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Combined Measurement of the Higgs Boson Mass in pp Collisions at $\sqrt{s} = 7$ and 8 TeV with the ATLAS and CMS Experiments

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A measurement of the Higgs boson mass is presented based on the combined data samples of the ATLAS and CMS experiments at the CERN LHC in the $H \to \gamma\gamma$ and $H \to ZZ \to 4\ell$ decay channels. The results are obtained from a simultaneous fit to the reconstructed invariant mass peaks in the two channels and for the two experiments. The measured masses from the individual channels and the two experiments are found to be consistent among themselves. The combined measured mass of the Higgs boson is $m_H = 125.09 \pm 0.21$ (stat) $\pm 0.11$ (syst) GeV.

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The study of the mechanism of electroweak symmetry breaking is one of the principal goals of the CERN LHC program. In the standard model (SM), this symmetry breaking is achieved through the introduction of a complex doublet scalar field, leading to the prediction of the Higgs boson $H$ [1–6], whose mass $m_H$ is, however, not predicted by the theory. In 2012, the ATLAS and CMS Collaborations at the LHC announced the discovery of a particle with Higgs-boson-like properties and a mass of about 125 GeV [7–9]. The discovery was based primarily on mass peaks observed in the $\gamma\gamma$ and $ZZ \to \ell^+\ell^-\ell'^+\ell'^-$ (denoted $H \to ZZ \to 4\ell$ for simplicity) decay channels, where one or both of the $Z$ bosons can be off shell and where $\ell$ and $\ell'$ denote an electron or muon. With $m_H$ known, all properties of the SM Higgs boson, such as its production cross section and partial decay widths, can be predicted. Increasingly precise measurements [10–13] have established that all observed properties of the new particle, including its spin, parity, and coupling strengths to SM particles are consistent within the uncertainties with those expected for the SM Higgs boson.

The ATLAS and CMS Collaborations have independently measured $m_H$ using the samples of proton-proton collision data collected in 2011 and 2012, commonly referred to as LHC Run 1. The analyzed samples correspond to approximately 5 fb$^{-1}$ of integrated luminosity at $\sqrt{s} = 7$ TeV, and 20 fb$^{-1}$ at $\sqrt{s} = 8$ TeV, for each experiment. Combined results in the context of the separate experiments, as well as those in the individual channels, are presented in Refs. [12,14–16].

This Letter describes a combination of the Run 1 data from the two experiments, leading to improved precision for $m_H$. Besides its intrinsic importance as a fundamental parameter, improved knowledge of $m_H$ yields more precise predictions for the other Higgs boson properties. Furthermore, the combined mass measurement provides a first step towards combinations of other quantities, such as the couplings. In the SM, $m_H$ is related to the values of the masses of the $W$ boson and top quark through loop-induced effects. Taking into account other measured SM quantities, the comparison of the measurements of the Higgs boson, $W$ boson, and top quark masses can be used to directly test the consistency of the SM [17] and thus to search for evidence of physics beyond the SM.

The combination is performed using only the $H \to \gamma\gamma$ and $H \to ZZ \to 4\ell$ decay channels, because these two channels offer the best mass resolution. Interference between the Higgs boson signal and the continuum background is expected to produce a downward shift of the signal peak relative to the true value of $m_H$. The overall effect in the $H \to \gamma\gamma$ channel [18–20] is expected to be a few tens of MeV for a Higgs boson with a width near the SM value, which is small compared to the current precision. The effect in the $H \to ZZ \to 4\ell$ channel is expected to be much smaller [21]. The effects of the interference on the mass spectra are neglected in this Letter.

The ATLAS and CMS detectors [22,23] are designed to precisely reconstruct charged leptons, photons, hadronic jets, and the imbalance of momentum transverse to the direction of the beams. The two detectors are based on different technologies requiring different reconstruction and calibration methods. Consequently, they are subject to different sources of systematic uncertainty.

