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Measurement of the $D^{+}$-meson production cross section at low transverse momentum in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV


(CDF Collaboration)
We report on a measurement of the $D^+$-meson production cross section as a function of transverse momentum ($p_T$) in proton-antiproton ($p\bar{p}$) collisions at 1.96 TeV center-of-mass energy, using the full data set collected by the Collider Detector at Fermilab in Tevatron Run II and corresponding to 10 fb$^{-1}$ of integrated luminosity. We use $D^+ \rightarrow K^- \pi^+ \pi^+$ decays fully reconstructed in the central rapidity region $|y| < 1$ with transverse momentum down to 1.5 GeV/$c$, a range previously unexplored in $p\bar{p}$ collisions. Inelastic $p\bar{p}$-scattering events are selected online using minimally-biasing requirements followed by an optimized offline selection. The $K^-\pi^+\pi^+$ mass distribution is used to identify the $D^+$ signal, and the $D^+$ transverse impact-parameter distribution is used to separate prompt production, occurring directly in the hard scattering process, from secondary production from $b$-hadron decays. We obtain a prompt $D^+$ signal of 2950 candidates corresponding to a total cross section $\sigma(D^+, 1.5 < p_T < 14.5$ GeV/$c, |y| < 1) = 71.9 \pm 6.8$(stat) $\pm 9.3$(syst) $\mu$b. While the measured cross sections are consistent with theoretical estimates in each $p_T$ bin, the shape of the observed $p_T$ spectrum is softer than the expectation from quantum chromodynamics. The results are unique in $p\bar{p}$ collisions and can improve the shape and uncertainties of future predictions.

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Measurements of cross sections for the production of hadrons containing bottom or charm quarks (heavy-flavors) in hadron collisions offer fundamental information to test and refine phenomenological models of the strong interaction at small momentum transfer, a regime in which perturbative expansions are challenging. In addition, in searches for astrophysical neutrinos, knowledge of charm production cross sections may improve estimations of background rates from neutrinos produced in decays of charm hadrons from cosmic-ray interactions with atmospheric nuclei [1].

The first studies of heavy-flavor production performed at the Tevatron proton-antiproton ($p\bar{p}$) collider in 1992–1996 [2] yielded cross sections significantly larger than the predicted values [3] and prompted a dedicated effort in refining calculations [4], which resulted in reduced discrepancies. The program continued during Tevatron Run II (2001–2011), including first measurements of charm-meson cross sections using $p\bar{p}$ collisions at center-of-mass energy $\sqrt{s} = 1.96$ TeV [5]. Since 2010, CERN’s LHC $pp$ collider has replaced the Tevatron as the most prolific charm-meson source, allowing the ALICE and LHCb experiments to report measurements of charm cross sections at $\sqrt{s} = 2.76$–13.00 TeV [6].

Measurements based on $p\bar{p}$ collisions, and probing different collision energies, remain essential to extend the understanding of quantum chromodynamics (QCD), because differing admixtures of parton-level processes contribute at different energies and initial states. Previous measurements in $p\bar{p}$ collisions [5] were restricted to mesons with transverse momentum $p_T > 6.0$ GeV/$c$ because of the transverse-momentum thresholds used in the online event selection (trigger). The transverse momentum is the momentum component in the plane transverse to the beam. Extending the reach to lower $p_T$, hence further into the nonperturbative regime, provides novel and unique constraints to improve QCD phenomenological models.

