

First measurement of target and beam-target asymmetries in the $\gamma p \rightarrow \pi^0 \eta p$ reaction

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The first data on target and beam-target asymmetries for the $\gamma p \rightarrow \pi^0 \eta p$ reaction at photon energies from 1050 up to 1450 MeV are presented. The measurements were performed using the Crystal Ball and TAPS detector setup at the Glasgow tagged photon facility of the Mainz Microtron MAMI. The general assumption that the reaction is dominated by the $\Delta 3/2^-$ amplitude is confirmed. The data are in particular sensitive to small contributions from other partial waves.

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I. INTRODUCTION

Photoinduced production of $\pi^0 \eta$ pairs is a relatively new topic in particle physics. Nevertheless, since modern 4π photon detectors in combination with high intensity photons beams have become available, a large amount of data, primarily angular and momentum distributions have been measured. The production of the meson pairs is sensitive to sequential decays of baryon resonances such as $\Delta^* \rightarrow \Delta(1232)\eta \rightarrow N\pi^0\eta$ and $\Delta^* \rightarrow N^*(1535)\pi^0 \rightarrow N\eta\pi^0$. Hence, $\pi^0 \eta$ meson pair production is a complementary tool to study nucleon and Δ excitation spectra

providing additional information compared to single π or η photoproduction. Remarkably, till now no major disagreements between experimental data and state-of-the-art model predictions for the $\gamma p \rightarrow \pi^0 \eta p$ reaction have been observed. The main reason for this is due to the fact that this reaction seems to be dominated by just a single partial-wave amplitude. Several independent studies [1–9] agree with the assumption that the $\gamma p \rightarrow \pi^0 \eta p$ reaction mainly proceeds via excitation of the $\Delta 3/2^-$ amplitude with a moderate admixture of positive parity resonances and generally insignificant contributions from nonresonant Born terms. As a consequence, even though the models differ from each other in detail, they provide similar results for many observables. In order to disentangle small components in the reaction amplitude, it is therefore important to study spin observables which are especially sensitive to interference terms. The situ-

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ation is similar to single π^0 photoproduction at energies up to $E_\gamma = 400$ MeV, which is dominated by the magnetic $\Delta 3/2^+$ multipole amplitudes due to the excitation of the $\Delta(1232)P_{33}$ resonance or single η production close to threshold, which is dominated by the $N^*(1535)S_{11}$ resonance.

The possibility of model independent partial-wave analysis of a so-called ‘‘complete’’ set of measurements is often one of the main motivations given for polarization measurements. Such a ‘‘complete experiment,’’ which is a complex and extensive task for single meson photoproduction, is even more difficult for reactions in which two mesons are emitted. However, in some cases it is possible to study the partial wave content using a restricted number of observables, making some physically reasonable general assumptions about the production mechanisms. Some polarization observables for $\gamma p \rightarrow \pi^0 \eta p$ were already measured and analyzed in earlier papers [6, 10–13]. Here we report the first measurements of asymmetries obtained using a transversely polarized proton target. Our main objectives are to check the consistency of the experimental target and beam-target asymmetry data with the dominant $\pi^0 \eta$ production mechanism and to investigate small contributions from partial waves other than the dominant $\Delta 3/2^-$ amplitude.

II. GENERAL FORMALISM

The general formalism for photoproduction of two pseudoscalar mesons on nucleons has been developed in Refs. [14] and [15], where the formulas for different polarization observables are presented. In the expressions below, we denote the final state particles as 1, 2, and 3 and consider the particle selection $1 + (23)$, with reference to the coordinate system presented in Fig. 1. The results are presented for three independent particle sets, corresponding to the numbering $1 + (23) = \eta + (\pi p)$, $\pi + (\eta p)$, and $p + (\pi \eta)$. In each case the z axis is directed along the photon momentum. The x and y axes are chosen such that the momentum of particle 1 has a positive x projection and is orthogonal to the y axes. As independent kinematical variables we choose angles $\Omega_1 = (\Theta_1, \Phi_1 = 0)$ of particle 1 in the overall center-of-mass (cm) system, together with angles $\Omega_{23}^* = (\theta_{23}^*, \phi_{23}^*)$ of particle 2 in the cm system of the pair (23) and their corresponding invariant mass M_{23} .

If the target nucleon is transversally polarized and the incident photon beam is circularly polarized, the cross section can be written in the form (see Eq. (57) of Ref. [15])

$$\frac{d\sigma}{d\Omega_1 dM_{23} d\Omega_{23}^*} = \frac{d\sigma_0}{d\Omega_1 dM_{23} d\Omega_{23}^*} \left\{ 1 + h P_\odot I^\odot + \frac{1}{\sqrt{2}} P_T [P_x \cos \phi - P_y \sin \phi + h P_\odot (P_x^\odot \cos \phi - P_y^\odot \sin \phi)] \right\}, \quad (1)$$

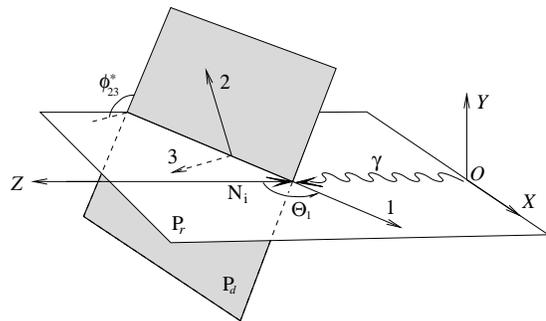


FIG. 1: Definition of the coordinate systems used in the present work. The azimuthal angle ϕ_{23}^* is defined in the center-of-mass system (cm) system of particles 2 and 3 with the z axis opposite to the momentum of particle 1 and y axis parallel to OY . It is equal to the angle between the reaction plane P_r and the decay plane P_d .