The $H \to \gamma\gamma$ channel is characterized by a narrow resonant signal peak containing several hundred events per experiment above a large falling continuum background. The overall signal-to-background ratio is a few...
percent. Both experiments divide the $H \rightarrow \gamma\gamma$ events into different categories depending on the signal purity and mass resolution, as a means to improve sensitivity. While CMS uses the same analysis procedure for the measurement of the Higgs boson mass and couplings [14], ATLAS implements separate analyses for the couplings [24] and for the mass [14]; the latter analysis classifies events in a manner that reduces the expected systematic uncertainties in $m_H$.

The $H \rightarrow ZZ \rightarrow 4\ell$ channel yields only a few tens of signal events per experiment, but has very little background, resulting in a signal-to-background ratio larger than 1. The events are analyzed separately depending on the flavor of the lepton pairs. To extract $m_H$, ATLAS employs a two-dimensional (2D) fit to the distribution of the four-lepton mass and a kinematic discriminant introduced to reject the main background, which arises from ZZ continuum production. The CMS procedure is based on a three-dimensional fit, utilizing the four-lepton mass distribution, a kinematic discriminant, and the estimated event-by-event uncertainty in the four-lepton mass. Both analyses are optimized for the mass measurement and neither attempts to distinguish between different Higgs boson production mechanisms.

There are only minor differences in the parametrizations used for the present combination compared to those used for the combination of the two channels by the individual experiments. These differences have almost no effect on the results.

The measurement of $m_H$, along with its uncertainty, is based on the maximization of profile-likelihood ratios $\Lambda(\alpha)$ in the asymptotic regime [25,26]:

$$\Lambda(\alpha) = \frac{L(\alpha, \hat{\theta}(\alpha))}{L(\hat{\alpha}, \hat{\theta})},$$

where $L$ represents the likelihood function, $\alpha$ the parameters of interest, and $\theta$ the nuisance parameters. There are three types of nuisance parameters: those corresponding to systematic uncertainties, the fitted parameters of the background models, and any unconstrained signal model parameters not relevant to the particular hypothesis under test. Systematic uncertainties are discussed below. The other two types of nuisance parameters are incorporated into the statistical uncertainty. The $\theta$ terms are profiled, i.e., for each possible value of a parameter of interest (e.g., $m_H$), all nuisance parameters are refitted to maximize $L$. The $\hat{\alpha}$ and $\hat{\theta}$ terms denote the unconditional maximum likelihood estimates of the best-fit values for the parameters, while $\hat{\theta}(\alpha)$ is the conditional maximum likelihood estimate for given parameter values $\alpha$.

The likelihood functions $L$ are constructed using signal and background probability density functions (PDFs) that depend on the discriminating variables: for the $H \rightarrow \gamma\gamma$ channel, the diphoton mass, and, for the $H \rightarrow ZZ \rightarrow 4\ell$ channel, the four-lepton mass (for CMS, also its uncertainty) and the kinematic discriminant. The signal PDFs are derived from samples of Monte Carlo (MC) simulated events. For the $H \rightarrow ZZ \rightarrow 4\ell$ channel, the background PDFs are determined using a combination of simulation and data control regions. For the $H \rightarrow \gamma\gamma$ channel, the background PDFs are obtained directly from the fit to the data. The profile-likelihood fits to the data are performed as a function of $m_H$ and the signal-strength scale factors defined below. The fitting framework is implemented independently by ATLAS and CMS, using the RooFit [27], RooStats [28], and HistFactory [29] data modeling and handling packages.