In this paper, we report on a measurement of the production cross section for $D^+$ mesons down to 1.5 GeV/$c$ $p_T$, a range unexplored in $p\bar{p}$ collisions, and unlikely to be explored in the foreseeable future with this initial state. The measurement is performed as a function of meson transverse momentum using $D^+ \rightarrow K^-\pi^+\pi^+$ decays reconstructed in the full CDF Run II data set, corresponding to 10 fb$^{-1}$ of integrated luminosity. Throughout this paper charge-conjugate decays are implied. Candidate $D^+$ signal events are selected from a minimum-bias sample, collected by imposing minimal requirements on the event features in order to minimize biases on the physics properties of charm decays. Events are divided into independent subsamples ($p_T$ bins) according to the $D^+$ candidate $p_T$. In each, we apply a data-driven optimization of the offline selection and perform a two-dimensional simultaneous fit of the resulting distributions of the $K^-\pi^+\pi^+$-mass and $D^+$ impact-parameter, defined as the minimum transverse distance between a particle’s trajectory and the beam. The fit determines, for each $p_T$ bin, the prompt $D^+$ yield ($D^+$ mesons directly produced in the $pp$ interaction or originating from charm resonances) by
statistically subtracting secondary $D^+$ candidates ($D^+$ mesons originating from $b$-hadron decays). Each prompt yield is combined with the corresponding reconstruction and selection efficiencies, derived using simulation, to determine the cross section,

$$\sigma_i = \frac{N_i/2}{\int \mathcal{L} dt \cdot \epsilon_i \cdot B},$$

(1)

where $N_i$ is the observed number of prompt $D^+$ and $D^-$ mesons in the $i$th $p_T$ bin. The factor $1/2$ is included because both $D^+$ and $D^-$ mesons contribute to $N_i$ and we report results solely for $D^+$, assuming charge-symmetric production of charm quarks in the strong $p\bar{p}$ interaction. The integrated luminosity $\int \mathcal{L} dt$ is normalized to an inelastic cross section of $\sigma_{pp} = 60.7 \pm 2.4$ mb \cite{2} and $\epsilon_i$ is the global detection, reconstruction, and selection efficiency. The branching fraction used for the $D^+ \rightarrow K^-\pi^+\pi^+$ decay is $B = (9.46 \pm 0.24)\%$ \cite{8}.

The CDF II detector is a multipurpose magnetic spectrometer surrounded by calorimeters and muon detectors \cite{9}. It is roughly cylindrically symmetric around the beams and is described in a cylindrical coordinate system with the $z$ axis along the incident proton beam direction. The detector components relevant for this analysis are as follows. A silicon microstrip vertex detector and a cylindrical open-cell drift chamber immersed in a nearly uniform 1.4 T axial magnetic field allow the reconstruction of charged-particle trajectories (tracks) in the pseudorapidity range $|\eta| < 1$. The vertex detector contains seven concentric layers of single- and double-sided silicon sensors at radii between 1.5 and 22 cm, each providing a position measurement with up to 15 (70) $\mu$m resolution in the azimuthal (longitudinal) direction \cite{10}. The drift chamber has 96 measurement layers, located between 40 and 137 cm in radius, organized into alternating axial and $\pm 2\theta$ stereo superlayers \cite{11}. The transverse momentum is determined with a resolution of $\sigma_{p_T}/p_T^2 \approx 0.07\%$ (GeV/c)$^{-1}$, corresponding to a typical mass resolution of 6.0 MeV/c$^2$ for a $D^+ \rightarrow K^-\pi^+\pi^+$ decay. Gas Cherenkov detectors (CLC) covering the symmetric regions at small polar angle around the interaction region $3.7 < |\eta| < 4.7$ are used to detect hard-scatter interactions and measure luminosity \cite{12}. CDF has a three-level trigger system. We use events collected by the zero- and minimum-bias triggers, which are designed to collect events while introducing minimal bias in the properties of the particles produced in the collision. The zero-bias trigger applies no selection requirements and accepts a $10^{-6}$ fraction (prescale factor) of $p\bar{p}$ crossings, randomly chosen. At the first trigger level, the minimum-bias trigger accepts a $10^{-5}$ prescale fraction of the events in which a time-coincidence between signals in the CLC at opposite sides of the interaction region is detected, which enriches the sample in $p\bar{p}$ crossings that yield inelastic interactions. At the second (third) trigger level, the minimum-bias trigger applies no requirements and accepts events with 3 (1) Hz maximum rates. The large prescale factors and accept-rate reductions avoid saturation of the data-writing rate. The resulting samples contain 183 million zero-bias and 133 million minimum-bias events. Of these, 409 events are common to both samples and used only once in the analysis.