TABLE I: Polarization observables measured in the present work. Notations from Ref. [14] are used.

Beam	Target	
	x	y
–	P_x	P_y
c	P_x^\odot	P_y^\odot

where P_\odot and P_T denote the degree of circular beam and transverse target polarization, $h = \pm 1$ is the beam helicity, and ϕ is the azimuthal angle of the target polarization vector in a coordinate frame fixed to the reaction plane. The unpolarized differential cross section is denoted as σ_0 . The circular photon asymmetry I^\odot has already been discussed in detail in Ref. [6]. For the asymmetries we have used the notation of Ref. [14]. As is evident from Eq. (1), for the totally exclusive fivefold cross section there are two independent transverse target asymmetries (P_x and P_y) and two independent beam-target asymmetries (P_x^\odot and P_y^\odot). Table I schematically explains how these asymmetries are separated by a proper variation of the photon and proton polarization parameters. The observables P_y and P_x^\odot are equivalent to the T and F asymmetries in single pseudoscalar meson photoproduction.

III. MODEL

For the interpretation of our results we adopted an isobar model approach as used, for example, for double pion photoproduction in Refs. [16–20]. The main ingredients are described in detail in Refs. [4, 5]. Here we limit ourselves to a brief overview needed for the discussion below.

The reaction amplitude T contains background and

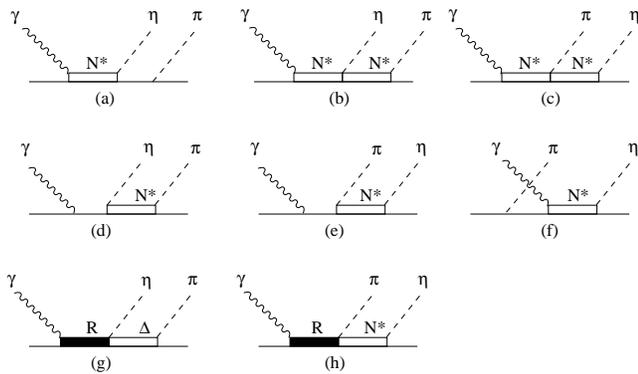


FIG. 2: Diagrams representing the amplitude for the $\gamma N \rightarrow \pi\eta N$. The notations Δ and N^* are used for the resonances $\Delta(1232)$ and $S_{11}(1535)$.

resonance terms

$$T = T^B + \sum_{R(J^\pi; I)} T^R, \quad (2)$$

where each resonance state $R(J^\pi; I)$ is determined by spin-parity J^π and isospin I .

The resonance sector [diagrams (g) and (h) in Fig. 2] includes only the states with isospin $I = 3/2$. As already noted, analysis of the existing data for $\gamma p \rightarrow \pi^0 \eta p$ is in general agreement with the assumption that in the energy region $E_\gamma < 1.4$ GeV the reaction is dominated by the D_{33} partial wave. In the present model, the latter is populated by the $\Delta(1700)3/2^-$ and $\Delta(1940)3/2^-$ states. The resonance $\Delta(1940)3/2^-$ was introduced into the reaction $\gamma p \rightarrow \pi^0 \eta p$ in Ref. [2]. In Ref. [5] it was needed in order to maintain the importance of the D_{33} wave at energies above 1.3 GeV, which otherwise would rapidly decrease with increasing energy. Other $I = 3/2$ resonances entering the amplitude are $\Delta(1750)P_{31}$, $\Delta(1920)P_{33}$, $\Delta(1600)P_{33}$, and $\Delta(1905)F_{35}$.

According to the isobar model concept, each resonance state $R(J^\pi; T)$ generates the final $\pi\eta N$ state via intermediate transitions to $\eta\Delta(1232)$ and $\pi S_{11}(1535)$ configurations. In this respect the resonance terms T^R in (2) are given by a coherent sum of two amplitudes,

$$T^R = T^{(\eta\Delta)} + T^{(\pi N^*)}, \quad (3)$$

where the isobars $\Delta(1232)$ and $S_{11}(1535)$ are denoted as Δ and N^* , respectively. Each term in (3) has the form

$$T^{(\alpha)} = A_\lambda G_R(W) f^{(\alpha)}(W, \vec{q}_\pi, \vec{q}_\eta, \vec{p}_N), \quad (4)$$

$$\alpha = \eta\Delta, \pi N^*.$$

with W being the total center-of-mass energy. The quantities A_λ are helicity functions determining the transition $\gamma N \rightarrow R$. The propagators G_R were calculated in the nonrelativistic form

$$G_R(W) = \frac{1}{W - M_R + \frac{i}{2}\Gamma(W)}. \quad (5)$$

The total energy dependent width Γ is a sum of the partial decay widths in πN , $\eta\Delta$ and πN^* channels:

$$\Gamma = \Gamma_{\pi N} + \Gamma_{\pi\eta N}^{(\eta\Delta)} + \Gamma_{\pi\eta N}^{(\pi N^*)}. \quad (6)$$

The latter two, $\Gamma_{\pi\eta N}^{(\eta\Delta)}$ and $\Gamma_{\pi\eta N}^{(\pi N^*)}$, were calculated with explicit inclusion of the finite widths of the Δ and N^* isobars. Finally, the functions $f^{(\alpha)}$ in Eq.(4) depending on the three-momenta of the final particles describe decays of the resonances into the final $\pi\eta N$ state. As adjustable parameters the Breit-Wigner masses M_R , as well as the products $\sqrt{\Gamma_{\pi\eta N}^{(\alpha)}} A_\lambda$ ($\alpha = \eta\Delta, \pi N^*$), were used in [5]. The total widths of resonances were not varied. The closeness of the resonances to the $\pi\eta$ production threshold, especially of $\Delta(1700)D_{33}$, results in rather weak sensitivity of the cross section to their widths. Therefore the values of the total widths at the resonance position $\Gamma(M_R)$ were taken directly from the Particle Data Group (PDG) compilation [21] or from the references cited there. For the same reason, the masses of the resonances, rated by four or three stars, were varied around their PDG values.