Despite the current agreement between the measured Higgs boson properties and the SM predictions, it is pertinent to perform a mass measurement that is as independent as possible of SM assumptions. For this purpose, three signal-strength scale factors are introduced and profiled in the fit, thus reducing the dependence of the results on assumptions about the Higgs boson couplings and about the variation of the production cross section ($\sigma$) times branching fraction (BF) with the mass. The signal strengths are defined as $\mu = (\sigma_{\text{expt}} \times \text{BF}_{\text{expt}})/(\sigma_{\text{SM}} \times \text{BF}_{\text{SM}})$, representing the ratio of the cross section times branching fraction in the experiment to the corresponding SM expectation for the different production and decay modes. Two factors, $\mu_{ggF+iH}$ and $\mu_{VBF+VH}$, are used to scale the signal strength in the $H \rightarrow \gamma\gamma$ channel. The production processes involving Higgs boson couplings to fermions, namely gluon fusion ($ggF$) and associated production with a top quark-antiquark pair ($t\bar{t}H$), are scaled with the $\mu_{ggF+iH}$ factor. The production processes involving couplings to vector bosons, namely vector boson fusion (VBF) and associated production with a vector boson ($VH$), are scaled with the $\mu_{VBF+VH}$ factor. The third factor $\mu^{d\ell}$ is used to scale the signal strength in the $H \rightarrow ZZ \rightarrow 4\ell$ channel. Only a single signal-strength parameter is used for $H \rightarrow ZZ \rightarrow 4\ell$ events because the $m_H$ measurement in this case is found to exhibit almost no sensitivity to the different production mechanisms.

The procedure based on the two scale factors $\mu_{ggF+iH}$ and $\mu_{VBF+VH}$ for the $H \rightarrow \gamma\gamma$ channel was previously employed by CMS [15] but not by ATLAS. Instead, ATLAS relied on a single $H \rightarrow \gamma\gamma$ signal-strength scale factor. The additional degree of freedom introduced by ATLAS for the present study results in a shift of about 40 MeV in the ATLAS $H \rightarrow \gamma\gamma$ result, leading to a shift of 20 MeV in the ATLAS combined mass measurement.

The individual signal strengths $\mu_{ggF+iH}$, $\mu_{VBF+VH}$, and $\mu^{d\ell}$ are assumed to be the same for ATLAS and CMS, and are profiled in the combined fit for $m_H$. The corresponding profile-likelihood ratio is

$$\Lambda(m_H) = \frac{\frac{L(m_H, \hat{\mu}_{ggF+iH}(m_H), \hat{\mu}_{VBF+VH}(m_H), \hat{\mu}^{d\ell}(m_H), \hat{\theta}(m_H))}{L(\hat{m}_H, \hat{\mu}_{ggF+iH}, \hat{\mu}_{VBF+VH}, \hat{\mu}^{d\ell}, \hat{\theta})}}.$$
Slightly more complex fit models are used, as described below, to perform additional compatibility tests between the different decay channels and between the results from ATLAS and CMS.

Combining the ATLAS and CMS data for the $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ \rightarrow 4\ell$ channels according to the above procedure, the mass of the Higgs boson is determined to be

$$m_H = 125.09 \pm 0.24 \text{ GeV}$$

$$= 125.09 \pm 0.21 \text{ (stat)} \pm 0.11 \text{ (syst) GeV.} \quad (3)$$

where the total uncertainty is obtained from the width of a negative log-likelihood ratio scan with all parameters profiled. The statistical uncertainty is determined by fixing all nuisance parameters to their best-fit values, except for the three signal-strength scale factors and the $H \rightarrow \gamma\gamma$ background function parameters, which are profiled. The systematic uncertainty is determined by subtracting in quadrature the statistical uncertainty from the total uncertainty. Equation (3) shows that the uncertainties in the $m_H$ measurement are dominated by the statistical term, even when the Run 1 data sets of ATLAS and CMS are combined. Figure 1 shows the negative log-likelihood ratio scans as a function of $m_H$, with all nuisance parameters profiled (solid curves), and with the nuisance parameters fixed to their best-fit values (dashed curves).