The offline reconstruction of $D^+ \rightarrow K^-\pi^+\pi^+$ candidates is based solely on tracking information without using particle identification, the same-charge particles being assigned the pion mass. Three good-quality tracks, associated with drift-chamber and silicon-detector information and consistent with a $K^-\pi^+\pi^+$ decay, are combined in a kinematic fit to a common decay vertex to form a $D^+$ signal candidate. Additional selection criteria are applied on the vertex-fit quality; the minimum azimuthal separation of any pair of signal tracks; the product of their impact parameters; and the minimum value of $D^+$ transverse decay-length projected onto the direction of its $p_T$, $L_{xy}$. These criteria are fully efficient for signal and reduce backgrounds from combinations of random charged particles (combinatorics). No events are observed with more than one reconstructed candidate. We further improve the signal-to-background ratio by optimizing the selection, separately for events restricted to each of the five $D^+$ candidate $p_T$ bins, 1.5–2.5, 2.5–3.5, 3.5–4.5, 4.5–6.5, and 6.5–14.5 GeV/c. First, we apply an upper threshold of 100 $\mu$m on the impact parameter of the $D^+$ candidates. This suppresses secondary $D^+$ candidates, which are less likely to point back to the $p\bar{p}$ vertex because of the combined effect of the long lifetime of $b$ hadrons and the energy released in their decay. This requirement is applied only for the optimization (see below), but is lifted in further analy-
sis, where a fit of the $D^+$ impact-parameter distribution separates statistically the signal of prompt $D^+$ candidates from the secondaries. Then we divide the sample randomly into two subsamples. In each, we conduct an independent optimization by maximizing the quantity $S/S^+B$ over 1000 possible configurations of requirements on the minimum $p_T$ ($p_{T,\min}$) of any two final-state particles, minimum $L_{xy}$, and maximum value of the vertex-fit $\chi^2$. The signal (background) yields $S$ ($B$) are estimated from fits of the $K^-\pi^+\pi^+$ mass distributions with a Gaussian model for the signal and a smooth empirical function for the background. Finally, the optimal configuration resulting from each subsample is applied on the complementary subsample. Use of a data-driven optimization avoids the modeling uncertainties of simulation-driven methods. Biases due to statistical fluctuations are avoided by applying selection criteria identified on one subsample to the other half of the sample. The optimized criteria vary in the ranges $p_{T,\min} > 0.6 - 1.1$ GeV/$c$, $L_{xy} > 600 - 700 \mu$m, and $\chi^2 < 2 - 7$, depending on subsample and $p_T$ bin. The $K^-\pi^+\pi^+$ mass distribution of the resulting sample, summed over all $p_T$ range, is shown in Fig. 1. A prominent narrow peak of approximately 3400 $D^+\rightarrow K^-\pi^+\pi^+$ decays, comprising both prompt signal and secondary charm candidates, overlaps a smooth background dominated by combinatorics. In each $p_T$ bin, we determine the yield of prompt $D^+$ decays using a simultaneous maximum-likelihood fit to the unbinned distributions of $K^-\pi^+\pi^+$ mass, to separate $D^+$ decays from combinatorics, and $D^+$ impact parameter, to separate prompt from secondary $D^+$ decays. The fit model is a linear combination of probability density functions (pdf) for prompt $D^+$ signal, secondary $D^+$, and combinatorial background, each consisting of the product of mass and impact-parameter pdfs. In the mass pdf, prompt and secondary components are modeled jointly with a Gaussian function determined from simulation; the background pdf is a second-order polynomial function derived empirically from regions with $D^+$ mass in 1.7–1.8 or 1.9–2.0 GeV/$c^2$ (sidebands). In the impact-parameter pdf, the prompt (secondary) component is modeled with the sum of three narrow (broad) Gaussian distributions determined using simulation whereas the background is modeled with a combination of Gaussian shapes that empirically reproduce the impact-parameter distribution of sideband events. The only free parameters in the fit are the numbers of prompt $D^+$ (signal) decays and secondary $D^+$ decays. Tests on simplified simulated experiments show that the fit estimates are unbiased and have proper Gaussian uncertainties. Figure 2 shows examples of fits in two $p_T$ bins, 2.5 $< p_T < 3.5$ GeV/$c$ and 6.5 $< p_T < 14.5$ GeV/$c$. A total signal of approximately 2950 prompt $D^+$ decays is obtained. The observed fraction of secondary decays is typically 15% of the total $D^+$ yield, but ranges between 0% and 40% with large uncertainties, depending on $p_T$. We vary the parameters and assumptions of the signal and background models and attribute systematic uncertainties on prompt signal yields in the range 0.9%–1.5%, depending on the $p_T$ of the candidate.