The slowly varying background T^B is presented in Fig.2 by the diagrams (a) to (f). Only those diagrams were taken into account whose contribution is appreciable. We have omitted, for example, the terms with Δ and N^* isobars in the u channel. The diagrams (b) and (c) contain the unknown coupling constants in the $\pi N^* N^*$ and $\eta N^* N^*$ vertices. Since the corresponding terms have rather small impact on the calculation results, these constants were not treated as adjustable parameters and just for simplicity were fixed according to the prescription

$$f_{\pi N^* N^*} = f_{\pi N N}, \quad f_{\eta N^* N^*} = f_{\eta N N}. \quad (7)$$

As the direct calculation in [1, 4, 5] shows, the background terms do not contribute significantly to the cross section. The $\pi\eta$ system is assumed not to resonate in the energy region considered. The validity of this assumption is confirmed by the results of Ref. [2] where the contribution of the resonance $a_0(980)$ at energies $E_\gamma < 1.4$ GeV is shown to be less than 1%. Furthermore, the model does not contain relative phases in the electromagnetic couplings which are sometimes used in the multipole analyses. Although these phases allow one to make the phenomenological formulation more flexible, their inclusion leads to unnecessary increase of the number of adjustable parameters.

IV. EXPERIMENTAL SETUP

The experiment was performed at the MAMI C accelerator in Mainz [22] using the Glasgow-Mainz tagged photon facility [23]. Bremsstrahlung photons were produced by scattering a longitudinally polarized electron beam with an energy of 1557 MeV and a polarization degree of 80% on a 10- μm -thick copper radiator. The

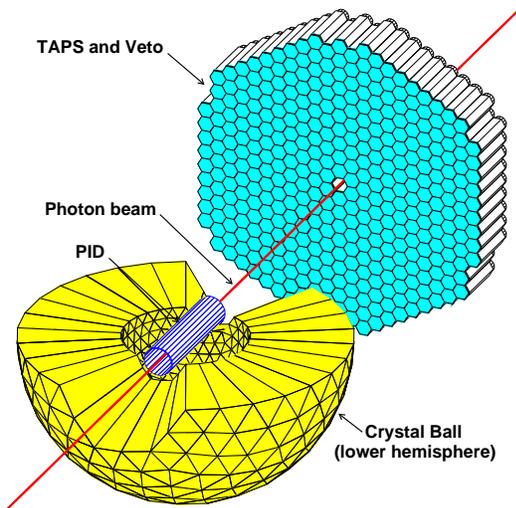


FIG. 3: (Color online) Experimental setup with the upper hemisphere of the Crystal Ball omitted to show the central region.

photons are energy tagged by momentum analysis of the scattered electrons in the dipole magnet spectrometer. The resulting energy-tagged photon beam covered an energy range from 450 to 1450 MeV with an average resolution of 4 MeV. The polarization degree of the electron beam was measured periodically using Mott scattering at the laser-driven source. The beam helicity was switched randomly, with a frequency of 1 Hz, during the experiment and the orientation of the polarization vector at the radiator position was checked using Moeller scattering. In the Bremsstrahlung process, the longitudinal polarization of the electrons is transferred to the circular polarization of the emitted photons [24]. The degree of circular photon polarization P_{\odot} depends on the photon energy and varied from 67% at 1050 MeV to 79% at 1450 MeV.

The reaction $\gamma p \rightarrow \pi^0 \eta p$ was measured using the Crystal Ball (CB) central spectrometer [25] with TAPS [26] as a forward angle spectrometer. The full detector setup is shown schematically in Fig. 3. The spherical CB detector consisted of 672 optically insulated NaI(Tl) crystals with a thickness of 15.7 radiation lengths pointing towards the center of the sphere. The crystals were arranged in two hemispheres covering 93% of the full solid angle. Electromagnetic showers were reconstructed with an energy resolution of $\Delta E/E = 1.7\%$ at 1 GeV. Shower directions were measured with a resolution of $\sigma_{\theta} \approx 2 - 3^{\circ}$ in the polar and $\sigma_{\phi} \approx 2^{\circ}/\sin\theta$ in the azimuthal angle. For charged-particle identification via differential energy loss, a barrel of 24 thin scintillation detectors surrounding the target was used [27]. The forward angular range $\theta = 1 - 20^{\circ}$ was covered by the TAPS calorimeter [26], arranged as a planar configuration of 384 hexagonally shaped BaF₂ detectors. Each detector had an inner diameter of 5.9 cm and was 25 cm long,

which corresponds to 12 radiation lengths. The resolutions for the reconstruction of electromagnetic showers, were $\sigma/E_{\gamma} = 0.0079/(E_{\gamma}/\text{GeV})^{0.5} + 0.018$ for the energy and $\sim 1^{\circ}$ for the direction. A 5-mm thick plastic scintillator in front of each module allows the separation of neutral and charged particles. Photons (or electrons) and hadrons can be separated by a pulse-shape analysis based on the properties of BaF₂. The crystals have the fast and long components of the scintillation, the intensity of which depends on the incident particle nature. Analysis of these components gives us an additional method of particle identification. The best way to identify the charged particle species in TAPS is a time-of-flight versus cluster energy analysis. The solid angle of the combined Crystal Ball and TAPS detection system is nearly 97% of 4π sr.