The signal strengths at the measured value of $m_H$ are found to be $\mu_{ggF+iH}^{\gamma\gamma} = 1.15^{+0.28}_{-0.25}$, $\mu_{VBF+VH}^{\gamma\gamma} = 1.17^{+0.58}_{-0.53}$, and $\mu^{4\ell} = 1.40^{+0.30}_{-0.25}$. The combined overall signal strength $\mu$ (with $\mu_{ggF+iH}^{\gamma\gamma} = \mu_{VBF+VH}^{\gamma\gamma} = \mu^{4\ell} \equiv \mu$) is $\mu = 1.24^{+0.18}_{-0.16}$.

The results reported here for the signal strengths are not expected to have the same sensitivity, nor exactly the same values, as those that would be extracted from a combined analysis optimized for the coupling measurements.

The combined ATLAS and CMS results for $m_H$ in the separate $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ \rightarrow 4\ell$ channels are

$$m_H^{\gamma\gamma} = 125.07 \pm 0.29 \text{ GeV}$$

$$= 125.07 \pm 0.25 \text{ (stat)} \pm 0.14 \text{ (syst) GeV} \quad (4)$$

and

$$m_H^{4\ell} = 125.15 \pm 0.40 \text{ GeV}$$

$$= 125.15 \pm 0.37 \text{ (stat)} \pm 0.15 \text{ (syst) GeV.} \quad (5)$$

The corresponding likelihood ratio scans are shown in Fig. 1. For the $H \rightarrow ZZ \rightarrow 4\ell$ channel, the systematic uncertainty is dominated by the absolute scale uncertainty in the momentum measurement for the muons and in the momentum and energy measurements for the electrons. Large samples (> $10^7$ events) of dilepton decays of the $J/\psi$, $\Upsilon(nS)$, and $Z$ resonances are used by both experiments to evaluate the absolute scales and to correct for residual misalignments in the inner tracker systems [14,16]. The systematic uncertainty in the ATLAS $m_H$ result from $H \rightarrow ZZ \rightarrow 4\ell$ decays was conservatively set to 60 MeV in Ref. [14] to account for the limited numerical precision in its estimate. A more precise procedure, resulting in a reduced systematic uncertainty of 40 MeV, is used here. For CMS, conservative systematic uncertainties of 0.1% for the $H \rightarrow ZZ \rightarrow 4\mu$ and $2\mu 2\ell$ channels, and 0.3% for the $H \rightarrow ZZ \rightarrow 4e$ channel, were obtained in Ref. [16] and are used here.

A summary of the results from the individual analyses and their combination is presented in Fig. 2.

The observed uncertainties in the combined measurement can be compared with expectations. The latter are evaluated by generating two Asimov data sets [26], where an Asimov data set is a representative event sample that provides both the median expectation for an experimental result and its expected statistical variation, in the asymptotic approximation, without the need for an extensive MC-based calculation. The first Asimov data set is a “prefit” sample, generated using $m_H = 125.0 \text{ GeV}$ and the SM predictions for the couplings, with all nuisance parameters fixed to their nominal values. The second Asimov data set is a “postfit” sample, in which $m_H$, the three signal strengths $\mu_{ggF+iH}^{\gamma\gamma}$, $\mu_{VBF+VH}^{\gamma\gamma}$, and $\mu^{4\ell}$, and all nuisance parameters are fixed to their best-fit values from the data. The expected uncertainties for the combined mass are

$$\delta m_{\text{prefit}} = \pm 0.24 \text{ GeV}$$

$$= \pm 0.22 \text{ (stat)} \pm 0.10 \text{ (syst) GeV} \quad (6)$$
Constraining all signal yields to their SM predictions results in an $m_H$ value that is about 70 MeV larger than the nominal result with a comparable uncertainty. The increase in the central value reflects the combined effect of the higher-than-expected $H \rightarrow ZZ \rightarrow 4\ell$ measured signal strength and the increase of the $H \rightarrow ZZ$ branching fraction with $m_H$. Thus, the fit assuming SM couplings forces the mass to a higher value in order to accommodate the value $\mu = 1$ expected in the SM.