We factorize the reconstruction efficiency $\epsilon_i$, relative to the $i$th $p_T$-bin, into the product of trigger efficiency, offline efficiency for reconstructing three tracks that meet the quality and fiducial requirements in the drift chamber, offline efficiency for assigning the information from the silicon detector to these tracks, and the efficiency of the offline selection requirements. The zero-bias trigger efficiency is 100% by construction. The minimum-bias trigger efficiency is determined to be $(98.8_{-0.4}^{+0.2})%$ from the ratio of $D^+$ signal yields observed in zero-bias events that meet, or fail, the minimum-bias requirements. All offline efficiencies are known to be reproduced accurately by the simulation except for the term associated with the silicon detector. We therefore use efficiencies derived from simulation as inputs for the measurement and use control samples of data to obtain systematic uncertainties that cover potential data-simulation discrepancies in the silicon-related efficiency. Offline efficiencies ranging from 0.27% to 7.5% are determined from simulated events containing $D^+ \rightarrow K^-\pi^+\pi^+$ decays, in which distributions are weighted so that the multiplicity of prompt vertices reproduces the distribution observed in data. Control samples of muons from $J/\psi \rightarrow \mu^+\mu^-$ decays and low-momentum pions from $D^{+}\rightarrow D^0(\rightarrow K^-\pi^+)\pi^+$ decays, in which only drift-chamber information is used to select and reconstruct the charged particle, are used to determine silicon efficiencies as functions of charged-particle $p_T$ and data-taking time from the fraction of charged particles that also meet the silicon requirements. The results are compared with silicon efficiencies determined in simulation, and the maximum observed deviation, 3.7%, is used as the systematic uncertainty on the per-track efficiency, resulting in an 11.5% uncertainty common to all $D^+$ transverse momentum bins. This is the largest systematic uncertainty. Additional systematic uncertainties associated with imperfect descriptions of multitrack efficiency correlations, ionization energy loss, and hadronic interactions in the inner tracker material are negligible. Repeating the measurement on independent subsamples of data split according to data-taking time and $D$ candidate charge shows no evidence of residual biases.