The transversely polarized target protons were provided by a frozen-spin butanol (C₄H₉OH) target [28]. A four-layer saddle coil provided a 0.45 T holding field perpendicular to the beam axis at a current of 35 A. A ³He/⁴He dilution refrigerator keeps the target material at a temperature of 25 mK which corresponds to relaxations times of 1500 h. The 2-cm-long and 2-cm-diameter cylindrical target cell was filled with 2-mm-diameter butanol spheres with a packing fraction (filling factor) of $\sim 60\%$. The target polarization was measured using the NMR techniques at the beginning and the end of each data taking period. The polarization was then calculated for each individual data file from the known exponential relaxation of the polarization. In order to reduce the systematic uncertainties, the direction of the target polarization vector was regularly reversed during the experiment. The average degree of polarization during the beam periods May-June 2010 and April 2011 was 70%.

V. DATA ANALYSIS

The reconstruction of the $\gamma p \rightarrow \pi^0 \eta p$ reaction is based on the two photon decays of the π^0 and the η meson as described in detail in Ref. [29]. As a first step, events with four neutral and one or zero charged particles in the Crystal Ball and TAPS detectors were selected. The distribution of invariant masses, calculated from all possible combinations of the four neutral hits is shown in Fig. 4. As there are three independent combinations of possible pairs, this histogram has three entries per event. The distribution shows already large peak corresponding to the $\pi^0 \pi^0$ channel and two smaller ones from the $\pi^0 \eta$ final state. In the next step, a χ^2 for both possible final states, $\pi^0 \pi^0$ and $\pi^0 \eta$, was calculated for each possible permutation of the four neutral hits:

$$\chi_{2\pi}^2 = \left(\frac{M_{\gamma_i \gamma_j} - m_{\pi^0}}{\sigma_{\pi^0}} \right)^2 + \left(\frac{M_{\gamma_k \gamma_l} - m_{\pi^0}(m_{\eta})}{\sigma_{\pi^0}(\sigma_{\eta})} \right)^2 \quad (8)$$

Here m_{π^0} and m_{η} are π^0 and η masses and $\sigma_{\pi^0} = 10$ MeV and $\sigma_{\eta} = 25$ MeV are the corresponding invariant mass

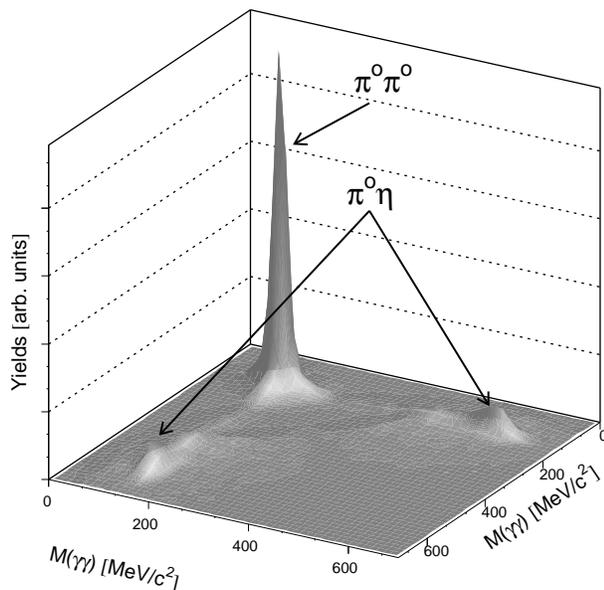


FIG. 4: Event selection for final states with four photons: $M_{\gamma\gamma}$ vs $M_{\gamma\gamma}$ for all possible independent combinations of $\gamma\gamma$ pairs (three entries for each event).

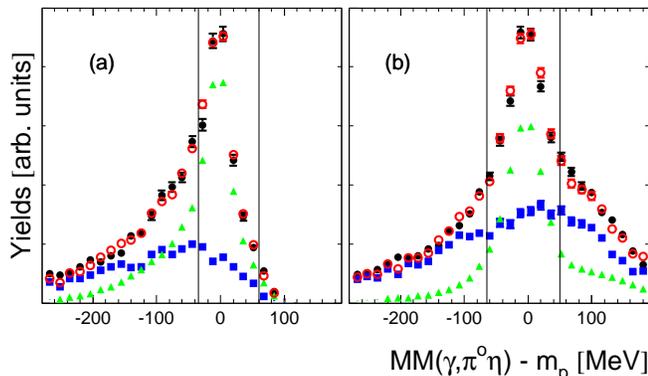


FIG. 5: (Color online) Missing mass distributions corresponding to photon beam energies of (a) 1100 MeV and (b) 1400 MeV. The full black circles are obtained with butanol data. The green triangles and blue squares are hydrogen and carbon data scaled to fit the butanol data. The fit result, which is a sum of the hydrogen and carbon partial contributions, is shown by the open red circles.

resolutions of the detector system. Each event was then assigned to either $\pi^0\pi^0$ or $\pi^0\eta$ production depending on the minimum of the χ^2 values. Further selection is based on selections in the invariant $M(\gamma\gamma)$ mass distributions and the $MM(\gamma, \pi^0\eta)$ missing mass calculated with the assumption of a γp initial state and the reconstructed $\pi^0\eta$ pair.