Since the discovery, both experiments have improved their understanding of the electron, photon, and muon measurements [16,30–34], leading to a significant reduction of the systematic uncertainties in the mass measurement. Nevertheless, the treatment and understanding of systematic uncertainties is an important aspect of the individual measurements and their combination. The combined analysis incorporates approximately 300 nuisance parameters. Among these, approximately 100 are fitted parameters describing the shapes and normalizations of the background models in the $H \rightarrow \gamma\gamma$ channel, including a number of discrete parameters that allow the functional form in each of the CMS $H \rightarrow \gamma\gamma$ analysis categories to be changed [35]. Of the remaining almost 200 nuisance parameters, most correspond to experimental or theoretical systematic uncertainties.

Based on the results from the individual experiments, the dominant systematic uncertainties for the combined $m_H$ result are expected to be those associated with the energy or momentum scale and its resolution: for the photons in the $H \rightarrow \gamma\gamma$ channel and for the electrons and muons in the $H \rightarrow ZZ \rightarrow 4\ell$ channel [14–16]. These uncertainties are assumed to be uncorrelated between the two experiments since they are related to the specific characteristics of the detectors as well as to the calibration procedures, which are fully independent except for negligible effects due to the use of the common $Z$ boson mass [36] to specify the absolute energy and momentum scales. Other experimental systematic uncertainties [14–16] are similarly assumed to be uncorrelated between the two experiments. Uncertainties in the theoretical predictions and in the measured integrated luminosities are treated as fully and partially correlated, respectively.

To evaluate the relative importance of the different sources of systematic uncertainty, the nuisance parameters are grouped according to their correspondence to three broad classes of systematic uncertainty: (1) uncertainties in the energy or momentum scale and resolution for photons, electrons, and muons (“scale”), (2) theoretical uncertainties, e.g., uncertainties in the Higgs boson cross section and branching fractions, and in the normalization of SM background processes (“theory”), (3) other experimental uncertainties (“other”).

First, the total uncertainty is obtained from the full profile-likelihood scan, as explained above. Next, parameters associated with the scale terms are fixed and a new scan is performed. Then, in addition to the scale terms, the parameters associated with the theory terms are fixed and a scan performed. Finally, in addition, the other parameters are fixed and a scan performed. Thus the fits are performed iteratively, with the different classes of nuisance parameters cumulatively held fixed to their best-fit values. The uncertainties associated with the different classes of nuisance parameters are defined by the difference in quadrature.
The result in Eq. (8) is consistent with the values of \( m_H \) derived from the less precise WW and \( \tau \tau \) Higgs boson decay modes [37–40].

The relative importance of the various sources of systematic uncertainty is further investigated by dividing the nuisance parameters into yet-finer groups, with each group associated with a specific underlying effect, and evaluating the impact of each group on the overall mass uncertainty. The matching of nuisance parameters to an effect is not strictly rigorous because nuisance parameters in the two experiments do not always represent exactly the same effect and in some cases multiple effects are related to the same nuisance parameter. Nevertheless, the relative impact of the different effects can be explored. A few experiment-specific groups of nuisance parameters are defined. For example, ATLAS includes a group of nuisance parameters to account for the inaccuracy of the background modeling for the \( H \rightarrow \gamma \gamma \) channel. To model this background, ATLAS uses specific analytic functions in each category [14] while CMS simultaneously considers different background parametrizations [35]. The systematic uncertainty in \( m_H \) related to the background modeling in CMS is estimated to be negligible [15].

The impact of groups of nuisance parameters is evaluated starting from the contribution of each individual nuisance parameter to the total uncertainty. This contribution is defined as the mass shift \( \delta m_H \) observed when reevaluating the profile-likelihood ratio after fixing the nuisance parameter in question to its best-fit value increased or decreased by 1 standard deviation (\( \sigma \)) in its distribution. For a nuisance parameter whose PDF is a Gaussian distribution, this shift corresponds to the contribution of that particular nuisance parameter to the final uncertainty. The impact of a group of nuisance parameters is estimated by summing in quadrature the contributions from the individual parameters.

