronk Ramsey 2004:28, fig. 2.2; Bayliss 2009:132, fig. 9)

Figure 3: Bayesian chronological model structure demonstrating the use of radiocarbon measurements within **Boundaries**, **Sequence**, and a **Phase**. The large square ‘brackets’ along with the OxCal keywords define the overall model exactly. OxCal script for the model is shown below the model structure.

Figure 1

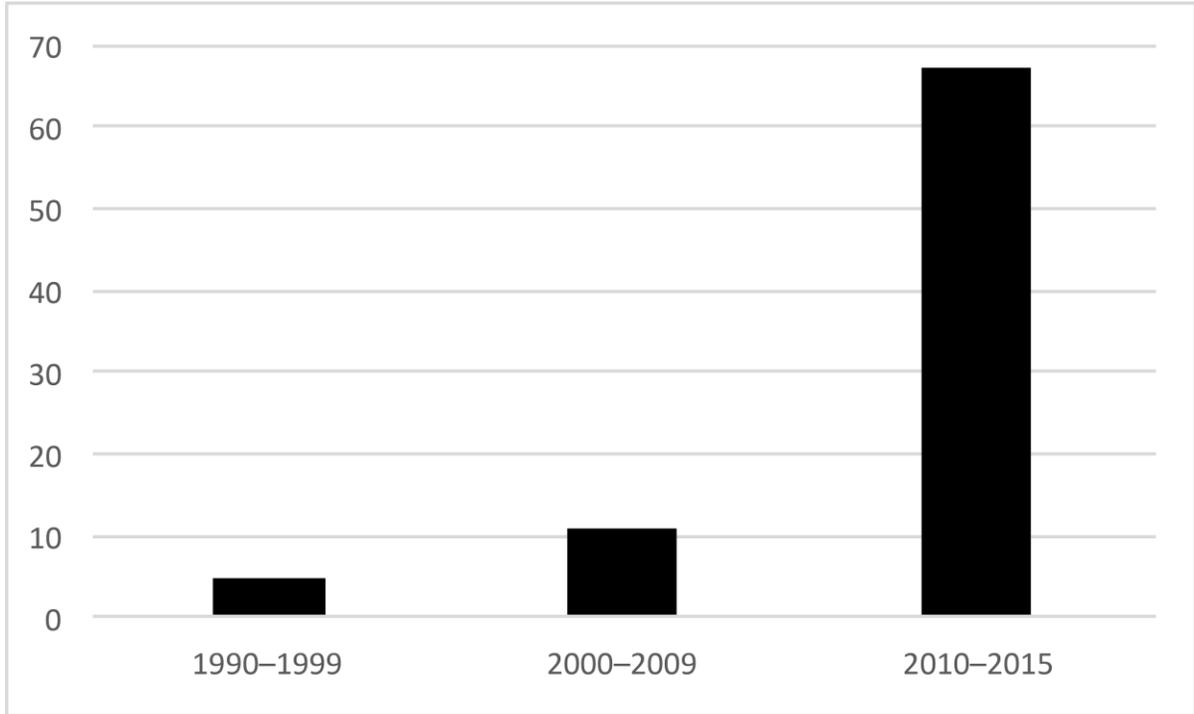


Figure 2

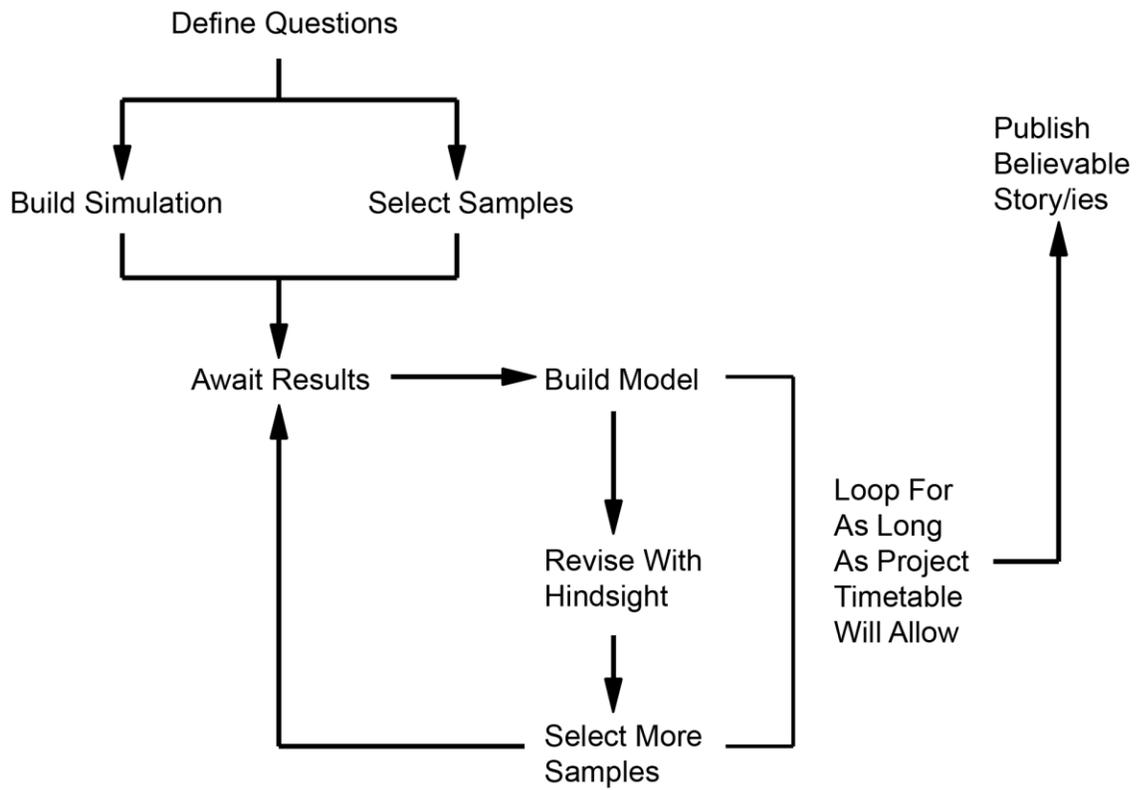


Figure 3



```
Plot()  
{  
  Sequence("settlement")  
  {  
    Boundary("start settlement activity");  
    Phase("continuous phase of activity")  
    {  
      R_Date("Radiocarbon date name", conventional radiocarbon age (BP), conventional radiocarbon age error);  
      R_Date("Radiocarbon date name", conventional radiocarbon age (BP), conventional radiocarbon age error);  
      R_Date("Radiocarbon date name", conventional radiocarbon age (BP), conventional radiocarbon age error);  
      R_Date("Radiocarbon date name", conventional radiocarbon age (BP), conventional radiocarbon age error);  
    };  
    Boundary("end settlement activity");  
  };  
};
```

Supplemental file 1: The references for the papers in Figure 1 not cited in text

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