In principle, the polarization observables in Eq. (1) can be determined in each photon energy, angular or invariant mass M_{23} bin as count rate asymmetries from

the number N^\pm of reconstructed $\vec{\gamma}\vec{p} \rightarrow \pi^0\eta p$ events with different orientations of target spin and beam helicity:

$$P_x = \frac{1}{P_T |\cos \phi|} \frac{N^{\pi=+1} - N^{\pi=-1}}{N^{\pi=+1} + N^{\pi=-1}}, \quad (9)$$

$$P_y = \frac{1}{P_T |\sin \phi|} \frac{N^{\pi=+1} - N^{\pi=-1}}{N^{\pi=+1} + N^{\pi=-1}}, \quad (10)$$

$$P_x^\odot = \frac{1}{P_T |\cos \phi|} \frac{1}{P_\odot} \frac{N^{\sigma=+1} - N^{\sigma=-1}}{N^{\sigma=+1} + N^{\sigma=-1}}, \quad (11)$$

$$P_y^\odot = \frac{1}{P_T |\sin \phi|} \frac{1}{P_\odot} \frac{N^{\sigma=+1} - N^{\sigma=-1}}{N^{\sigma=+1} + N^{\sigma=-1}}, \quad (12)$$

where $\pi = \vec{p}_T \cdot \hat{y} / |\vec{p}_T \cdot \hat{y}| = \pm 1$ denotes the orientation of the target polarization vector \vec{p}_T relative to the normal of the production plane and $\sigma = h \vec{p}_T \cdot \hat{x} / |\vec{p}_T \cdot \hat{x}| = \pm 1$ is given by the product of the beam helicity h and the orientation of \vec{p}_T relative to the x axis. In these asymmetries, systematic uncertainties related to the total photon flux normalization and the target filling factor cancel. However, using a butanol target has one essential disadvantage due to additional background from reactions on ^{12}C and ^{16}O nuclei. In the numerators of Eqs. (9)-(12), this background cancels because the nucleons bound in ^{12}C or ^{16}O are unpolarized. However, in order to determine the denominator, this contribution has to be taken into account. The detection of the outgoing protons and applying kinematic constraints already suppress this background significantly. In order to subtract the remaining background we analyzed $\pi^0\eta$ photoproduction on pure carbon and liquid hydrogen targets. The corresponding $MM(\gamma, \pi^0\eta)$ distributions were scaled and added in order to fit the corresponding distribution obtained with the butanol target. Since the magnitude and the shape of the background depend on the initial beam energy and on the momenta of the final particles, this procedure was performed for each individual kinematical bin. This subtraction method is illustrated on Fig. 5 for two photon energies, which are typical for the presented data analysis. Missing mass spectra for the reaction $\gamma p \rightarrow \pi^0\eta p$ with the butanol target are shown by the full black circles. Spectra measured with the hydrogen and carbon targets are represented by the green triangles and the blue squares respectively. Their absolute values were scaled to fit the butanol data. The red open circles represent the sum of the fitted hydrogen and carbon contributions. For further analysis only events around the proton peak, within the vertical lines, are used. The intervals were selected to optimize the signal-to-background ratio. Even in the distribution from the pure hydrogen (green triangles in Fig. 5 still some background remains. This is mainly due to misidentified $\gamma p \rightarrow \pi^0\pi^0 p$ reactions, split or overlapping photon clusters, and combinatoric mixing. This background is subtracted by fitting the missing mass distributions with the sum of a Gaussian and a third-order

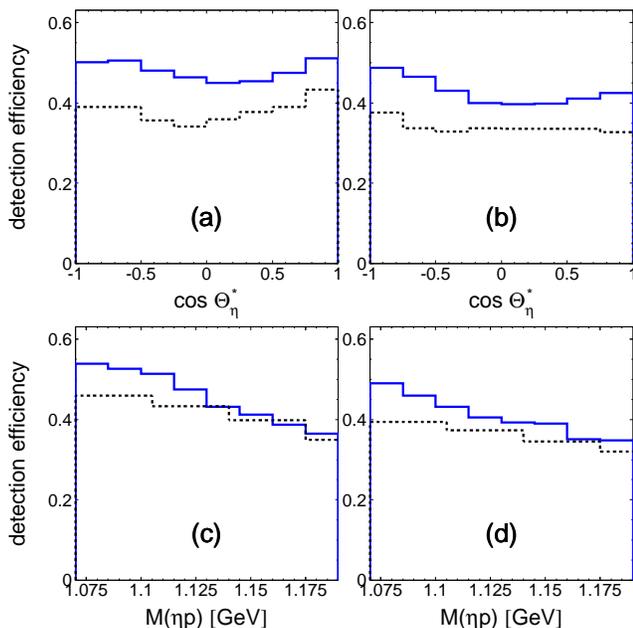


FIG. 6: (Color online) Detection efficiency at fixed Θ_π for two photon energy bins: 1100 ± 50 MeV (solid blue line) and 1400 ± 50 MeV (black dashed line). Θ_η^* is the polar angle in the cm system of the (ηp) pair. Panels (a) and (c) show the efficiency at $\cos \Theta_\pi = -0.9 \pm 0.1$, and (b) and (d) at $\cos \Theta_\pi = 0.9 \pm 0.1$.

polynomial function. After subtracting the polynomial background, the distribution is found to be in excellent agreement with results of a Monte Carlo simulation of the $\gamma p \rightarrow \pi^0 \eta p$ reaction (see Fig. 4 in Ref. [29]). The average detection efficiency for the $\gamma p \rightarrow \pi \eta p$ reaction after all analysis steps is about 50% for beam energies from 1.05 to 1.45 GeV.