The impacts \( \delta m_H \) due to each of the considered effects are listed in Table I. The results are reported for the four individual channels, both for the data and (in parentheses) the prefit Asimov data set. The row labeled “Systematic uncertainty (sum in quadrature)” shows the total sums in quadrature of the individual terms in the table. The row labeled “Systematic uncertainty (nominal)” shows the corresponding total systematic uncertainties derived using the subtraction in quadrature method discussed in connection with Eq. (3). The two methods to evaluate the total systematic uncertainty are seen to agree within 10 MeV, which is comparable with the precision of the estimates. The two rightmost columns of Table I list the contribution of each group of nuisance parameters to the uncertainties in the combined mass measurement, for ATLAS and CMS separately.

The statistical and total uncertainties are summarized in the bottom section of Table I. Since the weight of a channel in the final combination is determined by the inverse of the squared uncertainty, the approximate relative weights for the combined result are 19% (\( H \rightarrow \gamma \gamma \)) and 18% (\( H \rightarrow ZZ \rightarrow 4\ell \)) for ATLAS, and 40% (\( H \rightarrow \gamma \gamma \)) and 23% (\( H \rightarrow ZZ \rightarrow 4\ell \)) for CMS. These weights are reported in the last row of Table I, along with the expected values.

Figure 3 presents the impact of each group of nuisance parameters on the total systematic uncertainty in the mass measurement of ATLAS, CMS, and the combination. For the individual ATLAS and CMS measurements, the results in Fig. 3 are approximately equivalent to the sum in quadrature of the respective \( \delta m_H \) terms in Table I multiplied by their analysis weights, after normalizing these weights to correspond to either ATLAS only or CMS only. The ATLAS and CMS combined results in Fig. 3 are the sum in quadrature of the combined results in Table I.

The results in Table I and Fig. 3 establish that the largest systematic effects for the mass uncertainty are those related to the determination of the energy scale of the photons, followed by those associated with the determination of the electron and muon momentum scales. Since the CMS \( H \rightarrow \gamma \gamma \) channel has the largest weight in the combination, its impact on the systematic uncertainty of the combined result is largest.

The mutual compatibility of the \( m_H \) results from the four individual channels is tested using a likelihood ratio with four masses in the numerator and a common mass in the denominator, and thus three degrees of freedom. The three signal strengths are profiled in both the numerator and denominator as in Eq. (1). The resulting compatibility, defined as the asymptotic \( p \) value of the fit, is 10%. Allowing the ATLAS and CMS signal strengths to vary independently yields a compatibility of 7%. This latter fit results in an \( m_H \) value that is 40 MeV larger than the nominal result.

The compatibility of the combined ATLAS and CMS mass measurement in the \( H \rightarrow \gamma \gamma \) channel with the combined measurement in the \( H \rightarrow ZZ \rightarrow 4\ell \) channel is evaluated using the variable \( \Delta m_Z \equiv m_{H/} - m_{H/}^{\text{exp}} \) as the parameter of interest, with all other parameters, including \( m_H \), profiled. Similarly, the compatibility of the ATLAS combined mass measurement in the two channels with the CMS combined measurement in the two channels is evaluated using the variable \( \Delta m^{\text{exp}} \equiv m_{H/}^{\text{ATLAS}} - m_{H/}^{\text{CMS}} \).