The measured differential cross sections, averaged over each $p_T$ bin and integrated over the rapidity range $|y| < 1$, are shown in Table I and displayed in Fig. 3. The observed cross sections are compatible with those predicted in recent calculations except with those determined in early Run II using an independent data set. The total cross section for the production of $D^+$ mesons in the kinematic range $1.5 < p_T < 14.5$ GeV/$c$ and $|y| < 1$, obtained by summing over all $p_T$ bins, is $71.9\pm6.8\pm9.3 \mu$b, where the first contribution to the uncertainty is statistical and the second systematic.
In summary, we report on a measurement of the prompt \( D^+ \)-meson production cross-section, as a function of transverse momentum, in proton-antiproton collisions at \( \sqrt{s} = 1.96 \) TeV, using the full data set collected by the CDF experiment in Tevatron Run II, and corresponding to 10 fb\(^{-1}\) of integrated luminosity. We use prompt \( D^+ \rightarrow K^- \pi^+ \pi^+ \) decays with transverse-momenta down to 1.5 GeV/c fully reconstructed in the central rapidity region \( |y| < 1 \). The differential cross section is averaged in each \( p_T \) bin and integrated over the \( D^+ \) rapidity interval \( |y| < 1 \). The total cross section is \( \sigma(D^+, 1.5 < p_T < 14.5 \) GeV/c, \( |y| < 1) = 71.9 \pm 6.8(\text{stat}) \pm 9.3(\text{syst}) \) mb. The results are unique in that they probe strong-interaction dynamics in a low-\( p_T \) regime unexplored in charm-meson production from proton-antiproton collisions. At higher transverse momentum, where previous measurement are available, the current measurements agree with earlier results [5]. While the individual measurement points lie within the band of theoretical uncertainty, the experimental spectrum is systematically shifted to high \( p_T \)-values as compared with theory. Hence, these results may help to further refine the shape of the theoretical cross section as a function of transverse momentum. The results may also be helpful for understanding backgrounds in astrophysical neutrino experiments at a few PeV, where most background sources are suppressed and the contributions from charm hadrons produced in the interaction of cosmic rays and atmospheric nuclei could be important.

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| \( p_T \) range \( (\text{GeV}/c) \) | Eff. \( p_T \) \( \text{GeV}/c \) | \( d \sigma(D^+, |y| < 1)/dp_T \) \( \text{(mb/GeV}/c) \) | \( \sigma(D^+, |y| < 1) \) \( \text{(mb)} \) |
|---|---|---|---|
| 1.5 - 2.5 | 2.04 | 32.7 \pm 6.5 \pm 4.2 & 32.7 \pm 6.5 \pm 4.2 |
| 2.5 - 3.5 | 2.98 | 20.6 \pm 1.8 \pm 2.7 & 20.6 \pm 1.8 \pm 2.7 |
| 3.5 - 4.5 | 3.97 | 9.5 \pm 0.8 \pm 1.2 & 9.5 \pm 0.8 \pm 1.2 |
| 4.5 - 6.5 | 5.38 | 3.2 \pm 0.3 \pm 0.4 & 6.5 \pm 0.5 \pm 0.8 |
| 6.5 - 14.5 | 9.19 | 0.34 \pm 0.03 \pm 0.04 & 2.69 \pm 0.22 \pm 0.35 |

TABLE I. Prompt \( D^+ \)-meson cross-section results. All cross-section values are integrated over the range \( |y| < 1 \). The second column ("effective \( p_T \)"") lists the \( p_T \) values at which the differential cross section equals its average over that \( p_T \) bin, as determined using Ref. [14]. Values in the third (fourth) column are averaged (integrated) over each \( p_T \) bin. The first contribution to the uncertainties is statistical, the second systematic.

FIG. 2. Distributions of (a) \( K^- \pi^+ \pi^+ \) mass for candidates with \( 2.5 < p_T < 3.5 \) GeV/c and (b) \( D^+ \) impact parameter for those candidates, further restricted to have \( K^- \pi^+ \pi^+ \) mass within three standard deviations from the peak value. Fits are overlaid. Panels (c) and (d) show the same distributions for candidates with \( 6.5 < p_T < 14.5 \) GeV/c.
FIG. 3. Differential cross section as a function of $p_T$ for prompt $D^*$ mesons with $p_T > 1.5$ GeV/c, compared with predictions from Ref. [14]. In each bin, the data point is displayed at the $p_T$ value at which the differential cross section equals its average over that $p_T$ bin, as determined using predictions from Ref. [14]. These “effective $p_T$” values are also listed in Table I.

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