The asymmetries in each photon energy, angular or invariant mass M_{23} bin were obtained as count rate asymmetries by integrating the reaction yields in Eqs. (9)-(12) over four remaining variables. This procedure is exactly valid if the acceptance does not depend on any of these variables. However, a small and smooth variation of the acceptance can be taken into account in the systematic uncertainties. Figure 6 shows as an example the efficiency as function of those kinematic variables where the strongest variation of the acceptance is observed. The typical variation is less than 3%. The influence of the acceptance variations and background subtraction on the asymmetries was estimated by varying the applied selection criteria. The observed changes in the asymmetries by 3%-6% were smaller than the statistical uncertainty. Other systematic uncertainties of the present measurement are related to the determination of the proton polarization (4%) and the beam polarization (2%). By adding all contributions in quadrature, a total systematic uncertainty of less than 8% was obtained.

VI. DISCUSSION OF THE RESULTS

Figures 7, 8, and 9 show the measured asymmetries as function of the various scattering angles and invariant mass combinations. Data from the $\pi + (\eta p)$ analysis are shown in columns 1 and 4. The $\eta + (\pi p)$ and $p + (\pi \eta)$ data are shown in columns 2 and 5 and in columns 3 and 6, respectively. In this section we present a qualitative description of the reaction properties revealed by our data. A detailed partial wave analysis of the new data has started and will be published elsewhere.

As one can see in Figs. 7 and 8, both P_y and P_x^\odot have rather small values, except for $P_x^\odot(\cos \Theta_\pi)$ which strongly varies with pion angle (see first column in Fig. 8). This dependence can be described to a good approximation by an odd function with a maximum amplitude of about 0.8. This peculiar behavior is a direct signature of s -wave production of the $\eta\Delta$ configuration in the $J^\pi = 3/2^-$ state. As noted in Sec. I this partial wave appears to dominate the reaction amplitude in a wide energy region from threshold to $E_\gamma = 1.5$ GeV [3, 5]. Assuming that the reaction proceeds exclusively via the formation of an intermediate $\eta\Delta$ pair in the $3/2^-$ partial wave, one obtains the following simple form for P_x^\odot in the region of $\Delta(1700)D_{33}$:

$$P_x^\odot \approx -\frac{2}{\sqrt{3}} \frac{A_{1/2} A_{3/2} \sin 2\Theta_\pi}{A_{1/2}^2 (1/3 + \cos^2 \Theta_\pi) + A_{3/2}^2 \sin^2 \Theta_\pi}, \quad (13)$$

where A_λ ($\lambda = 1/2, 3/2$) are the helicity amplitudes for the transition $\gamma N \rightarrow \Delta(1700)D_{33}$. If we further assume that $A_{1/2} \approx A_{3/2}$ [21] Eq. (13) reduces to the simpler approximation

$$P_x^\odot \approx -\frac{\sqrt{3}}{2} \sin 2\Theta_\pi. \quad (14)$$

The function (14) reaches its maximum value $P_x^\odot = \sqrt{3}/2$ at $\cos \Theta_\pi = -1/\sqrt{2}$, in general agreement with our data (see red dotted lines in the first column in Fig. 8).

It is also worth noting that, in the same s -wave hypothesis of $\eta\Delta$ production, the behavior of $P_x^\odot(\cos \Theta_\pi)$ should be similar (up to the possible change of sign) to that of the observable F for single π^0 photoproduction in the Δ resonance region. Indeed, assuming that the $\Delta(1232)$ excitation is a pure magnetic dipole transition the distribution $F(\cos \Theta)$ has the form

$$F \approx \frac{3 \sin 2\Theta}{5 - 3 \cos^2 \Theta}, \quad (15)$$

so that, as in the case of P_x^\odot [see Eq. (13)], the angular dependence of F is mainly governed by the factor $\sin 2\Theta$.

Concerning the role of positive parity states, two important facts can be observed. First, the dependence of P_y and P_x^\odot on the invariant mass M_{23} is determined exclusively by an interference of partial wave amplitudes with opposite parities. The simple model with only the $\Delta 3/2^-$ amplitude therefore gives the trivial result