The observed results, \( \Delta m_Z = -0.1 \pm 0.5 \) GeV and \( \Delta m^{\text{exp}} = 0.4 \pm 0.5 \) GeV, are both consistent with zero within 1\( \sigma \). The difference between the mass values in
TABLE I. Systematic uncertainties $\delta m_H$ (see text) associated with the indicated effects for each of the four input channels, and the corresponding contributions of ATLAS and CMS to the systematic uncertainties of the combined result. “ECAL” refers to the electromagnetic calorimeters. The numbers in parentheses indicate expected values obtained from the prefit Asimov data set discussed in the text. The uncertainties for the combined result are related to the values of the individual channels through the relative weight of the individual channel in the combination, which is proportional to the inverse of the respective uncertainty squared. The top section of the table divides the sources of systematic uncertainty into three classes, which are discussed in the text. The bottom section of the table shows the total systematic uncertainties estimated by adding the individual contributions in quadrature, the total systematic uncertainties evaluated using the nominal method discussed in the text, the statistical uncertainties, the total uncertainties, and the analysis weights, illustrative of the relative weight of each channel in the combined $m_H$ measurement.

<table>
<thead>
<tr>
<th>Scale uncertainties:</th>
<th>ATLAS</th>
<th>CMS</th>
</tr>
</thead>
<tbody>
<tr>
<td>ATLAS ECAL nonlinearity or CMS photon nonlinearity</td>
<td>0.14 (0.16)</td>
<td>0.10 (0.13)</td>
</tr>
<tr>
<td>Material in front of ECAL</td>
<td>0.15 (0.13)</td>
<td>0.07 (0.07)</td>
</tr>
<tr>
<td>ECAL longitudinal response</td>
<td>0.12 (0.13)</td>
<td>0.02 (0.01)</td>
</tr>
<tr>
<td>ECAL lateral shower shape</td>
<td>0.09 (0.08)</td>
<td>0.06 (0.06)</td>
</tr>
<tr>
<td>Photon energy resolution</td>
<td>0.03 (0.01)</td>
<td>0.01 (&lt;0.01)</td>
</tr>
<tr>
<td>ATLAS H → $\gamma\gamma$ vertex and conversion reconstruction</td>
<td>0.05 (0.05)</td>
<td>0.01 (0.01)</td>
</tr>
<tr>
<td>Z → ee calibration</td>
<td>0.05 (0.04)</td>
<td>0.05 (0.05)</td>
</tr>
<tr>
<td>CMS electron energy scale and resolution</td>
<td>0.03 (0.02)</td>
<td>0.12 (0.09)</td>
</tr>
<tr>
<td>Muon momentum scale and resolution</td>
<td>0.03 (0.04)</td>
<td>0.11 (0.10)</td>
</tr>
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<table>
<thead>
<tr>
<th>Other uncertainties:</th>
<th>ATLAS</th>
<th>CMS</th>
</tr>
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<tbody>
<tr>
<td>ATLAS H → $\gamma\gamma$ background modeling</td>
<td>0.04 (0.03)</td>
<td>0.01 (0.01)</td>
</tr>
<tr>
<td>Integrated luminosity</td>
<td>0.01 (&lt;0.01)</td>
<td>0.01 (&lt;0.01)</td>
</tr>
<tr>
<td>Additional experimental systematic uncertainties</td>
<td>0.03 (&lt;0.01)</td>
<td>0.01 (&lt;0.01)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Theory uncertainties:</th>
<th>ATLAS</th>
<th>CMS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Systematic uncertainty (sum in quadrature)</td>
<td>0.27 (0.27)</td>
<td>0.15 (0.17)</td>
</tr>
<tr>
<td>Systematic uncertainty (nominal)</td>
<td>0.27 (0.27)</td>
<td>0.15 (0.17)</td>
</tr>
<tr>
<td>Statistical uncertainty</td>
<td>0.43 (0.45)</td>
<td>0.31 (0.32)</td>
</tr>
<tr>
<td>Total uncertainty</td>
<td>0.51 (0.52)</td>
<td>0.34 (0.36)</td>
</tr>
<tr>
<td>Analysis weights</td>
<td>19% (22%)</td>
<td>40% (46%)</td>
</tr>
</tbody>
</table>