$$d\mathcal{O}/dM_{23} = 0, \quad \mathcal{O} = \{P_y, P_x^\odot\}. \quad (16)$$

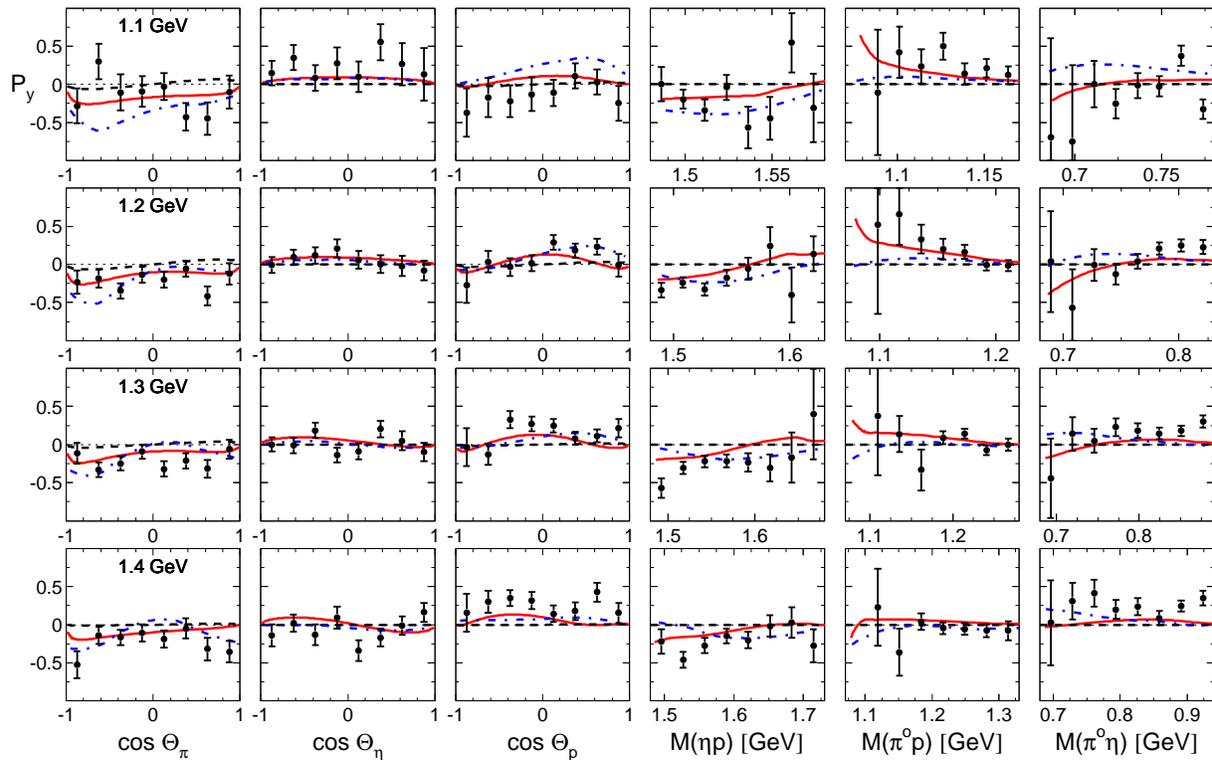


FIG. 7: (Color online) Angular and invariant mass distributions for the target asymmetry P_y of the $\gamma p \rightarrow \pi^0 \eta p$ reaction for incident photon energies from 1050 to 1450 MeV. Our experimental results with statistical uncertainties are shown by filled circles. The solid curves show the prediction of the isobar model [5]. The dashed curves include only the $3/2^-$ partial wave. Predictions of the Bonn-Gatchina model [7] are shown by dashed-dotted curves. The energy labels on the left panels indicate the central energy of the four 100-MeV-wide photon energy bins.

Second, if only the dominant $\Delta 3/2^-$ wave is included, both P_y and P_x° are odd functions of $\Theta_1 - \pi/2$

$$\mathcal{O}(-\cos \Theta_1) = -\mathcal{O}(\cos \Theta_1), \quad \mathcal{O} = \{P_x, P_y^\circ\}, \quad (17)$$

and reach zero at $\Theta_1 = \pi/2$. In this respect, the nonzero values of P_y and P_x° at $\Theta_1 = \pi/2$ as well as of their distribution over the invariant mass M_{23} may be viewed as a signature of the presence of partial waves with positive parity. However, as evident from Figs. 7 and 8 the deviation of the measured values from the simple rules (16) and (17) is small, indicating that the role of states besides $\Delta 3/2^-$ is not large. This is in full agreement with our previous results for the unpolarized angular distribution [8] as well as for the helicity beam asymmetry [6].

The solid lines in Figs. 7-9 show the prediction of the isobar model described in Sec. III. Here we use the parameter set (I) (see Table I in Ref. [5]) which was preferred since it gives the best description of the measured linear beam asymmetry Σ [10, 11]. This solution also reproduces the invariant mass distributions measured in [10] (see Fig. 9 in Ref. [5]) and describes reasonably well the data for the beam asymmetries I° , I^c and I^s presented in Refs. [6, 12].

The dash-dotted lines in Figs. 7 and 8 show predictions of the Bonn-Gatchina multichannel fit [7] (solution

BG2011-02). In contrast to [5], where only the data for $\gamma p \rightarrow \pi^0 \eta p$ were fitted, within the Bonn-Gatchina approach, the positions of resonances, their partial decay widths, and relative strengths were fitted simultaneously to the data sets in different channels, including single and double meson production as well as strangeness production. The application to the reaction $\gamma p \rightarrow \pi^0 \eta p$ is described in detail in Ref. [2]. In this analysis some contributions from N^* resonances, which do not enter the amplitude in [5], in particular the $N(1880)P_{11}$, are also included.

Both models describe the new data equally well. The present statistics do not allow any discrimination between the different model predictions in kinematic regions where they show small differences, e.g., at low values of $M(\pi^0 p)$.

The other two observables P_x and P_y° contribute exclusively to the distribution of the cross section over the azimuthal angle ϕ_{23}^* and vanish in the distribution over Θ_1 and M_{23} . In Fig. 9 we show data for the particle selection $1 + (23) = p + (\pi^0 \eta)$. As in Ref. [6] the denominators of the asymmetries are averaged over the whole $\phi_{\pi\eta}^*$ region. Parity conservation requires

$$\mathcal{O}(\phi_{23}^*) = -\mathcal{O}(2\pi - \phi_{23}^*), \quad \mathcal{O} = \{P_x, P_y^\circ\}. \quad (18)$$

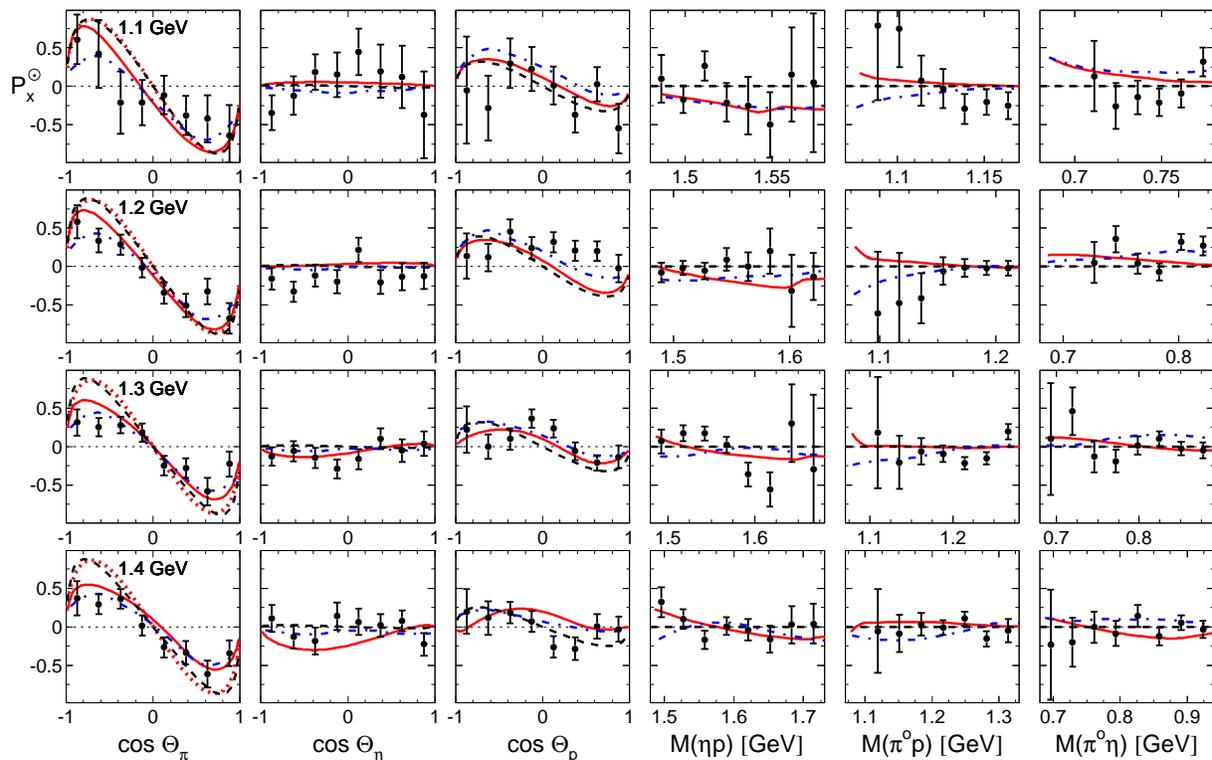


FIG. 8: (Color online) Same as Fig. 7 for the beam-target asymmetry P_x^{\odot} . The red dotted line in the first column was obtained using Eq. (7).

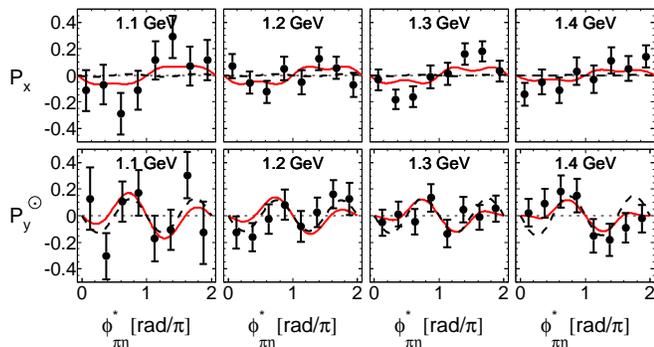


FIG. 9: (Color online) The target asymmetry P_x and beam-target asymmetry P_y^{\odot} as functions of $\phi_{\pi\eta}^*$. All notation is the same as in Fig. 7.

Using angular momentum algebra it can be shown that if only the states with $J^P = 3/2^-$ enter the amplitude (in our case $\Delta 3/2^-$ resonances) the product $\mathcal{O}d\sigma_0/d\phi_{23}^*$, for both $\mathcal{O} = P_x$ and $\mathcal{O} = P_y^{\odot}$, is proportional to $\sin 2\phi_{\pi\eta}^*$ and does not contain higher order harmonics. The presence of states with positive parity leads to a more complicated shape for these observables, as observed in our data.

VII. SUMMARY AND CONCLUSIONS

We have presented the first experimental results for the target and the beam-target asymmetries of the $\gamma p \rightarrow \pi^0 \eta p$ cross section obtained with circularly polarized photons and transversely polarized protons. The measurements were performed using Crystal Ball and TAPS spectrometers. We presented a qualitative analysis which shows that the new data for all four observables are in broad agreement with the dominance of the $\Delta 3/2^-$ amplitude, confirming the theoretical interpretation of previous measurements [6, 8] and other analyses [2, 5], in the region below $E_{\gamma} = 1.5$ GeV. However, the detailed distributions of the measured observables are sensitive to the contribution of small components in the reaction amplitude. Specifically an interference between $\Delta 3/2^-$ and the positive parity amplitudes $\Delta 1/2^+$ and $\Delta 3/2^+$ is responsible for the nontrivial angular and energy dependence of the asymmetries presented.

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