The compatibility of the signal strengths from ATLAS and CMS is evaluated through the ratios $\lambda_{\text{expt}} = \mu_{\text{ATLAS}} / \mu_{\text{CMS}}$, $\lambda_{\text{expt}} = \mu_{\text{ATLAS}} / \mu_{\text{CMS}}$, and $\lambda_{\text{expt}} = \mu_{\text{ATLAS}} / \mu_{\text{CMS}}$. For this purpose, each ratio is individually taken to be the parameter of interest, with all other nuisance parameters profiled, including the remaining two ratios for the first two tests. We find $\lambda_{\text{expt}} = 1.21^{+0.30}_{-0.24}$, $\lambda_{\text{expt}} = 1.3^{+0.3}_{-0.2}$, and $\lambda_{\text{expt}} = 1.3^{+0.3}_{-0.2}$, all of which are consistent with unity within 1σ. The ratio $\lambda = \mu_{\text{VBF}+VH} / \mu_{\text{VBF}+VH}$ is omitted because the ATLAS mass measurement in the $H \rightarrow \gamma\gamma$ channel is not sensitive to $\mu_{\text{VBF}+VH} / \mu_{\text{VBF}+\tilde{t}H}$. The correlation between the signal strength and the measured mass is explored with 2D likelihood scans as functions of $\mu$ and $m_H$. The three signal strengths are assumed to be the same: $\mu_{\text{VBF}+\tilde{t}H} = \mu_{\text{VBF}+VH} = \mu_{\text{expt}}$, and thus the ratios of the production cross sections times branching fractions are constrained to the SM.
predictions. Assuming that the negative log-likelihood ratio 
−2 ln Λ(μ, m_H) is distributed as a χ^2 variable with two
degrees of freedom, the 68% confidence level (C.L.)
confidence regions are shown in Fig. 4 for each individual
measurement, as well as for the combined result.

In summary, a combined measurement of the Higgs
boson mass is performed in the H \rightarrow γγ and H \rightarrow ZZ \rightarrow 4ℓ
channels using the LHC Run 1 data sets of the ATLAS
and CMS experiments, with minimal reliance on the
assumption that the Higgs boson behaves as predicted
by the SM.

The result is

\[ m_H = 125.09 \pm 0.24 \text{ GeV} \]
\[ = 125.09 \pm 0.21 \text{ (stat) } \pm 0.11 \text{ (syst) GeV}, \]  

where the total uncertainty is dominated by the statistical
term, with the systematic uncertainty dominated by effects
related to the photon, electron, and muon energy or
momentum scales and resolutions. Compatibility tests are
performed to ascertain whether the measurements are
consistent with each other, both between the different decay
channels and between the two experiments. All tests on
the combined results indicate consistency of the different
measurements within 1σ, while the four Higgs boson mass
measurements in the two channels of the two experiments
agree within 2σ. The combined measurement of the Higgs
boson mass improves upon the results from the individual
experiments and is the most precise measurement to date of
this fundamental parameter of the newly discovered particle.

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BMWF and FWF (Austria); ANAS (Azerbaijan);
SSTC (Belarus); FNRS and FWO (Belgium); CNPq,
CAPES, FAPERJ, and FAPESP (Brazil); MES

FIG. 4 (color online). Summary of likelihood scans in the 2D
plane of signal strength μ versus Higgs boson mass m_H for the
ATLAS and CMS experiments. The 68% C.L. confidence regions
of the individual measurements are shown by the dashed curves
and of the overall combination by the solid curve. The markers
indicate the respective best-fit values. The SM signal strength is
indicated by the horizontal line at μ = 1.
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[14] ATLAS Collaboration, Measurement of the Higgs boson mass from the \( H \rightarrow \gamma\gamma \) and \( H \rightarrow ZZ' \rightarrow 4\ell \) channels in \( pp \) collisions at center-of-mass energies of 7 and 8 TeV with the ATLAS detector, Phys. Rev. D 90, 052004 (2014).


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<tr>
<th>Institution</th>
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<td>Piscataway, New Jersey, USA</td>
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